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EX 3







# ERRATA FOR LEE'S TABLES

By PROFESSOR BARTLETT.

Page 20.—Strike out lines 14 and 15 from top, and which give the length of a parabolic arc, and substitute :

$$y \cdot \sqrt{1 + \frac{4x^2}{y^2}} + 2, 3 \times \frac{y^2}{2x} \cdot \text{Log} \left[ \frac{2x}{y} + \sqrt{1 + \frac{4x^2}{y^2}} \right].$$

In which  $x$  is the abeissa, and  $y$  the ordinate—the origin being at the vertex.

Pages 224–231.—Replace the whole of Art. XVII by the following :

## XVII. *Longitude by Lunar Culminations.*

### 1. Make

$l$  = true longitude sought,

$l'$  = approximate longitude,

$m$  = observed change, in right ascension, of the moon's bright limb between the first meridian and that sought,

$m'$  = computed change in same, by interpolation.

$V$  = rate of motion, in right ascension, of the moon's bright limb, when on the meridian  $l'$ .

$I$  = the constant difference between the values of the independent variable, or arguments, corresponding to the consecutive tabulated values of the right ascension of the moon.

Then :

$$l = l' + I \cdot \frac{m - m'}{V} \quad . \quad . \quad . \quad . \quad . \quad (1)$$

OXF



2. *Interpolation.*—Take the following scheme, viz :

I	F	$\Delta_1$	$\Delta_2$	$\Delta_3$	$\Delta_4$	$\Delta_5$
$t'''$	$a'''$	$b''$				
$t''$	$a''$	$b'$	$c''$			
$t'$	$a'$	$b$	$c'$	$d'$	$e'$	
$t$	$a$	$b$	$c$	$d$	$e$	$f$
$t_{,}$	$a_{,}$	$b_{,}$	$c_{,}$	$d$		
$t_{,,}$	$a_{,,}$	$b_{,,}$	$c_{,,}$			
$t_{,,,}$	$a_{,,,}$					

In which the column I contains the independent variable, or argument, as time, terrestrial longitude, degrees, and the like ; F the value of the function of this variable, as found in any set of tables ;  $\Delta_1$ ,  $\Delta_2$ , etc., the first, second, etc., order of differences of these functions.

Make

$s$  = the value of the function corresponding to any value  $t_{,}$ , between  $t'$  and  $t$  ;

$$\left. \begin{aligned} t &= \frac{t_{,} - t'}{t - t'} ; \\ a &= \frac{a' + a_{,}}{2} , \\ c &= \frac{c' + c_{,}}{2} , \\ e &= \frac{e' + e_{,}}{2} ; \end{aligned} \right\} \dots \dots \dots (2)$$

Then, according to Bessel, Ast. Nach. No. 30 :

$$s = a + \frac{t - \frac{1}{2}}{1} \cdot b + \frac{t(t-1)}{1 \cdot 2} \cdot c + \frac{t(t-1)(t-\frac{1}{2})}{1 \cdot 2 \cdot 3} \cdot d \\ + \frac{(t+1) \cdot t \cdot (t-1)(t-2)}{1 \cdot 2 \cdot 3 \cdot 4} \cdot e + \text{etc.}$$

Or, making,

$$\left. \begin{aligned} \Delta_1 &= b, \\ \Delta_2 &= \frac{c' + c_i}{2}, \\ \Delta_3 &= d, \\ \Delta_4 &= \frac{e' + e_i}{2}, \end{aligned} \right\} \dots \dots \dots (3)$$

$$s = a' + t \Delta_1 + \frac{t(t-1)}{1 \cdot 2} \cdot \Delta_2 + \frac{t(t-1)(t-\frac{1}{2})}{1 \cdot 2 \cdot 3} \cdot \Delta_3 \\ + \frac{(t+1) \cdot t \cdot (t-1)(t-2)}{1 \cdot 2 \cdot 3 \cdot 4} \cdot \Delta_4 + \text{etc.}$$

or by the ascending powers of  $t$ .

$$s = a' + At + Bt^2 + Ct^3 + Dt^4 + \text{etc.}, \quad (4)$$

in which, stopping at the fourth differences,

$$\left. \begin{aligned} A &= \Delta_1 - \frac{1}{2} \Delta_2 + \frac{1}{12} \Delta_3 - \frac{1}{24} \Delta_4, \\ B &= \frac{1}{2} \Delta_2 - \frac{1}{4} \Delta_3 + \frac{1}{24} \Delta_4, \\ C &= \frac{1}{6} \Delta_3 - \frac{1}{24} \Delta_4, \\ D &= \frac{1}{24} \Delta_4. \end{aligned} \right\} \dots \dots (5)$$

Also,

$$V = \frac{ds}{dt} = A + 2Bt + 3Ct^2 + 4Dt^3. \quad (6)$$

$$m' = s - a' = At + Bt^2 + Ct^3 + Dt^4. \quad (7)$$

The value of  $m$  may be obtained either from observations on the two meridians, or by observations on one and the tabulated results under the head of Moon Culminations in the Nautical Almanac, which may be used as actual observations on the meridian of the ephemeris.

3. *Example.*—Let

$$l' = 4^{\text{h}} 55^{\text{m}} 50^{\text{s}} \text{ west from Greenwich,}$$

and suppose the following transits with a chronometer marking sidereal time. The *error* of the time-keeper is not material, and the transit is very nearly in the meridian, viz :

Feb. 18, $\zeta$ Geminorum	$6^{\text{h}} 54^{\text{m}} 41^{\text{s}}.75$	
$\delta$ Geminorum	$7 \ 10 \ 38.97$	
$\delta$ 's 1st Limb	— — —	$7^{\text{h}} 38^{\text{m}} 06^{\text{s}}.76$
$\zeta$ Cancrī	$8 \ 03 \ 06.11$	
	$3)22 \ 08 \ 26.83$	$7 \ 22 \ 48.948$
		$0 \ 15 \ 17.817$
Chronometer rate + $3^{\text{s}}$ daily		$- 0 \ 03 \ 18 \dots 6^{\text{h}} 15^{\text{m}} 17^{\text{s}}.785$

The corresponding observations at Greenwich,  
as given by the Naut. Almanac, are :

Feb. 18, $\zeta$ Geminorum	$6^{\text{h}} 54^{\text{m}} 57^{\text{s}}.41$	
$\delta$ Geminorum	$7 \ 10 \ 54.36$	
$\delta$ 's 1st Limb	— — —	$7^{\text{h}} 27^{\text{m}} 47^{\text{s}}.66$
$\zeta$ Cancrī	$8 \ 03 \ 21.44$	
	$3)22 \ 09 \ 13.21$	$7 \ 23 \ 04.403$
		$0^{\text{h}} 04^{\text{m}} 43^{\text{s}}.257$
		$m = 634^{\text{s}}.528 = 0 \ 10 \ 34.528$

Next compute this increase from Nautical Almanac. The right ascensions of the moon are given in that work for the upper and lower passages over the meridian of Greenwich. The independent variable is, therefore, terrestrial longitude, of which the unit is one hour, and the intervals between the consecutive tabulated values of its function, 12. The increase to be computed is for the interval of passage from the upper meridian of Greenwich to that  $4^{\text{h}} 55^{\text{m}} 50^{\text{s}}$  west. Now, according to the scheme and Eqs. (2), (3) and (5),

$\Delta_1$	AR. L's 1st Limb, Naut. Almanac.	$\Delta_1$	$\Delta_2$	$\Delta_3$	$\Delta_4$	
17 U	6 <sup>h</sup> 35 <sup>m</sup> 55 <sup>s</sup> .73	+26 <sup>m</sup> 00 <sup>s</sup> .54				$t = \frac{h_s - t'}{t_s - t'} = \frac{4^h 55^m 50^s}{12^h}$
" L	7 01 56.57	+25 51.39	9 <sup>s</sup> .15	-1 <sup>s</sup> .06		
18 U	7 27 47.66		$e' = -10.21$	$d = -0.25$	$e' = +0.81$	
" L	7 53 28.84	$b = +25 41.18$	$e_j = -10.46$	$-0.59$	$e_j = +0.84$	
19 U	8 18 59.56	+25 30.72	- 9.87			$\log t = 9.6137147$
" L	8 44 20.41	+25 20.85				
Sum of differences . . . .		2 <sup>h</sup> 08 <sup>m</sup> 24 <sup>s</sup> .68	- 0 <sup>m</sup> 39 <sup>s</sup> .69	- 0 <sup>s</sup> .72	+1 <sup>s</sup> .65	$\Delta_1 = 25^m 41^s.180$
Top of left column . . . .		6 35 55.73	26 00.54	- 9.15	-1 <sup>s</sup> .06	$\Delta_2 = - 10.335$
Check-Sum = bottom left col.		8 44 20.41	25 20.85	- 9.87	+0.59	$\Delta_3 = - 0.250$
						$\Delta_4 = + 0.825$
						$\log A = 3.1893180$
						$\log B = 0.7108786$
						$\log C = 9.0374265$
						$\log D = 8.5910646$

$$A = 25^m 41^s.180 + 5^s.167 - 0^s.021 + 0^s.068 = + 1546^s.394.$$

$$B = . - 5.167 + 0.062 - 0.034 = - 5.139.$$

$$C = . . . - 0.041 - 0.068 = - 0.109.$$

$$D = . . . + 0.034 = + 0.034.$$

Then Eq. (7).	A Log	3.1893180	
	<i>t</i> "	9.6137147	
		<u>2.8030327</u>	Nos. . . + 635°.337
	B Log	0.7108786	
	<i>t</i> ² "	9.2274294	
		<u>9.9383080</u>	Nos. . . - 0.867
	C Log	9.0374265	
	<i>t</i> ³ "	8.8411441	
		<u>7.8785706</u>	Nos. . . - 0.007
	D Log	8.5910646	
	<i>t</i> ⁴ "	8.4548588	
		<u>7.0459234</u>	Nos. . . + 0.001
	<i>m</i> ' =	. . . . .	<u>634.464</u>

And Eq. (6)	A	. . . . .	1546°.394
	B Log	0.7108786	
	<i>t</i> "	9.6137147	
	2 "	0.3010300	
		<hr/>	
		0.6256233	Nos. . . -- 4.222
	C Log	9.0374265	
	<i>t</i> <sup>2</sup> "	9.2274294	
	3 "	0.4771213	
		<hr/>	
		8.7419772	Nos. . . — 0.055
	D Log	8.5910646	
	<i>t</i> <sup>3</sup> "	8.8411441	
	4 "	0.6020600	
		<hr/>	
		8.0342687	Nos. . . + 0.011.
	<i>V</i> =	. . . . .	<hr/>
			1542.128

And Eq. (1)

$I = 12^h$	. . . . .	Log	4.6354837
$m - m' = 0^s.064$	. . . . .	"	8.8061800
$V = 1542^s.128$	. . . . .	" ac.	6.8118797
$1^s.792$	. . . . .		0.2535434

Whence

$$l = 4^h 55^m 50^s + 1^s.792 = 4^h 55^m 51^s.792.$$

If  $m$  be the *observed* increase of right ascension between any meridian not the first, (but of which the longitude is well known,) and the meridian sought, interpolate the increase  $m$ , for the known meridian as well as  $m'$  for that sought. Then for  $m - m'$ , in Eq. (1), substitute  $m - \overline{m' - m}$ , and the result, will be the corrected longitude from the first meridian, as before.

It often happens that two observers do not use the same number of wires, or do not observe the same number of stars at the two places. In such cases the observed increase of the right ascension of the moon's limb requires a correction, which Mr. Walker deduces as follows, from Gauss's method :

For the Eastern observatory and western station, respectively, let

$A'$  and  $A$  = the observed AR of a star,

$E = A' - A$  for the same star,

$E'$  = a similar value for another star,

$l$  and  $l'$  = the number of wires on which each limb was observed,

$\alpha$  and  $\alpha'$  = similar values for a star,

$$\lambda = \frac{l l'}{l + l'}, \text{ for the moon's limb,}$$

$$u = \frac{\alpha \alpha'}{\alpha + \alpha'}, \text{ for one star.}$$

$u'$  = a similar value for another star,

$\Sigma$  = symbol to denote the aggregate of similar quantities,

$\varepsilon$  = the correction required.

Then

$$\varepsilon = \frac{\Sigma \left( E \frac{\lambda u}{\lambda + u} \right)}{\Sigma \frac{\lambda u}{\lambda + u}};$$

$$L = l + I \frac{m - m' + \varepsilon}{V}.$$

Also, calling  $W$ , the *weight* of each day's comparison,

$$W = \frac{\sigma \lambda}{(\sigma + \lambda) z^2};$$

in which  $z$  is the same as  $\frac{I}{V}$ , and  $\sigma = u + u' + u''$ , etc.

For the weight of the result of all the comparisons, we have

$$\Sigma W = \Sigma \frac{\sigma \lambda}{(\sigma + \lambda) z^2}.$$

Let  $e$  denote the probable error of observation, and  $E$  the probable error of the final result ; then,

$$E = \frac{e}{\sqrt{\Sigma \frac{\sigma \lambda}{(\sigma + \lambda) z^2}}}$$

It also frequently happens that the moon cannot be observed on the middle wire, in which case she is far enough from the meridian to have a sensible parallax in right ascension ; and, as it may be very desirable not to lose the observation, this parallax must be computed and applied to the

hour angle from the middle wire, which is supposed to be nearly coincident with the meridian.

Denoting this parallax in right ascension by  $p$ , the horizontal parallax by  $w$ , the latitude of the place of observation by  $\phi$ , and the true declination of the moon by  $\delta$ , we have from the ordinary series for the parallax in right ascension, neglecting the terms after the first, which would in this case be insignificant,

$$p = \theta \sin w \cos \phi \sec \delta,$$

in which  $\theta$ , is the hour angle, or equatorial interval in sidereal time from the lateral wire on which the moon is observed to the central wire; so that, at the instant of observation, the actual distance of the moon's limb from the central wire is:

$$\theta - \theta \sin w \cos \phi \sec \delta,$$

and the reduction to meridian or middle wire will be

$$\pm \frac{\theta}{\cos \delta} \cdot \frac{1 - \sin w \cos \phi \sec \delta}{1 - 0.00277m},$$

in which  $m$ , is the motion of the moon in right ascension in one day, expressed in degrees. The upper sign is to be used when the observation is on a wire *before*, and the lower *after* the middle wire.

In what precedes, the approximate longitude  $l'$  is supposed to be known. When this is not the case, it may be found from

$$l' = 12^h \frac{m}{\Delta'}.$$

and the interpolation is then to be made for this value of  $l'$  to obtain the value of  $m'$ .





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A COLLECTION  
OF  
TABLES AND FORMULÆ  
USEFUL IN  
SURVEYING,  
GEODESY, AND PRACTICAL ASTRONOMY,  
INCLUDING  
ELEMENTS FOR THE PROJECTION OF MAPS.

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PREPARED FOR THE USE OF THE  
CORPS OF TOPOGRAPHICAL ENGINEERS,  
BY  
CAPTAIN T. J. LEE,  
Topographical Engineers, U. S. Army.

SECOND EDITION, WITH ADDITIONS.

WASHINGTON:  
TAYLOR & MAURY.  
GIDEON AND CO., PRINTERS,  
1853.

new

BUREAU OF TOPOGRAPHICAL ENGINEERS,

*Washington, April 4, 1853.*

SIR: The edition of Topographical Papers, No. 3, a collection of Tables and Formulæ, etc., prepared by you in 1849, having become exhausted, and the great use of the collection being fully proved, the Hon. Secretary of War, appreciating its value, has authorized the printing of a new edition, with the corrections and additions which have been suggested by experience.

You will give this your immediate attention.

Respectfully, sir,

Your obedient servant,

J. J. ABERT,

*Col. Corps T. E.*

CAPT. T. J. LEE,

*Corps Top'l Eng'rs, Washington.*

TO COL. J. J. ABERT,

*Chief Corps of Topographical Engineers.*

SIR : I have endeavored, in the following pages, to comply with your instructions by presenting, in as condensed a form as practicable, such Tables and Formulæ as may prove most useful to an officer engaged in the active duties of a survey.

In the selection of the matter it has been my aim to present the best methods, as far as they have been practised by us, or may be applicable to the nature of our duties, in such forms as to be convenient for reference, and still secure a high degree of accuracy in the reduction of such observations as may be requisite for the minute survey of a limited extent of country, as well as for the exact determination of Geographical Positions or for distant Explorations.

With such a subject I can lay claim to but little that is original, and although aware of the many imperfections in this Collection, I still trust that it may not be without its utility, and that as a *Manual* of easy reference it may meet the wants of my brother officers.

Although every precaution has been taken to ensure accuracy of print, it is not improbable that some errors may have escaped correction. A table of errata is appended, and I would be obliged by the communication of any others that may be detected.

Very respectfully,

Your obedient servant,

THOMAS J. LEE,

*Cap. Top. Engineers*

WASHINGTON, August 8, 1849.

## ERRATA.

- Page 9.  $10^{-7} \sim 10^{-8}$  square feet = 1 square mile.  
 Page 64:  $Dp = 5.9 \sim 57556^\circ \cos \phi - (2.00835) \cos 3\phi + \text{etc.};$   
 Page 145:  $\phi = 0$  in 24 hours, read  $3 = 56^\circ.555$ .

## PREFATORY.

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The following explanations of the sources from which the several portions of this Collection were derived, will serve to establish the degree of confidence with which each may be received.

### PART I.

- Pp. 1—3. Baily, *Astronomical Tables and Formulæ*.  
Francœur, *Géodésie*, Paris, 1840.
4. Francœur, *Géodésie*.
- 5—7. Bégat, *Traité de Géodésie*, Paris, 1839.
- 8—14. Weights and measures. Those of the United States will be found in the Report of Professor Bache, Superintendent of Weights and Measures, July 30, 1848, Ex. Doc., No. 84, 30th Congress, 1st session. The remaining part of the article is from Brande's *Dictionary of Science and Art*, American edition, the quantities having been compared, when practicable, with Alexander's *Universal Dictionary of Weights and Measures*, Baltimore, 1850, and with the tables in Appleton's *Dictionary of Mechanics and Engineering*.
- 14—15. These tables are from the *Edinburg Philosophical Journal* of October, 1837.
- 16—17. Abridged from tables in Hulsse's *Sammlung Mathematischer Tafeln*, Leipsic, 1840, with the addition of the relation of Spanish and Mexican measures.
18. Claudel, *Aide Memoire des Ingenieurs*, etc., Paris, 1849. The length of the Spanish vara was compared with its value given in Francœur, Bégat, Brande, and Hulsse's works.
19. Ordnance Manuel, 1850.
- 20—22. Bégat, *Géodésie*.



- 
- Pp. 23. Mc Niel's Railway Tables, London, 1833. Beardmore, Hydraulic and other Tables, London, 1852.  
 24—25. Storrow on Water Works, Boston, 1833.  
 26—30. Railroad Manual, by Brevet Lieut. Col. Long, Corps Topographical Engineers, Baltimore, 1829.  
 31—32. Davies' Surveying.  
 33—47. Abridged from the Traverse Tables of Captain J. T. Boileau, Bengal Engineers.  
 48—49. Beardmore, Hydraulic and other tables, London, 1852.  
 50. Regulations of the Subsistence Department.

## PART II.

53. Bégat Géodésie.  
 54—55. Galbraith, Mathematical Tables and Formulæ, Edinburgh, 1834.  
 56. Francœur, Géodésie.  
 57. Baily, Astronomical Tables and Formulæ, London, 1827.  
 58—59. Galbraith, Mathematical Tables, etc.  
 60. Baily, Astronomical Tables.—Bégat, Géodésie.  
 61. These values were carefully compared with the original in the *Astronomische Nachrichten*, No. 438.  
 62—64. I have adopted the yard as a unit, it being the unit of our lineal measures, and have, in the text, given the reasons for adhering to Kater's value of the metre. I have also preferred the *established* ratio of the metre to the toise, to that derived from Mr. Hassler's comparisons. (See Hassler's report of 1832, Doc. No. 299, 22d Congress, 1st session.)

In reducing Bessel's Terrestrial Elements to English yards, and in other computations hereafter to be noticed, I was fortunate in securing the services of Mr. John Downes, now attached to the American Nautical Almanac establishment, whose well known reputation is the surest evidence of their accuracy. These reductions were also compared with a computation of my own.

- Pp. 65—69. These are in the form given in Bégat, Géodésie. They are sufficiently accurate for our ordinary wants; for very extended operations, it is not to be presumed that the officer would make this collection his only guide.
- 70—71. At the solicitation of several officers I have introduced into this edition examples to explain the application of many of the formulæ.
- 72—77. The values of  $N$  and  $R$ , etc., within the limiting parallels of the territory of the United States, were computed by Lieut. Thom, Corps Topographical Engineers; afterwards by Mr. Downes, and the two carefully compared.
- 78—80. Bégat, Géodésie.
- 81—82. Trigonometrical surveying—Lieutenant Frome, Royal Engineers.
- 83—86. Baily, Astronomical Tables and Formulæ.
- 87—94. Abridged from Guyot's Meteorological Tables—prepared for the Smithsonian Institution. 1852.
95. Adapted, from Guyot's tables, to English inches and Fahrenheit's Thermometer scale.
- 96—98. The first method is from a manuscript of the late J. N. Nicollet, who probably obtained it from Mr. Hassler, as it is the projection in use at the Coast Survey office. The remaining methods will be found in Francœur, Géodésie.
- 99—128. The whole of these tables were computed, under my direction, for the Bureau of Topographical Engineers, by Mr. Downes. They were, occasionally, compared with similar quantities (in metres) in the manuscript tables in the Coast Survey office.
- Appendix. Magnetical observations—from the Magnetical Instructions prepared by order of the British Government, by Lieut. J. C. B. Riddel, Royal Artillery. 1844.
- 129—137.
138. Eighth report of the British Association, 1838, page 91.

## PART III.

- Pp. 141—143. Francœur, *Astronomie Pratique*—Baily, *Ast. Tables and Formulæ*.
- 144—145. Baily, *Ast. Tables and Formulæ*.
- 146—157. Downes, *U. S. Almanac*, 1845. Compared, also, with Baily, *Ast. Tables* whenever practicable.
- 158—160. This, with subsequent examples of Sextant observations, was obtained through the kindness of Brevet Lieut. Col. J. D. Graham, Corps Topographical Engineers, from the records of the Northeastern Boundary Survey.
- 161—169. Baily, *Ast. Tables*.
- 170—172. Lieut. Col. Graham.
173. *American Almanac*; Downes's *U. S. Almanac*.
- 174—181. Ivory's Refractions, from Galbraith, *Math. Tables and Formulæ*. The zenith distances are changed to altitudes, as more convenient for our purposes.
- 182—184. Baily, *Ast. Tables and Form.*; Simms on *Math. Instruments*, London, 1836.
185. Original. This table, and the one on page 188, will be found convenient in *setting up* a Transit Instrument.
- 186—187. Extracted from some of my own observations whilst attached to the Coast Survey.
- 189—191. Francœur, *Astronomie Pratique*.
- 192—199. Baily, *Ast. Tables and Formulæ*.
- 200—202. Lieut. Col. J. D. Graham.
203. Francœur, *Astronomie Pratique*.
- 204—206. Lieut. Col. J. D. Graham.
- 207—210. From a manuscript translation of an article by Prof. Hanson, *Ast. Nach.*, No. 143. The method of *reversals*, described by Struve in his notice of the Rhapsold Instrument, *Ast. Nach.*, Vol. 20, is undoubtedly the best; but, for the want of a reversing apparatus, is ill suited to such Transit Instruments as are usually carried into the field.

- 
- Pp. 211—214. From a description, by myself, of the use of the zenith and equal altitude Telescope, printed for the Bureau of Topographical Engineers in 1848.
- 215—218. Francœur, Ast. Prat.; Simms on Math. Instruments. Reduction to elongation and corrections for level, R. H. Fauntleroy, U. S. Coast Survey.
218. Correction for *Run*. Henderson's Edinb. Ast. Observations.
- 219—221. Downes, U. S. Almanac. Francœur, Ast. Prat.
- 222—223. Frome, Trigonometrical Surveying.
- 224—231. Downes, U. S. Almanac; Walker, Trans. Am. Phil. Society, Vol. VI; Prof. Bartlett on Longitude by lunar culminations, printed for the Bureau of Topographical Engineers.
- 232—237. Gummere's Astronomy.
- 238—240. From a manuscript explanation, by Prof. Bartlett, of an article by Encke, translated in Taylor's Scientific Memoirs, part VII.
- 241—242. The authorities are given in the text.

T. J. L.



# CONTENTS.



## PART 1.—*Miscellaneous.*

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**TABLES AND FORMULÆ.**

**PART I.**

**MISCELLANEOUS.**

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# TRIGONOMETRY.

## I. Equivalent Expressions.

$$\sin^2 x + \cos^2 x = 1.$$

$$\sin x = \cos x \cdot \tan x$$

$$= \frac{\cos x}{\cot x}$$

$$= \sqrt{1 - \cos^2 x}$$

$$= 2 \sin \frac{1}{2} x \cdot \cos \frac{1}{2} x$$

$$= \frac{\tan x}{\sqrt{1 + \tan^2 x}}$$

$$= \frac{1}{\operatorname{cosecant} x}$$

$$\cos x = \frac{\sin x}{\tan x}$$

$$= \sin x \cdot \cot x$$

$$= \sqrt{1 - \sin^2 x}$$

$$= \cos^2 \frac{1}{2} x - \sin^2 \frac{1}{2} x$$

$$= \frac{1}{\secant x}$$

$$\tan x = \frac{\sin x}{\cos x}$$

$$= \frac{1}{\cot x}$$

$$= \frac{\sin x}{\sqrt{1 - \sin^2 x}}$$

$$= \frac{\sin 2 x}{1 + \cos 2 x}$$

$$\operatorname{Cotang} x = \frac{1}{\tan x}$$

$$\text{Secant } x = \frac{1}{\cos x}$$

$$\text{Cosecant } x = \frac{1}{\sin x}$$

$$\text{Versed sin } x = 1 - \cos x = 2 \sin^2 \frac{1}{2} x$$

$$\text{Co-versed sin } x = 1 - \sin x$$

$$\text{Chord } x = 2 \sin \frac{1}{2} x$$

$$\sin (A \pm B) = \sin A \cos B \pm \sin B \cos A$$

$$\cos (A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\sin 2A = 2 \sin A \cos A$$

$$\begin{aligned} \cos 2A &= 2 \cos^2 A - 1 = 1 - 2 \sin^2 A \\ &= \cos^2 A - \sin^2 A \end{aligned}$$

$$2 \cos^2 \frac{1}{2} A = 1 + \cos A$$

$$2 \sin^2 \frac{1}{2} A = 1 - \cos A$$

$$\text{Tang } (A \pm B) = \frac{\text{tang } A \pm \text{tang } B}{1 \mp \text{tang } A \text{ tang } B}$$

$$\text{Tang } \frac{1}{2} A = \sqrt{\frac{1 - \cos A}{1 + \cos A}} = \frac{1 - \cos A}{\sin A}$$

$$\sin A \pm \sin B = 2 \sin \frac{1}{2} (A \pm B) \cos \frac{1}{2} (A \mp B)$$

$$\cos A + \cos B = 2 \cos \frac{1}{2} (A + B) \cos \frac{1}{2} (A - B)$$

$$\cos A - \cos B = 2 \sin \frac{1}{2} (A + B) \sin \frac{1}{2} (B - A)$$

$$\sin^2 A - \sin^2 B = \sin (A + B) \sin (A - B)$$

$$\cos^2 A - \sin^2 B = \cos (A + B) \cos (A - B)$$

$$\text{Tang } A \pm \text{tang } B = \frac{\sin (A \pm B)}{\cos A \cos B}$$

$$\text{Cot } A \pm \text{cot } B = \frac{\sin (A \pm B)}{\sin A \sin B}$$

$$\frac{\sin A + \sin B}{\sin A - \sin B} = \frac{\tan \frac{1}{2}(A+B)}{\tan \frac{1}{2}(A-B)}$$

$$\frac{1 \pm \sin A}{1 \mp \sin A} = \tan^2(45^\circ \pm \frac{1}{2}A)$$

$$\frac{1 \pm \sin A}{\cos A} = \tan(45^\circ \pm \frac{1}{2}A)$$

## II. Trigonometrical Series.

$$\sin A = A - \frac{A^3}{2.3} + \frac{A^5}{2.3.4.5} - \frac{A^7}{2.3....7} + \text{etc.}$$

$$\cos A = 1 - \frac{A^2}{2} + \frac{A^4}{2.3.4} - \frac{A^6}{2....6} + \text{etc.}$$

$$\begin{aligned} \text{Arc } A &= \sin A + \frac{\sin^3 A}{2.3} + \frac{3 \sin^5 A}{2.4.5} + \frac{3.5 \sin^7 A}{2.4.6.7} \text{ etc.} \\ &= \tan A - \frac{1}{3} \tan^3 A + \frac{1}{5} \tan^5 A - \frac{1}{7} \tan^7 A \dots \end{aligned}$$

$$\log \sin A = \log A + \log \left(1 - \frac{x^2}{6} + \frac{x^4}{120} - \text{etc.}\right)$$

$$= \log A - M \left( \frac{x^2}{6} + \frac{x^4}{180} + \frac{x^6}{2835} \right)$$

$$M = \text{logarithmic modulus} = 0.4342945 \dots$$

$$\log M = 9.6377843113 \dots$$

## III. Table of signs of Trigonometrical lines.

| Quadrants.    | Sine.                                                           | Cosine. | Tang. | Cot. | Secant. | Cosecant. |
|---------------|-----------------------------------------------------------------|---------|-------|------|---------|-----------|
| 1. 5. 9.      | $\left\{ \begin{array}{c} + \\ + \\ - \\ - \end{array} \right.$ | +       | +     | +    | +       | +         |
| 2. 6. 10.     |                                                                 | -       | -     | -    | -       | +         |
| 3. 7. 11.     |                                                                 | -       | +     | +    | -       | -         |
| 4. 8. 12, &c. |                                                                 | +       | -     | -    | +       | -         |



IV. *Ratio of the circumference of a circle to its diameter.*

$$\pi = 3.14159\ 26535\ 898\ \dots$$

$$\text{Log } \pi = 0.49714\ 98726\ 941\ \dots$$

The radius being unity, the number of degrees in an arc equal to radius =  $r^\circ = \frac{180^\circ}{\pi} = \frac{1}{\text{arc } 1^\circ} = 57^\circ.29578 = 57^\circ.17'.44''.8$ .

The number of minutes =  $r' = \frac{10800'}{\pi} = \frac{1}{\text{arc } 1'} \text{ or } \frac{1}{\sin 1'} = 3437'.74677$ .

The number of seconds =  $r'' = \frac{648000''}{\pi} = \frac{1}{\sin 1''} = 206264''.80625$ .

$$\text{Log } r^\circ = 1\ 75812\ 26324\ 09172$$

$$\text{Comp log } r^\circ = 8.24187\ 73675\ 90828$$

$$\text{Log } r' = 3.53627\ 38827\ 92816$$

$$\text{Comp log } r' = 6.46372\ 61172\ 07184 = \text{log } \sin 1'$$

$$\text{Log } r'' = 5.31442\ 51331\ 76459$$

$$\text{Comp log } r'' = 4.68557\ 48668\ 23541 = \text{log } \sin 1''$$

Let  $a$  be the length of an arc of a circle whose radius is 1, and  $a''$  the number of seconds in that arc, as

$$r'' = \frac{1}{\sin 1''} \text{ and } R : r'' :: a : a'' \text{ or } a'' = r'' a; a = a'' \sin 1''$$

In an equation, therefore, any arc  $a$  of a circle whose radius is 1, is expressed in seconds by changing  $a$  into  $a'' \sin 1''$ .

### V. *Solution of Plane Triangles.*

In the following formulæ A, B, C, represent the angles, and  $a, b, c$ , the sides opposite, respectively.

#### 1. Any plane triangle,

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

$$\frac{\tan \frac{1}{2}(A+B)}{\tan \frac{1}{2}(A-B)} = \frac{\cot \frac{1}{2}C}{\tan \frac{1}{2}(A-B)} = \frac{a+b}{a-b}$$

$$\sin \frac{1}{2}A = \left\{ \frac{(s-b)(s-c)}{bc} \right\}^{\frac{1}{2}}$$

$$\cos \frac{1}{2}A = \left\{ \frac{s(s-a)}{bc} \right\}^{\frac{1}{2}}$$

$$s = \frac{a+b+c}{2}$$

#### 2. Right angled triangles,

making  $A = 90^\circ$  in the preceding, they become

$$a^2 = b^2 + c^2$$

$$b = a \sin B = a \cos C, \quad c = a \sin C = a \cos B$$

$$\tan B = \frac{b}{c} \qquad \tan C = \frac{c}{b}$$

### VI. Solution of Spherical Triangles.

$a, b, c$ , represent the arcs, and  $A, B, C$ , the angles opposite.

#### 1. Oblique spherical triangles

$$\frac{\sin A}{\sin a} = \frac{\sin B}{\sin b} = \frac{\sin C}{\sin c}$$

$$\begin{cases} \cos a = \frac{\cos b \sin (c + \phi)}{\sin \phi} \\ \cot \phi = \tan b \cos A \end{cases}$$

$$\begin{cases} \cos A = \frac{\cos B \sin (C - \phi)}{\sin \phi} \\ \cot \phi = \tan B \cos a \end{cases}$$

$$\begin{cases} \cot a \tan b = \frac{\sin (C + \phi)}{\sin \phi} \\ \cot \phi = \frac{\cot A}{\cos b} \end{cases}$$

#### *Napier's Analogies.*

$$\begin{cases} \tan \frac{1}{2} (a + b) = \tan \frac{1}{2} c \frac{\cos \frac{1}{2} (A - B)}{\cos \frac{1}{2} (A + B)} \\ \tan \frac{1}{2} (a - b) = \tan \frac{1}{2} c \frac{\sin \frac{1}{2} (A - B)}{\sin \frac{1}{2} (A + B)} \\ \tan \frac{1}{2} (A + B) = \cot \frac{1}{2} C \frac{\cos \frac{1}{2} (a - b)}{\cos \frac{1}{2} (a + b)} \\ \tan \frac{1}{2} (A - B) = \cot \frac{1}{2} C \frac{\sin \frac{1}{2} (a - b)}{\sin \frac{1}{2} (a + b)} \end{cases}$$

VI. *Solution of Spherical Triangles*—Continued.

$$\sin \frac{1}{2} a = \frac{\sin S \cdot \sin (A - S)}{\sin B \cdot \sin C}$$

$$\cos \frac{1}{2} a = \frac{\sin (B - S) \cdot \sin (C - S)}{\sin B \cdot \sin C}$$

$$\tan \frac{1}{2} a = \frac{\sin S \cdot \sin (A - S)}{\sin (B - S) \cdot \sin (C - S)}$$

$$\sin \frac{1}{2} A = \frac{\sin (s - b) \cdot \sin (s - c)}{\sin b \cdot \sin c}$$

$$\cos \frac{1}{2} A = \frac{\sin s \cdot \sin (s - a)}{\sin b \cdot \sin c}$$

$$\tan \frac{1}{2} A = \frac{\sin (s - b) \cdot \sin (s - c)}{\sin s \cdot \sin (s - a)}$$

In which  $S$  and  $s$  represent the half sum of the three angles diminished by  $90^\circ$  and the half sum of the three sides, respectively.

2. Right angled spherical triangles,  $a$ , being the hypotenuse.

$$\begin{aligned} \cos a &= \cos b \cdot \cos c \\ \cos a &= \cot B \cdot \cot C \\ \cos B &= \sin C \cdot \cos b \\ \cos C &= \sin B \cdot \cos c \\ \tan b &= \tan a \cdot \cos C \\ \tan c &= \tan a \cdot \cos B \end{aligned}$$

$$\begin{aligned} \cot B &= \cot b \cdot \sin c \\ \cot C &= \cot c \cdot \sin b \\ \tan b &= \tan B \cdot \sin c \\ \tan c &= \tan C \cdot \sin b \\ \sin b &= \sin a \cdot \sin B \\ \sin c &= \sin a \cdot \sin C \end{aligned}$$

### I. *Weights and Measures of the United States.*

The *actual standard of length* is a brass scale of 82 inches in length, made by Troughton, of London, and now in the possession of the Treasury Department.

The *standard of weight* is the *troy pound*, copied in 1827, by Captain Kater, from the imperial troy pound of England, for the use of the Mint of the United States, and there deposited.

This pound is a standard at 30 inches of the Barometer and 62° of the Fahrenheit Thermometer.

The *units of capacity measure* are the *gallon* for *liquid* and the *bushel* for *dry* measure. The gallon is a vessel containing 58372.2 grains, (8.3389 pounds avoirdupois,) of the standard pound of distilled water, at the temperature of maximum density of water, the vessel being weighed in air in which the Barometer is 30 inches at 62° Fahrenheit. The bushel is a measure containing 543391.89 standard grains (77.6274 pounds avoirdupois) of distilled water, at the temperature of maximum density of water, and Barometer 30 inches at 62° Fahrenheit.

The gallon is thus the Wine gallon (of 231 cubic inches) nearly, and the bushel the Winchester bushel, nearly.

The temperature of maximum density of water was determined by Mr. Hassler to be 39°.83 Fahrenheit.

The avoirdupois pound is greater than the troy pound in the proportion of 7000 to 5760 ; that is, the avoirdupois pound is equivalent, in weight, to 7000 grains troy.

## II. *English System of Measures.*

The unit of lineal measure is the *yard*. The yard is divided into 3 feet, and the foot subdivided into 12 inches. The multiples of the yard are the *pole* or *perch*, the *furlong*, and the *mile*. But the pole and furlong are now scarcely ever used, itinerary distances being reckoned in miles and yards. The following are the relations:

| Inches. | Feet. | Yards. | Poles.  | Furlongs.  | Miles.       |
|---------|-------|--------|---------|------------|--------------|
| 1       | 0.083 | 0.028  | 0.00505 | 0.00012626 | 0.0000157828 |
| 12      | 1.    | 0.333  | 0.06060 | 0.00151515 | 0.00018939   |
| 36      | 3.    | 1.     | 0.1818  | 0.004545   | 0.00056818   |
| 198     | 16.5  | 5.5    | 1.      | 0.025      | 0.003125     |
| 7920    | 660.  | 220.   | 40.     | 1.         | 0.125        |
| 63360   | 5280. | 1760.  | 320.    | 8.         | 1.           |

### *Measures of Superficies.*

In square measure the yard is subdivided as in general measure into *feet* and *inches*; 144 square inches being equal to a square foot. For land measure the multiples of the yard are the *pole*, the *rood*, and the *acre*. Very large surfaces, as of whole countries, are expressed in square miles.

The following are the relations of square measure:

| Sq. feet. | Sq. yards. | Poles.     | Roods.      | Acres.      | Sq. mile. |
|-----------|------------|------------|-------------|-------------|-----------|
| 1.        | 0.1111     | 0.00367309 | 0.000091827 | 0.000022957 |           |
| 9.        | 1.         | 0.0330579  | 0.000826448 | 0.000206612 |           |
| 272.25    | 30.25      | 1.         | 0.025       | 0.00625     |           |
| 10890.    | 1210.      | 40.        | 1.          | 0.25        |           |
| 43560.    | 4840.      | 160.       | 4.          | 1.          |           |
| 292800.   | 3097600.   | 102400.    | 2560.       | 640.        | 1.        |

$$\text{Log. } 3097600 = 6.4910253.$$

### III. Measures of Volume.

Solids are measured by cubic yards, feet, and inches; 1728 cubic inches making a cubic foot, and 27 cubic feet a cubic yard. For all sorts of liquids, grain, and other dry goods, the standard measure is declared, by the act of 1824, to be the *imperial gallon*, the capacity of which is determined immediately by weight, and remotely by the standard of length, in the following manner: According to the act, the imperial standard gallon contains 10 pounds avoirdupois weight of distilled water, weighed in air at the temperature of 62° Fahrenheit's Thermometer, the Barometer being at 30 inches. The pound avoirdupois contains 7,000 troy grains; and it is declared that a cubic inch of distilled water (temperature 62°, barometer 30 inches) weighs 252.458 grains. Hence the contents of the imperial standard gallon are 277.274 cubic inches. The parts of the gallon are *quarts* and *pints*. Its multiples are the *peck*, the *bushel*, and the *quarter*.

The following are the relations:

| Pints. | Quarts. | Gallons. | Pecks. | Bushels. | Quarters.   |
|--------|---------|----------|--------|----------|-------------|
| 1      | 0.5     | 0.125    | 0.0625 | 0.015625 | 0.001953125 |
| 2      | 1.      | 0.25     | 0.125  | 0.03125  | 0.00390625  |
| 4      | 2.      | 0.5      | 0.25   | 0.0625   | 0.0078125   |
| 8      | 4.      | 1.       | 0.5    | 0.125    | 0.015625    |
| 16     | 8.      | 2.       | 1.     | 0.25     | 0.03125     |
| 32     | 16.     | 4.       | 2.     | 0.5      | 0.0625      |
| 64     | 32.     | 8.       | 4.     | 1.       | 0.125       |
| 128    | 64.     | 16.      | 8.     | 2.       | 0.25        |
| 256    | 128.    | 32.      | 16.    | 4.       | 0.5         |
| 512    | 256.    | 64.      | 32.    | 8.       | 1.          |

IV. *Tables of British Weights.*1.—*Imperial Troy Weight.*

Standard: One cubic inch of distilled water, at 62° Fahrenheit's Thermometer, the Barometer being 30 inches, weighs 252.458 Troy grains.

$$\begin{array}{rcl} \text{grs.} & & \text{dwt.} \\ 24 & = & 1 \end{array}$$

$$\begin{array}{rcl} & & \text{oz.} \\ 480 & = & 20 = 1 \end{array}$$

$$\begin{array}{rcl} & & \text{lb.} \\ 5760 & = & 240 = 12 = 1 \end{array}$$

Troy weight is used in weighing gold, silver, jewels, &c., and in philosophical experiments.

2.—*Imperial Avoirdupois Weight.*

Standard: The same as in Troy weight, and one avoirdupois pound = 7000 Troy grains.

$$\begin{array}{rcl} \text{drs.} & & \text{oz.} \\ 16 & = & 1 \end{array}$$

$$\begin{array}{rcl} & & \text{lb.} \\ 256 & = & 16 = 1 \end{array}$$

$$\begin{array}{rcl} & & \text{qr.} \\ 7168 & = & 448 = 28 = 1 \end{array}$$

$$\begin{array}{rcl} & & \text{cwt.} \\ 28672 & = & 1792 = 112 = 4 = 1 \end{array}$$

$$\begin{array}{rcl} & & \text{ton.} \\ 573440 & = & 35840 = 2240 = 80 = 20 = 1 \end{array}$$

This weight is used for the general purposes of commerce.



*V. Miscellaneous.*

**Length.**—Gunter's chain = 66 feet = 4 poles = 100 links of 7.92 inches.

1 fathom = 6 feet; 1 cable length = 120 fathoms.

1 hand = 4 inches; 1 palm = 3 inches; 1 span = 9 inches.

**Solid.**—1 cubic yard = 27 cubic feet (B. M.) = 1728 cubic inches.

1 reduced foot (B. M.) = 1 square foot  $\times$  1 inch thick = 144 cubic inches.

1 perch of masonry = 1 perch ( $16\frac{1}{2}$  feet) long  $\times$  1 foot high  $\times$   $1\frac{1}{2}$  foot thick = 24.75 cub. feet; 25 cubic feet has generally been adopted for convenience.

1 cord fire wood = 8 feet long  $\times$  4 feet high  $\times$  4 feet deep = 128 cubic feet.

1 chaldron coal = 36 bushels = 57.25 cub. feet.

**Paper.**—24 sheets = 1 quire.

20 quires = 1 ream = 480 sheets.

*Dimensions of Drawing Paper.*

|              |                                      |                |                                          |
|--------------|--------------------------------------|----------------|------------------------------------------|
| Cap - - -    | 13 $\times$ 16 in.                   | Elephant -     | $27\frac{1}{4} \times 22\frac{1}{4}$ in. |
| Demy - - -   | $19\frac{1}{2} \times 15\frac{1}{2}$ | Columbia -     | $33\frac{1}{4} \times 23$                |
| Medium - -   | 22 $\times$ 18                       | Atlas - - -    | 33 $\times$ 26                           |
| Royal - - -  | 24 $\times$ 19                       | Theorem -      | 34 $\times$ 28                           |
| Super Royal  | 27 $\times$ 19                       | Double eleph't | 40 $\times$ 26                           |
| Imperial - - | 29 $\times$ $21\frac{1}{4}$          | Antiquarian -  | 52 $\times$ 31                           |

*Capacities.*

|                                        |                        |                |
|----------------------------------------|------------------------|----------------|
| A box 16 $\times$ 16.8 $\times$ 8. in. | contains 1 bushel      | } dry measure  |
| 12 $\times$ 11.2 $\times$ 8.           | " $\frac{1}{2}$ bushel |                |
| 8 $\times$ 8.4 $\times$ 8.             | " 1 peck               |                |
| 6 $\times$ 6 $\times$ 6.4              | " 1 gallon             | } liquid meas. |
| 4 $\times$ 4 $\times$ 3.6              | " 1 quart              |                |

VI. *French System of Measures.*

The *unit of measures of length* is the *metre*. The unit of *superficial measure* is the *are*, a surface of 10 metres each way, or 100 square metres. The unit of *measures of capacity* is the *litre*, a vessel containing the cube of the tenth part of the metre. The standard temperature is that of melting ice.

The measures of length are:

|            |   |               |
|------------|---|---------------|
| Myriametre | = | 10000 metres. |
| Kilometre  | = | 1000          |
| Hectometre | = | 100           |
| Metre      | = | 1             |
| Decimetre  | = | 0.1           |
| Centimetre | = | 0.01          |
| Millimetre | = | 0.001         |

The measures of surface are:

|          |   |                   |
|----------|---|-------------------|
| Hectare  | = | 10000 sq. metres. |
| Are      | = | 100               |
| Centiare | = | 1                 |

The measures of capacity are:

|            |   |              |
|------------|---|--------------|
| Kilolitre  | = | 1000 litres. |
| Hectolitre | = | 100          |
| Decalitre  | = | 10           |
| Litre      | = | 1            |
| Decilitre  | = | 0.1          |
| Centilitre | = | 0.01         |

The unit of solid measure is the *stere* or cube of the metre, equal to 35.31658 English cubic feet.

*Table for converting Metres into Toises and French and English feet and inches.*

| Met.  | Toises.    | French. |     |        | English. |         |
|-------|------------|---------|-----|--------|----------|---------|
|       |            | Feet.   | In. | Lines. | Feet.    | Inches. |
| 1     | 0.51307    | 3       | 0   | 11.296 | 3        | 3.708   |
| 2     | 1.02615    | 6       | 1   | 10.592 | 6        | 6.7416  |
| 3     | 1.53922    | 9       | 2   | 9.888  | 9        | 10.1124 |
| 4     | 2.05230    | 12      | 3   | 9.184  | 13       | 1.4832  |
| 5     | 2.56537    | 15      | 4   | 8.480  | 16       | 4.8539  |
| 6     | 3.07844    | 18      | 5   | 7.776  | 19       | 8.2247  |
| 7     | 3.59152    | 21      | 6   | 7.072  | 22       | 11.5955 |
| 8     | 4.10459    | 24      | 7   | 6.368  | 26       | 2.9663  |
| 9     | 4.61767    | 27      | 8   | 5.664  | 29       | 6.3371  |
| 10    | 5.13074    | 30      | 9   | 4.960  | 32       | 9.7079  |
| 20    | 10.26148   | 61      | 6   | 9.920  | 65       | 7.4158  |
| 30    | 15.39222   | 92      | 4   | 2.880  | 98       | 5.1237  |
| 40    | 20.52296   | 123     | 1   | 7.840  | 131      | 2.8316  |
| 50    | 25.65370   | 153     | 11  | 0.800  | 164      | 0.5395  |
| 60    | 30.78444   | 184     | 8   | 5.760  | 196      | 10.2474 |
| 70    | 35.91519   | 215     | 5   | 10.720 | 229      | 7.9553  |
| 80    | 41.04593   | 246     | 3   | 3.680  | 262      | 5.6632  |
| 90    | 46.17667   | 277     | 0   | 8.640  | 295      | 3.3711  |
| 100   | 51.30741   | 307     | 10  | 1.600  | 328      | 1.0790  |
| 200   | 102.61481  | 615     | 8   | 3.200  | 656      | 2.1580  |
| 300   | 153.92222  | 923     | 6   | 4.800  | 984      | 3.2370  |
| 400   | 205.22963  | 1231    | 4   | 6.400  | 1312     | 4.3160  |
| 500   | 256.53704  | 1539    | 2   | 8.000  | 1640     | 5.3950  |
| 600   | 307.84444  | 1847    | 0   | 9.600  | 1968     | 6.4740  |
| 700   | 359.15185  | 2154    | 10  | 11.200 | 2296     | 7.5530  |
| 800   | 410.45926  | 2462    | 9   | 0.800  | 2624     | 8.6320  |
| 900   | 461.76667  | 2770    | 7   | 2.400  | 2952     | 9.7110  |
| 1000  | 513.07407  | 3078    | 5   | 4.000  | 3280     | 10.7900 |
| 2000  | 1026.14815 | 6156    | 10  | 8.000  | 6561     | 9.5800  |
| 3000  | 1539.22222 | 9235    | 4   | 0.000  | 9842     | 8.3790  |
| 4000  | 2052.29630 | 12313   | 9   | 4.000  | 13123    | 7.1600  |
| 5000  | 2565.37037 | 15392   | 2   | 8.000  | 16404    | 5.9500  |
| 6000  | 3078.44444 | 18470   | 8   | 0.000  | 19685    | 4.7400  |
| 7000  | 3591.51852 | 21549   | 1   | 4.000  | 22966    | 3.5300  |
| 8000  | 4104.59259 | 24627   | 6   | 8.000  | 26247    | 2.3200  |
| 9000  | 4617.66667 | 27706   | 0   | 0.000  | 29528    | 1.1100  |
| 10000 | 5130.74074 | 30784   | 5   | 4.000  | 32808    | 11.9000 |

Log. to reduce metres to Eng. feet = 0.5159929.

*Table for converting English Feet into French Toises, Metres, and Feet.*

| English<br>feet. | Toises.    | Metres.    | French. |     |        |
|------------------|------------|------------|---------|-----|--------|
|                  |            |            | Feet.   | In. | Lines. |
| 1                | 0.15638    | 0.30479    | 0       | 11  | 3.114  |
| 2                | 0.31276    | 0.60959    | 1       | 10  | 6.228  |
| 3                | 0.46915    | 0.91438    | 2       | 9   | 9.343  |
| 4                | 0.62553    | 1.21918    | 3       | 9   | 0.457  |
| 5                | 0.78191    | 1.52397    | 4       | 8   | 3.571  |
| 6                | 0.93829    | 1.82877    | 5       | 7   | 6.685  |
| 7                | 1.09468    | 2.13356    | 6       | 6   | 9.799  |
| 8                | 1.25106    | 2.43836    | 7       | 6   | 0.913  |
| 9                | 1.40744    | 2.74315    | 8       | 5   | 4.028  |
| 10               | 1.56382    | 3.04794    | 9       | 4   | 7.142  |
| 20               | 3.12764    | 6.09589    | 18      | 9   | 2.284  |
| 30               | 4.69146    | 9.14383    | 28      | 1   | 9.425  |
| 40               | 6.25529    | 12.19178   | 37      | 6   | 4.567  |
| 50               | 7.81911    | 15.23972   | 46      | 10  | 11.709 |
| 60               | 9.38293    | 18.28767   | 56      | 3   | 6.851  |
| 70               | 10.94675   | 21.33561   | 65      | 8   | 1.993  |
| 80               | 12.51057   | 24.38536   | 75      | 0   | 9.134  |
| 90               | 14.07439   | 27.43150   | 84      | 5   | 4.276  |
| 100              | 15.63822   | 30.47945   | 93      | 9   | 11.418 |
| 200              | 31.27643   | 60.95850   | 187     | 7   | 10.836 |
| 300              | 46.91465   | 91.43835   | 281     | 5   | 10.254 |
| 400              | 62.55286   | 121.91780  | 375     | 3   | 9.672  |
| 500              | 78.19108   | 152.39725  | 469     | 1   | 9.090  |
| 600              | 93.82929   | 182.87670  | 562     | 11  | 8.508  |
| 700              | 109.46751  | 213.35615  | 656     | 9   | 7.926  |
| 800              | 125.10572  | 243.83559  | 750     | 7   | 7.344  |
| 900              | 140.74394  | 274.31504  | 844     | 5   | 6.762  |
| 1000             | 156.38215  | 304.79449  | 938     | 3   | 6.180  |
| 2000             | 312.76431  | 609.58899  | 1876    | 7   | 0.360  |
| 3000             | 469.14646  | 914.38348  | 2814    | 10  | 6.539  |
| 4000             | 625.52861  | 1219.17797 | 3753    | 2   | 0.719  |
| 5000             | 781.91076  | 1523.97246 | 4691    | 5   | 6.899  |
| 6000             | 938.29292  | 1823.76696 | 5629    | 9   | 1.079  |
| 7000             | 1094.67507 | 2133.56145 | 6568    | 0   | 7.259  |
| 8000             | 1251.05722 | 2438.35594 | 7506    | 4   | 1.438  |
| 9000             | 1407.43937 | 2743.15044 | 8444    | 7   | 7.618  |
| 10000            | 1563.82153 | 3047.94493 | 9382    | 11  | 1.798  |

Log. to reduce English feet to metres = 9.4840071.

## VII. Foreign Measures of Length.

Table of relations between the Linear Measures of several countries, with corresponding logarithms.

| Metre.                 | France.<br>Paris foot. | England.<br>Russia.<br>foot. | Prussia.<br>Denmark.<br>foot. | Bavaria.<br>foot.     | Saxony.<br>foot.      | Baden.<br>Switzerland.<br>foot. | Austria.<br>Vienna foot. | Spain.<br>Mexico.<br>foot. |
|------------------------|------------------------|------------------------------|-------------------------------|-----------------------|-----------------------|---------------------------------|--------------------------|----------------------------|
| 1                      | 3.078444<br>0.4883313  | 3.280899<br>0.5159929        | 3.186199<br>0.5032720         | 3.426310<br>0.5348986 | 3.531197<br>0.5479220 | 3.333333<br>0.5228787           | 3.163446<br>0.5001605    | 3.537877<br>0.5487487      |
| 0.3948394<br>9.5116687 | 1<br>0.0276816         | 1.065765<br>0.0276816        | 1.035003<br>0.0149417         | 1.113000<br>0.0464954 | 1.147072<br>0.0383907 | 1.082798<br>0.0345475           | 1.027612<br>0.0118282    | 1.149242<br>0.0604114      |
| 0.3047945<br>9.4940071 | 1                      | 1                            | 0.971136<br>9.9872891         | 1.044320<br>0.0186337 | 1.076290<br>0.0319391 | 1.015982<br>0.0068659           | 0.964201<br>9.9841676    | 1.078325<br>0.0327496      |
| 0.3138535<br>9.4867270 | 1.029722<br>0.0137199  | 1.029722<br>0.0137199        | 1<br>0.0315536                | 1.075359<br>0.0315536 | 1.108279<br>0.0446400 | 1.046178<br>0.0196058           | 0.922859<br>9.9868875    | 1.110375<br>0.0454687      |
| 0.2918592<br>9.4651794 | 0.898472<br>9.9350417  | 0.957561<br>9.9811663        | 0.929922<br>9.9684464         | 1<br>0.0315536        | 1.030612<br>0.0130954 | 0.972864<br>9.9890321           | 0.923281<br>9.9653339    | 1.032562<br>0.0139161      |
| 0.2831901<br>9.4520780 | 0.871785<br>9.9404093  | 0.929118<br>9.9680709        | 0.902300<br>9.9553510         | 0.970297<br>9.9869046 | 1<br>0.050433         | 0.943967<br>9.9748567           | 0.895856<br>9.9638385    | 1.001892<br>9.9003907      |
| 0.3000000<br>9.4771213 | 0.922533<br>9.9654525  | 0.984270<br>9.9831141        | 0.955860<br>9.9803842         | 1.027893<br>0.0119479 | 1.059359<br>0.0250433 | 1<br>0.0237183                  | 0.949034<br>9.9772817    | 1.061361<br>0.0658630      |
| 0.3161109<br>9.4963385 | 0.973130<br>9.9681708  | 1.037128<br>0.0155394        | 1.007193<br>0.0631135         | 1.083094<br>0.0346661 | 1.116250<br>0.0477615 | 1.053703<br>0.0237183           | 1<br>0.9772817           | 1.118361<br>0.0485322      |
| 0.2896553<br>9.4512573 | 0.870139<br>9.9395886  | 0.927364<br>9.9672502        | 0.900597<br>9.9545303         | 0.968465<br>9.9860639 | 0.998112<br>9.9991793 | 0.942184<br>9.9741360           | 0.894165<br>9.9314178    | 1                          |

VIII. Table of relations between Itinerary Measures of several countries, with the corresponding logarithms.

| France.<br>Myriametre<br>= 10000 M. | England.<br>Stat. mile<br>= 5280'. | Prussia.<br>Denmark<br>= 24000'. | Austria<br>mile<br>= 24000'. | Russia<br>verst<br>= 3500'. | Spain.<br>Mexico<br>Jud. league<br>= 15000'. | Germany.<br>Geo. mile<br>15 = 1 deg. | England.<br>France.<br>Naut. league<br>20 = 1 deg. |
|-------------------------------------|------------------------------------|----------------------------------|------------------------------|-----------------------------|----------------------------------------------|--------------------------------------|----------------------------------------------------|
| 1                                   | 6.213424<br>0.7533590              | 1.327583<br>0.1230617            | 1.318103<br>0.1194492        | 9.373997<br>0.9719948       | 2.358584<br>0.3726514                        | 1.347680<br>0.1266869                | 1.796907<br>0.9543256                              |
| 0.1609315<br>9.2066410              | 1<br>0.7533590                     | 0.213650<br>9.3287028            | 0.212124<br>9.3265903        | 1.508571<br>0.1785659       | 0.379570<br>9.5792924                        | 0.216884<br>9.3362279                | 0.289179<br>9.4611666                              |
| 0.7532485<br>9.8768353              | 4.680554<br>0.6702972              | 1<br>0.7532485                   | 0.992859<br>9.9968875        | 7.060950<br>0.8488631       | 1.776600<br>0.2495397                        | 1.015138<br>0.0063231                | 1.353518<br>0.1314639                              |
| 0.7586663<br>9.8900508              | 4.714219<br>0.6734097              | 1.007193<br>0.0031125            | 1<br>0.140613                | 7.111736<br>0.8519756       | 1.789379<br>0.2527022                        | 1.023440<br>0.0098376                | 1.363253<br>0.1345764                              |
| 0.1066781<br>9.0289752              | 0.662879<br>9.8314341              | 0.141624<br>9.1511366            | 0.140613<br>9.149244         | 1<br>0.8519756              | 2.516092<br>0.4072066                        | 0.143768<br>9.1576620                | 0.191691<br>9.2866008                              |
| 0.4239831<br>9.6273486              | 2.634556<br>0.4207076              | 0.562873<br>9.7504103            | 0.558853<br>9.7472978        | 0.397442<br>9.5992734       | 1<br>0.4072066                               | 0.571394<br>9.7563355                | 0.761868<br>9.8818742                              |
| 0.7420158<br>9.8704131              | 4.610755<br>0.6637721              | 0.985088<br>9.9934749            | 0.978053<br>9.9903694        | 6.955654<br>0.8233680       | 1.750197<br>0.2430645                        | 0.571394<br>9.7563355                | 1.333333<br>0.1249387                              |
| 0.5565118<br>9.7454744              | 3.458067<br>0.5388334              | 0.738816<br>9.8685361            | 0.733540<br>9.8654226        | 5.216740<br>0.7173992       | 1.312580<br>0.1181928                        | 0.750000<br>9.8750613                | 1                                                  |

1 English or French geographical mile = 1.60 of a degree of longitude at the Equator =  
= 2028.7 English yards.

|                       |                   |
|-----------------------|-------------------|
| Modern Roman mile     | Eng. stat. miles. |
| Tuscan mile           | = 0.925           |
| Old Scottish mile     | = 1.027           |
| Irish mile            | = 1.127           |
| French posting league | = 1.273           |
|                       | = 2.422           |

|                       |                   |
|-----------------------|-------------------|
| Portugal league       | Eng. stat. miles. |
| Flanders league       | = 3.841           |
| Spanish common league | = 3.900           |
| Hungarian mile        | = 4.214           |
| Swedish mile          | = 5.178           |
|                       | = 6.648           |

## VII. Foreign Measures of Length.

Table of relations between the Linear Measures of several countries, with corresponding logarithms.

| Metre.                 | France.<br>Paris foot. | England.<br>Russia.<br>foot. | Prussia.<br>Denmark.<br>foot. | Bavaria.<br>foot.          | Saxony.<br>foot.      | Baden.<br>Switzerland.<br>foot. | Austria.<br>Vienna foot. | Spain.<br>Mexico.<br>foot. |
|------------------------|------------------------|------------------------------|-------------------------------|----------------------------|-----------------------|---------------------------------|--------------------------|----------------------------|
| 1                      | 3.078444<br>0.4883313  | 3.280899<br>0.5159929        | 3.186199<br>0.5037730         | 3.426310<br>0.5348966      | 3.531197<br>0.5479220 | 3.333333<br>0.5228787           | 3.163446<br>0.5001805    | 3.537877<br>0.5487437      |
| 0.3948394<br>1.5116657 | 1<br>0.0276616         | 1.065765<br>0.0149417        | 1.035003<br>0.0149417         | 1.113000<br>0.0464954      | 1.147072<br>0.0595907 | 1.082798<br>0.0345475           | 1.027612<br>0.0118292    | 1.149242<br>0.0604114      |
| 0.047945<br>340071     | 1                      | 0.971136<br>9.9872801        | 1.044320<br>0.0188337         | 1.075359<br>0.0315536      | 1.076290<br>0.0319291 | 1.015982<br>0.0068859           | 0.964201<br>9.9641676    | 1.078325<br>0.0327498      |
| 8535<br>70             | 1.029722<br>0.0127199  | 1<br>0.929922<br>9.9684464   | 1.075359<br>0.0315536         | 1.075359<br>0.0315536      | 1.08279<br>0.046490   | 1.046178<br>0.0196058           | 0.922859<br>9.9988575    | 1.110375<br>0.0454697      |
| 92                     | 0.898472<br>9.9535047  | 0.957561<br>9.9811663        | 0.929922<br>9.9684464         | 1<br>0.970297<br>9.9880046 | 1.030612<br>0.0130954 | 0.973864<br>9.9880521           | 0.923281<br>9.9633339    | 1.032562<br>0.0139161      |
| 0.871785<br>0.04093    | 0.929118<br>9.9680709  | 0.902300<br>9.9533510        | 0.902300<br>9.9533510         | 0.970297<br>9.9880046      | 1<br>0.0250433        | 0.943967<br>9.9749567           | 0.895856<br>9.9522385    | 1.001892<br>0.0008207      |
| 0.984270<br>9.923141   | 0.984270<br>9.923141   | 0.955860<br>9.9903942        | 0.955860<br>9.9903942         | 1.027893<br>0.0119479      | 1.059359<br>0.0250433 | 1<br>0.022183                   | 0.949034<br>9.9772817    | 1.061361<br>0.0258630      |
| 1.037128<br>0.158324   | 1.007193<br>0.0031125  | 1.083094<br>0.0346661        | 1.083094<br>0.0346661         | 1.083094<br>0.0346661      | 1.116250<br>0.0477615 | 1.053703<br>0.022183            | 1<br>0.0485822           | 1.118361<br>0.0485822      |
| 927364<br>9672502      | 0.900597<br>9.95453603 | 0.968465<br>9.9860839        | 0.968465<br>9.9860839         | 0.968465<br>9.9860839      | 0.998112<br>9.9991793 | 0.942184<br>9.9741360           | 0.894165<br>9.954178     | 1                          |

VIII Table of relations between Binary Measures of  
several countries, with the corresponding logarithms.

| Country.         | Capital.        | Population.  | Area.                | Climate.       | Government.              | Religion.   | Language.   | Notes.                |
|------------------|-----------------|--------------|----------------------|----------------|--------------------------|-------------|-------------|-----------------------|
| England.         | London.         | 45,000,000.  | 29,000 sq. miles.    | Temperate.     | Constitutional Monarchy. | Anglican.   | English.    | 1. 700,000 sq. miles. |
| France.          | Paris.          | 35,000,000.  | 210,000 sq. miles.   | Temperate.     | Republic.                | Catholic.   | French.     | 0. 400,000 sq. miles. |
| Germany.         | Berlin.         | 60,000,000.  | 354,000 sq. miles.   | Temperate.     | Empire.                  | Lutheran.   | German.     | 0. 100,000 sq. miles. |
| Spain.           | Madrid.         | 15,000,000.  | 195,000 sq. miles.   | Temperate.     | Monarchy.                | Catholic.   | Spanish.    | 0. 100,000 sq. miles. |
| Italy.           | Rome.           | 28,000,000.  | 110,000 sq. miles.   | Mediterranean. | Monarchy.                | Catholic.   | Italian.    | 0. 100,000 sq. miles. |
| Sweden.          | Stockholm.      | 2,500,000.   | 450,000 sq. miles.   | Temperate.     | Monarchy.                | Lutheran.   | Swedish.    | 0. 100,000 sq. miles. |
| Norway.          | Oslo.           | 1,500,000.   | 150,000 sq. miles.   | Temperate.     | Monarchy.                | Lutheran.   | Norwegian.  | 0. 100,000 sq. miles. |
| Denmark.         | Copenhagen.     | 1,500,000.   | 15,000 sq. miles.    | Temperate.     | Monarchy.                | Lutheran.   | Danish.     | 0. 100,000 sq. miles. |
| Poland.          | Warsaw.         | 10,000,000.  | 119,000 sq. miles.   | Temperate.     | Republic.                | Catholic.   | Polish.     | 0. 100,000 sq. miles. |
| Czechoslovakia.  | Prague.         | 3,500,000.   | 78,000 sq. miles.    | Temperate.     | Republic.                | Catholic.   | Czech.      | 0. 100,000 sq. miles. |
| Austria.         | Vienna.         | 2,500,000.   | 83,000 sq. miles.    | Temperate.     | Monarchy.                | Catholic.   | Austrian.   | 0. 100,000 sq. miles. |
| Hungary.         | Budapest.       | 3,500,000.   | 93,000 sq. miles.    | Temperate.     | Monarchy.                | Catholic.   | Hungarian.  | 0. 100,000 sq. miles. |
| Russia.          | Moscow.         | 100,000,000. | 1,700,000 sq. miles. | Temperate.     | Monarchy.                | Orthodox.   | Russian.    | 0. 100,000 sq. miles. |
| Japan.           | Tokyo.          | 60,000,000.  | 377,000 sq. miles.   | Temperate.     | Monarchy.                | Buddhist.   | Japanese.   | 0. 100,000 sq. miles. |
| China.           | Peking.         | 400,000,000. | 3,700,000 sq. miles. | Temperate.     | Monarchy.                | Buddhist.   | Chinese.    | 0. 100,000 sq. miles. |
| India.           | Calcutta.       | 300,000,000. | 1,900,000 sq. miles. | Tropical.      | Monarchy.                | Hindu.      | Hindustani. | 0. 100,000 sq. miles. |
| United States.   | Washington.     | 100,000,000. | 3,600,000 sq. miles. | Temperate.     | Republic.                | Protestant. | English.    | 0. 100,000 sq. miles. |
| Canada.          | Ottawa.         | 10,000,000.  | 9,000,000 sq. miles. | Temperate.     | Monarchy.                | Protestant. | English.    | 0. 100,000 sq. miles. |
| South Africa.    | Cape Town.      | 10,000,000.  | 2,200,000 sq. miles. | Temperate.     | Monarchy.                | Protestant. | Dutch.      | 0. 100,000 sq. miles. |
| South America.   | Buenos Aires.   | 15,000,000.  | 1,700,000 sq. miles. | Tropical.      | Republic.                | Catholic.   | Spanish.    | 0. 100,000 sq. miles. |
| Central America. | Guatemala City. | 2,000,000.   | 110,000 sq. miles.   | Tropical.      | Republic.                | Catholic.   | Spanish.    | 0. 100,000 sq. miles. |
| Caribbean.       | Kingston.       | 1,000,000.   | 10,000 sq. miles.    | Tropical.      | Monarchy.                | Catholic.   | English.    | 0. 100,000 sq. miles. |

It is a pleasure to have you here, and I am sure you will find the meeting very interesting.



*Comparison of French and English Measures.*

Metre . . . . . 39.37079 inches.

“ . . . . . 3.28089 feet.

“ . . . . . 1.09363 yards.

Kilometre . . . . . 0.62138 miles.

Myriametre . . . . . 6.2138 miles.

Square metre . . . . . 1.196033 square yards.

Are . . . . . .119.6033 square yards.

Hectare . . . . . 2.471143 acres.

Litre . . . . . 1.760773 pints.

“ . . . . . 0.220096 gallons.

Decalitre . . . . . 2.200967 gallons.

Hectolitre . . . . . 22.009668 gallons.

Gramme . . . . . 15.438 grains, troy.

“ . . . . . 0.032 ounce, troy.

Kilogramme . . . . . 2.680 pounds, troy.

“ . . . . . 2.205 pounds, avoirdupois.

*IX. Spanish and Mexican Measures of length.*

1 Castilian foot = 11.1284 English inches.

3 Castilian feet = 1 vara = 33.3852 English inches.

= 0.927365 English yards.

5000 varas = 1 judicial league = 4637. English yards.

X. *Specific Gravities.*

| Substance.          | Specific gravity. | Weight of 1 cub. inch. | Substance.         | Specific gravity. | Weight of 1 cub. in. |
|---------------------|-------------------|------------------------|--------------------|-------------------|----------------------|
|                     |                   | Lbs.                   |                    |                   | Lbs.                 |
| Brass, (cast).....  | 8.396             | 0.3037                 | Sand.....          | 1.800             | 0.0652               |
| Bronze, (gun metal) | 8.700             | 0.3147                 | Stone, (common)    | 2.520             | 0.0911               |
| Copper, (cast)..... | 8.788             | 0.3179                 | Wood, ash.....     | 0.722             | 0.0261               |
| Iron, (bar).....    | 7.788             | 0.2817                 | “ cypress ..       | 0.441             | 0.0160               |
| Iron, (cast).....   | 7.207             | 0.2607                 | “ hickory...       | 0.838             | 0.0303               |
| Lead, (cast).....   | 11.352            | 0.4106                 | “ oak.....         | 0.687             | 0.0248               |
| Tin, (cast).....    | 7.291             | 0.2637                 | “ pine .....       | 0.541             | 0.0196               |
| Bricks.....         | 1.900             | 0.0690                 | Coal, (bitumin's)  | 1.270             | 0.0460               |
| Earth, (common)...  | 1.500             | 0.0543                 | Water, (distilled) | 1.000             | 0.0361               |

The weight of dry atmospheric air at the temperature of 32°, the barometer being at 30 in., is  $\frac{1}{16}$  of that of distilled water.

The weight of a cubic foot of distilled water *at the maximum density* being nearly 1000 ounces avoirdupois, the specific gravity of a solid or liquid body expresses the weight of a cubic foot, in ounces; therefore the weight of such a body in ounces will be found by multiplying its contents in cubic feet by its specific gravity.

According to Mr. Hassler's comparisons, the weight of a cubic foot of water at its maximum density, the barometer being at 30 in., is 998.068 oz.

According to the British imperial standards, the weight of a cubic foot of water, at 62°, the barometer being at 30 in., is 997.136 oz.; this would give for the cubic foot of water, at the maximum density, 998.224 oz.

By the investigations of Prof. R. S. McCulloch, the maximum density of water is at the temperature of 39°.6 Fahr.; this agrees very nearly with Mr. Hassler's determination of the maximum density, 39°.83.

# XI. *Analytical Expressions for different Lines, Surfaces, and Solids.*

## 1. *Lines.*

Circle. Ratio of circumference to diameter = 3.1415926  
=  $\frac{22}{7}$  nearly.

Length of an arc =  $\frac{a\pi r}{180}$ ;  $r$  being the radius of the circle, and  $a$  the number of degrees in the arc;  
or, nearly =  $\frac{2c' - c}{3}$ ;  $c$  being the chord of the arc, and  $c'$  (the chord of half the arc) =  
 $\sqrt{\frac{1}{4}c^2 + \text{versine}^2}$ .

Ellipse. Circumference =  $\frac{22}{7} \pi \sqrt{\frac{1}{2}(a^2 + b^2)}$  nearly;  $a$   
and  $b$  being the axes.

Parabola. Length of an arc, commencing at vertex =  
 $\sqrt{\frac{4a^3}{3}} + \sqrt{b}$  nearly;  $a$  being the abscissa, and  
 $b$  the ordinate.

## 2. *Surfaces.*

### 1. Triangle in terms of—

its base and its altitude . . . . . =  $\frac{b A}{2}$

two sides and the included angle . . . . . =  $\frac{a b \sin C}{2}$

its three sides . . =  $[s(s-a)(s-b)(s-c)]^{\frac{1}{2}}$

where  $A$  = the altitude;  $a, b, c$  = the three sides, and  $C$   
the angle included between  $a$  and  $b$ ;  $s = \frac{a+b+c}{2}$

2. Parallelogram in terms of—

its base and its altitude . . . . . =  $b A$

two sides and the included angle . . . . . =  $a b \sin C$

two sides and their corresponding diagonal

$$= 2 [s (s - a) (s - b) (s - c)]^{\frac{1}{2}}$$

where  $C$  = the angle included between two adjacent sides  $a, b$ ;

$c$  = the diagonal opposite, and  $s = \frac{a + b + c}{2}$ .

3. Trapezium in terms of—

its two parallel bases and its altitude . . . . . =  $\frac{B + b}{2} A$

its two parallel bases, one of its oblique  
sides and the angle between one of  
these bases and this side . . . . . } =  $\frac{B + b}{2} l \sin C$

where  $A$  = the distance between the two parallel bases  $B, b$ ;  $l$  = the length of one of the oblique sides, and  $C$  the angle between one of these bases and this side.

4. Any Quadrilateral = half the product of its two diagonals multiplied by the sine of the included angle.

5. Regular Polygon . . . . . =  $\frac{n \left(\frac{a}{2}\right)^2}{\tan \frac{180^\circ}{n}}$

where  $n$  = the number of sides;  $a$  = the length of one of them.

6. Circle . . . . . =  $\pi R^2$

7. Ellipse . . . . . =  $\pi a b$   
 $a$  and  $b$  being the semi-axes.

8. Right cylinder, exclusive of its bases . . . =  $2 \pi R A$

9. Sphere . . . . . =  $4 \pi R^2$

10. Zone . . . =  $4 \pi R^2 \sin \frac{1}{2} (L' - L) \cos \frac{1}{2} (L' + L)$

11. Spherical Quadrilateral, formed by two parallels of Latitude and two meridians

$$= \frac{\pi}{90^\circ} (M' - M) R^2 \sin \frac{1}{2} (L' - L) \cos \frac{1}{2} (L' + L)$$

where  $R$  = the radius of the sphere;  $L, L'$  = the latitudes of the bases of the zone,  $+$  when North,  $-$  South;  $M', M$  = the longitudes of the extreme meridians of the quadrilateral.  $(M' - M)$  being expressed in degrees and decimals.

In the place of  $R$ , the normal  $N$ , of the mean Latitude  $\left(\frac{L' + L}{2}\right)$ , can be used.

12. Right cone . . . . . =  $\pi R L$

13. Frustrum of cone with parallel bases =  $\pi l (R + r)$

When  $R$  and  $r$  = the radii of the bases of these solids,  $L$  and  $l$  = the lengths of their generating elements.

### 3. Solids.

14. Prism . . . . . =  $B A$

where  $B$  = the area of the base,  $A$  = the altitude.

15. Rectangular parallelopiped . . . =  $p \times q \times r$

Cube . . . . . =  $p^3$

where  $p, q, r$ , = the lengths of the three contiguous edges.

16. Pyramid . . . . . =  $\frac{B A}{3}$

The area  $B$  being found from No. 5.

17. Right cylinder . . . . . =  $\pi R^2 A$

18. Right cone . . . . . =  $\frac{1}{3} \pi R^2 A$

19. Sphere . . . . . =  $\frac{4}{3} \pi R^3$

20. Prismoid, or solid figure, similar to that which is formed in excavations or embankments of roads; terminated by parallel cross sections. Solid content = area of each end, added to four times the middle area, and the sum multiplied by the length divided by 6, or

$$= \left\{ (b + r h') h' + (b + r h) h + 4 \left( b + r = \frac{h + h'}{2} \right) \frac{h + h'}{2} \right\} \frac{l}{6}$$

where  $b$  = the breadth at the bottom of the cutting

$h$  = the perpendicular depth of cutting at higher end

$h'$  = the perpendicular depth of cutting at lower end

$l$  = the length of the solid

$r$  = the ratio of the perpendicular height of the slope to its horizontal base.

*Lengths of Circular Arcs,  
Taking the base of Segments as unity.*

| Ver. Sin. | Length. | Ver. Sin. | Length. | Ver. Sin. | Length. | Ver. Sin. | Length. | Ver. Sin. | Length. |
|-----------|---------|-----------|---------|-----------|---------|-----------|---------|-----------|---------|
| .01       | 1.000   | .11       | 1.032   | .21       | 1.114   | .31       | 1.239   | .41       | 1.401   |
| .02       | "       | .12       | 1.038   | .22       | 1.124   | .32       | 1.254   | .42       | 1.418   |
| .03       | "       | .13       | 1.044   | .23       | 1.135   | .33       | 1.269   | .43       | 1.437   |
| .04       | "       | .14       | 1.051   | .24       | 1.147   | .34       | 1.284   | .44       | 1.455   |
| .05       | "       | .15       | 1.059   | .25       | 1.159   | .35       | 1.300   | .45       | 1.474   |
| .06       | 1.006   | .16       | 1.067   | .26       | 1.171   | .36       | 1.316   | .46       | 1.493   |
| .07       | 1.014   | .17       | 1.075   | .27       | 1.184   | .37       | 1.332   | .47       | 1.512   |
| .08       | 1.018   | .18       | 1.084   | .28       | 1.197   | .38       | 1.349   | .48       | 1.531   |
| .09       | 1.020   | .19       | 1.093   | .29       | 1.212   | .39       | 1.366   | .49       | 1.551   |
| .10       | 1.026   | .20       | 1.103   | .30       | 1.225   | .40       | 1.383   | .50       | 1.571   |

XII. *Hydrometry.*

1. To determine the mean velocity of a stream from observations of the velocity at its surface.

Let  $\alpha$  = the observed surface velocity, in inches,

$\beta$  = the bottom velocity,

$\gamma$  = the mean velocity,

$$\beta = (\sqrt{\alpha} - 1)^2, \quad \gamma = \frac{\alpha + \beta}{2}$$

$$\gamma = \frac{\alpha + (\sqrt{\alpha} - 1)^2}{2}.$$

Prony has given the very simple formula

$$\gamma = 0.816458 \alpha$$

which is, perhaps, more correct than the above of Dubuat.

2. In open streams which are flowing with an *uniform motion*, calling

$\omega$ , the area of the section of the stream,

$\pi$ , that portion of the perimeter of the section of the bed, which is in contact with the water,

$I$ , the fall divided by the length,

$\nu$ , the mean velocity per second =  $\frac{Q}{\omega}$ ,

$Q$ , the discharge per second,

$R$ , the *hydraulic depth*, or  $\frac{\omega}{\pi}$ ,

(the unit being English feet), the relations, according to Eytelwein, between these several quantities, may be expressed by the following,

$$0.0000242651 \nu + 0.0001114155 \nu^3 = R I.$$

Whence

$$\nu = -0.1088941694 + \sqrt{0.0118580490 + 8975.414285 R I}.$$

$$\text{And } 0.0000242651 Q \omega + 0.0001114155 Q^3 = \frac{\omega^3}{\pi} I.$$

Whence

$$Q = \sqrt{\left(8975.414285 \frac{\omega^3}{x} I + 0.01213425 \omega^3\right) - 0.1088942 \omega}$$

$$\text{Log } 0.01213425 = 8.0840130$$

$$\text{Log } 0.1088942 = 9.0370065$$

$$\text{Log } 8975.414285 = 3.9530545$$

$$\text{Log } 0.0000242651 = 5.3849821$$

$$\text{Log } 0.0001114155 = 6.0469456$$

To realize in practice what would be called uniform motion, the canal or stream should be straight, and with the same section and inclination from one end to the other. In proportion as it varies from these conditions, we may expect to find the formula in fault.

*Table of Surface, Bottom and Mean Velocities.*

| VELOCITY IN INCHES. |         |        |          |         |        |
|---------------------|---------|--------|----------|---------|--------|
| Surface.            | Bottom. | Mean.  | Surface. | Bottom. | Mean.  |
| 5                   | 1.527   | 3.263  | 55       | 41.167  | 48.083 |
| 10                  | 4.675   | 7.337  | 60       | 45.508  | 52.754 |
| 15                  | 8.254   | 11.627 | 65       | 49.875  | 57.436 |
| 20                  | 12.055  | 16.027 | 70       | 54.266  | 62.133 |
| 25                  | 16.000  | 20.500 | 75       | 58.679  | 66.839 |
| 30                  | 20.045  | 25.022 | 80       | 63.111  | 71.555 |
| 35                  | 24.167  | 29.583 | 85       | 67.561  | 76.280 |
| 40                  | 28.350  | 34.175 | 90       | 72.026  | 81.006 |
| 45                  | 32.583  | 38.791 | 95       | 76.506  | 85.753 |
| 50                  | 36.857  | 43.428 | 100      | 81.000  | 90.500 |



### XIII. To trace Railroad Curves by means of deflections.

#### General Propositions.

1. The angle formed by a tangent and a chord is equal to half the angle at the centre of the circle, subtended by the chord.
2. The angle of deflection formed by any two equal chords meeting at the circumference, is equal to the angle at the centre, subtended by either chord.
3. A line bisecting the angle of deflection formed by any two equal chords, is a tangent to the arc at the point where the two chords meet.
4. If an arc of a circle be subdivided into any number of equal parts, and lines be drawn from the several points of subdivision so as to meet at any point in the circumference, these several lines will form equal angles at the point of meeting, and the angles thus formed will be respectively measured by one half the subdivided arc.

TABLE 1.

*Table of deflections for chords and tangents with radii and versed sines corresponding.*

| Angle of deflection between tangent and chord. |       | Corresponding radius of circle. | Length of versed sine for chords of 100 feet. | Angle of deflection between tangent and chord. |       | Corresponding radius of circle. | Length of versed sine for chords of 100 feet. |
|------------------------------------------------|-------|---------------------------------|-----------------------------------------------|------------------------------------------------|-------|---------------------------------|-----------------------------------------------|
| D. M.                                          | D. M. |                                 |                                               | D. M.                                          | D. M. |                                 |                                               |
| 0 /                                            | 0 /   |                                 |                                               | 0 /                                            | 0 /   |                                 |                                               |
| 0.15                                           | 0.30  | 11460.                          | .106                                          | 3.45                                           | 7.30  | 764.                            | 1.635                                         |
| 0.30                                           | 1.00  | 5730.                           | .217                                          | 4.00                                           | 8.00  | 716.2                           | 1.744                                         |
| 0.45                                           | 1.30  | 3820.                           | .328                                          | 4.15                                           | 8.30  | 674.1                           | 1.853                                         |
| 1.00                                           | 2.00  | 2865.                           | .435                                          | 4.30                                           | 9.00  | 636.6                           | 1.960                                         |
| 1.15                                           | 2.30  | 2292.                           | .545                                          | 4.45                                           | 9.30  | 603.1                           | 2.070                                         |
| 1.30                                           | 3.00  | 1910.                           | .655                                          | 5.00                                           | 10.00 | 573.                            | 2.180                                         |
| 1.45                                           | 3.30  | 1637.1                          | .762                                          | 5.15                                           | 10.30 | 545.7                           | 2.286                                         |
| 2.00                                           | 4.00  | 1432.5                          | .872                                          | 5.30                                           | 11.00 | 520.9                           | 2.394                                         |
| 2.15                                           | 4.30  | 1273.3                          | .981                                          | 5.45                                           | 11.30 | 498.2                           | 2.505                                         |
| 2.30                                           | 5.00  | 1146.                           | 1.090                                         | 6.00                                           | 12.00 | 477.5                           | 2.613                                         |
| 2.45                                           | 5.30  | 1041.8                          | 1.199                                         | 6.15                                           | 12.30 | 458.4                           | 2.722                                         |
| 3.00                                           | 6.00  | 955.                            | 1.309                                         | 6.30                                           | 13.00 | 440.7                           | 2.828                                         |
| 3.15                                           | 6.30  | 881.5                           | 1.416                                         | 6.45                                           | 13.30 | 424.4                           | 2.940                                         |
| 3.30                                           | 7.00  | 818.5                           | 1.525                                         | 7.00                                           | 14.00 | 409.2                           | 3.048                                         |
| 3.45                                           | 7.30  | 764.                            | 1.635                                         | 7.15                                           | 14.30 | 395.2                           | 3.157                                         |

TABLE 2.

*Table showing, for arcs of different radii, the lengths of lines of deflection from a tangential point to points on the arc 100 feet apart, with the angles of deflection and versed sines corresponding.*

| Angle of deflection from Tangent. | Length of line of deflection. | Versed sine for line of deflection. | Angle of deflection from Tangent. | Length of line of deflection. | Versed sine for line of deflection. |
|-----------------------------------|-------------------------------|-------------------------------------|-----------------------------------|-------------------------------|-------------------------------------|
| deg. min.                         | feet.                         | feet.                               | deg. min.                         | feet.                         | feet.                               |
| <b>2° Radius 2865 ft.</b>         |                               |                                     | <b>2½° Rad. 2292 ft.</b>          |                               |                                     |
| 1°.00'                            | 100.00                        | .43                                 | 1°.15'                            | 100.00                        | .54                                 |
| 2.00                              | 199.97                        | 1.74                                | 2.30                              | 199.95                        | 2.18                                |
| 3.00                              | 299.88                        | 3.93                                | 3.45                              | 299.81                        | 4.90                                |
| 4.00                              | 399.70                        | 6.98                                | 5.00                              | 399.53                        | 8.72                                |
| 5.00                              | 499.39                        | 10.90                               | 6.15                              | 499.05                        | 13.62                               |
| <b>3° Rad. 1910 ft.</b>           |                               |                                     | <b>3½° Rad. 1637.1 ft.</b>        |                               |                                     |
| 1°.30'                            | 100.00                        | .65                                 | 1°.45'                            | 100.00                        | .76                                 |
| 3.00                              | 199.93                        | 2.62                                | 3.30                              | 199.91                        | 3.05                                |
| 4.30                              | 299.73                        | 5.89                                | 5.15                              | 299.63                        | 6.87                                |
| 6.00                              | 399.32                        | 10.46                               | 7.00                              | 399.07                        | 12.20                               |
| 7.30                              | 498.63                        | 16.34                               | 8.45                              | 498.14                        | 19.05                               |
| <b>4° Rad. 1432.5 ft.</b>         |                               |                                     | <b>4½° Rad. 1273.3 ft.</b>        |                               |                                     |
| 2°.00'                            | 100.00                        | .87                                 | 2°.15'                            | 100.00                        | .98                                 |
| 4.00                              | 199.88                        | 3.49                                | 4.30                              | 199.85                        | 3.92                                |
| 6.00                              | 299.51                        | 7.84                                | 6.45                              | 299.38                        | 8.90                                |
| 8.00                              | 398.78                        | 13.93                               | 9.00                              | 398.46                        | 15.67                               |
| 10.00                             | 497.57                        | 21.75                               | 11.15                             | 496.92                        | 24.46                               |
| <b>5° Rad. 1146 ft.</b>           |                               |                                     | <b>5½° Rad. 1041.8 ft.</b>        |                               |                                     |
| 2°.30'                            | 100.00                        | 1.09                                | 2°.45'                            | 100.00                        | 1.20                                |
| 5.00                              | 199.81                        | 4.36                                | 5.30                              | 199.77                        | 4.79                                |
| 7.30                              | 299.24                        | 9.80                                | 8.15                              | 299.08                        | 10.77                               |
| 10.00                             | 398.10                        | 17.41                               | 11.00                             | 397.70                        | 19.12                               |
| 12.30                             | 496.20                        | 27.16                               | 13.45                             | 495.41                        | 29.83                               |

Table 2—Continued.

| Angle of de-<br>flection from<br>Tangent. | Length of<br>line of<br>deflection. | Versed sine<br>for line of<br>deflection. | Angle of de-<br>flection from<br>Tangent. | Length of<br>line of<br>deflection. | Versed sine<br>for line of<br>deflection. |
|-------------------------------------------|-------------------------------------|-------------------------------------------|-------------------------------------------|-------------------------------------|-------------------------------------------|
| deg. min.                                 | feet.                               | feet.                                     | deg. min.                                 | feet.                               | feet.                                     |
| 6° Rad. 955 ft.                           |                                     |                                           | 6½° Rad. 881 ft.                          |                                     |                                           |
| 3°.00'                                    | 100.00                              | 1.31                                      | 3°.15'                                    | 100.00                              | 1.41                                      |
| 6.00                                      | 199.73                              | 5.23                                      | 6.30                                      | 199.68                              | 5.66                                      |
| 9.00                                      | 298.90                              | 11.75                                     | 9.45                                      | 298.71                              | 12.72                                     |
| 12.00                                     | 397.26                              | 20.86                                     | 13.00                                     | 396.79                              | 22.58                                     |
| 15.00                                     | 494.53                              | 32.54                                     | 16.15                                     | 493.59                              | 35.19                                     |
| 7° Rad. 818.5 ft.                         |                                     |                                           | 7½° Rad. 764 ft.                          |                                     |                                           |
| 3°.30'                                    | 100.00                              | 1.52                                      | 3°.45'                                    | 100.00                              | 1.63                                      |
| 7.00                                      | 199.63                              | 6.09                                      | 7.30                                      | 199.57                              | 6.53                                      |
| 10.30                                     | 298.61                              | 13.69                                     | 11.15                                     | 298.29                              | 14.68                                     |
| 14.00                                     | 396.28                              | 24.30                                     | 15.00                                     | 395.73                              | 26.03                                     |
| 17.30                                     | 492.57                              | 37.86                                     | 18.45                                     | 491.47                              | 40.54                                     |
| 8° Rad. 716.2 ft.                         |                                     |                                           | 8½° Rad. 674.1 ft.                        |                                     |                                           |
| 4°.00'                                    | 100.00                              | 1.74                                      | 4°.15'                                    | 100.00                              | 1.85                                      |
| 8.00                                      | 199.51                              | 6.97                                      | 8.30                                      | 199.48                              | 7.40                                      |
| 12.00                                     | 298.05                              | 15.64                                     | 12.45                                     | 297.84                              | 16.62                                     |
| 16.00                                     | 395.14                              | 27.73                                     | 17.00                                     | 394.57                              | 29.45                                     |
| 20.00                                     | 490.28                              | 43.18                                     | 21.15                                     | 489.13                              | 45.83                                     |
| 9° Rad. 636.6 ft.                         |                                     |                                           | 9½° Rad. 603.1 ft.                        |                                     |                                           |
| 4°.30'                                    | 100.00                              | 1.96                                      | 4°.45'                                    | 100.00                              | 2.07                                      |
| 9.00                                      | 199.39                              | 7.83                                      | 9.30                                      | 199.31                              | 8.27                                      |
| 13.30                                     | 297.54                              | 17.57                                     | 14.15                                     | 297.26                              | 18.55                                     |
| 18.00                                     | 393.86                              | 31.13                                     | 19.00                                     | 393.16                              | 32.85                                     |
| 22.30                                     | 487.75                              | 48.41                                     | 23.45                                     | 486.36                              | 51.07                                     |
| 10° Rad. 573 ft.                          |                                     |                                           | 10½° Rad. 545.7 ft.                       |                                     |                                           |
| 5°.00'                                    | 100.00                              | 2.18                                      | 5°.15'                                    | 100.00                              | 2.28                                      |
| 10.00                                     | 199.24                              | 8.70                                      | 10.30                                     | 199.16                              | 9.12                                      |
| 15.00                                     | 296.96                              | 19.52                                     | 15.45                                     | 296.65                              | 20.46                                     |
| 20.00                                     | 392.42                              | 34.55                                     | 21.00                                     | 391.65                              | 36.19                                     |
| 25.00                                     | 484.90                              | 53.68                                     | 26.15                                     | 483.37                              | 56.20                                     |

Table 2—Continued.

| Angle of deflection from Tangent. | Length of line of deflection. | Versed sine for line of deflection. | Angle of deflection from Tangent. | Length of line of deflection. | Versed sine for line of deflection. |
|-----------------------------------|-------------------------------|-------------------------------------|-----------------------------------|-------------------------------|-------------------------------------|
| deg. min.                         | feet.                         | feet.                               | deg. min.                         | feet.                         | feet.                               |
| <b>11°</b>                        | <b>Rad. 520.9 ft.</b>         |                                     | <b>11½°</b>                       | <b>Rad. 498.2 ft.</b>         |                                     |
| 5°.30'                            | 100.00                        | 2.39                                | 5°.45'                            | 100.00                        | 2.50                                |
| 11.00                             | 199.08                        | 9.56                                | 11.30                             | 198.99                        | 9.99                                |
| 16.30                             | 296.33                        | 21.41                               | 17.15                             | 295.99                        | 22.40                               |
| 22.00                             | 390.84                        | 37.86                               | 23.00                             | 390.00                        | 39.58                               |
| 27.30                             | 481.76                        | 58.75                               | 28.45                             | 480.10                        | 61.39                               |
| <b>12°</b>                        | <b>Rad. 477.5 ft.</b>         |                                     | <b>12½°</b>                       | <b>Rad. 458.4 ft.</b>         |                                     |
| 6°.00'                            | 100.00                        | 2.61                                | 6°.15'                            | 100.00                        | 2.72                                |
| 12.00                             | 198.90                        | 10.42                               | 12.30                             | 198.81                        | 10.85                               |
| 18.00                             | 295.63                        | 23.34                               | 18.45                             | 295.26                        | 24.30                               |
| 24.00                             | 389.12                        | 41.24                               | 25.00                             | 388.20                        | 42.91                               |
| 30.00                             | 478.34                        | 63.90                               | 31.15                             | 476.52                        | 66.45                               |
| <b>13°</b>                        | <b>Rad. 440.7 ft.</b>         |                                     | <b>13½°</b>                       |                               |                                     |
| 6°.30'                            | 100.00                        | 2.82                                | 6°.45'                            | 100.00                        | 2.94                                |
| 13.00                             | 198.71                        | 11.27                               | 13.30                             | 198.61                        | 11.71                               |
| 19.30                             | 294.87                        | 25.23                               | 20.15                             | 294.47                        | 26.20                               |
| 26.00                             | 387.24                        | 44.53                               | 27.00                             | 386.25                        | 46.21                               |
| 32.30                             | 474.63                        | 68.90                               | 33.45                             | 472.68                        | 71.45                               |
| <b>14°</b>                        |                               |                                     | <b>14½°</b>                       |                               |                                     |
| 7°.00'                            | 100.00                        | 3.04                                | 7°.15'                            | 100.00                        | 3.15                                |
| 14.00                             | 198.51                        | 12.14                               | 14.30                             | 198.40                        | 12.58                               |
| 21.00                             | 294.06                        | 27.16                               | 21.45                             | 293.63                        | 28.12                               |
| 28.00                             | 385.23                        | 47.87                               | 29.00                             | 384.16                        | 49.52                               |
| 35.00                             | 470.65                        | 73.96                               | 36.15                             | 468.55                        | 76.45                               |
| 42.00                             | 549.06                        | 105.05                              | 43.30                             | 545.45                        | 108.47                              |
| 49.00                             | 619.28                        | 140.67                              | 50.45                             | 613.63                        | 145.08                              |
| 56.00                             | 680.27                        | 180.29                              | 58.00                             | 671.99                        | 185.65                              |
| 63.00                             | 731.12                        | 223.32                              | 65.15                             | 719.61                        | 229.63                              |
| 70.00                             | 771.07                        | 269.11                              | 72.30                             | 755.73                        | 276.22                              |

TABLE 3.

*Table of ordinates to circular arcs on a chord of 100 feet.*

| Angle of deflection for chord. | ABSCISSA IN FEET. |            |            |            |            |            |            |            |            |      |
|--------------------------------|-------------------|------------|------------|------------|------------|------------|------------|------------|------------|------|
|                                | 5.<br>95.         | 10.<br>90. | 15.<br>85. | 20.<br>80. | 25.<br>75. | 30.<br>70. | 35.<br>65. | 40.<br>60. | 45.<br>55. | 50.  |
| 1.00                           | .04               | .07        | .11        | .14        | .16        | .18        | .20        | .21        | .21        | .22  |
| 1.30                           | .06               | .10        | .16        | .21        | .25        | .28        | .30        | .31        | .32        | .33  |
| 2.00                           | .08               | .14        | .22        | .28        | .33        | .37        | .40        | .41        | .43        | .44  |
| 2.30                           | .11               | .20        | .28        | .35        | .41        | .46        | .50        | .52        | .54        | .55  |
| 3.00                           | .13               | .24        | .33        | .42        | .49        | .55        | .59        | .63        | .65        | .66  |
| 3.30                           | .15               | .28        | .39        | .49        | .57        | .64        | .69        | .74        | .76        | .77  |
| 4.00                           | .17               | .32        | .44        | .56        | .66        | .73        | .79        | .84        | .86        | .87  |
| 4.30                           | .19               | .36        | .50        | .63        | .74        | .83        | .89        | .95        | .97        | .98  |
| 5.00                           | .21               | .40        | .56        | .70        | .82        | .92        | .99        | 1.05       | 1.08       | 1.09 |
| 5.30                           | .23               | .43        | .61        | .77        | .91        | 1.01       | 1.09       | 1.16       | 1.19       | 1.20 |
| 6.00                           | .25               | .47        | .67        | .84        | .99        | 1.10       | 1.19       | 1.26       | 1.30       | 1.31 |
| 6.30                           | .27               | .51        | .72        | .91        | 1.07       | 1.19       | 1.29       | 1.37       | 1.41       | 1.42 |
| 7.00                           | .29               | .55        | .78        | .98        | 1.15       | 1.28       | 1.39       | 1.47       | 1.52       | 1.53 |
| 7.30                           | .31               | .59        | .83        | 1.05       | 1.23       | 1.38       | 1.49       | 1.57       | 1.63       | 1.64 |
| 8.00                           | .33               | .63        | .89        | 1.13       | 1.31       | 1.47       | 1.59       | 1.68       | 1.74       | 1.75 |
| 8.30                           | .35               | .67        | .94        | 1.20       | 1.39       | 1.56       | 1.69       | 1.78       | 1.84       | 1.86 |
| 9.00                           | .37               | .71        | 1.00       | 1.26       | 1.47       | 1.65       | 1.78       | 1.89       | 1.95       | 1.97 |
| 9.30                           | .40               | .75        | 1.06       | 1.33       | 1.56       | 1.74       | 1.88       | 1.99       | 2.05       | 2.08 |
| 10.00                          | .42               | .79        | 1.11       | 1.40       | 1.64       | 1.83       | 1.98       | 2.10       | 2.15       | 2.19 |
| 10.30                          | .44               | .82        | 1.17       | 1.47       | 1.72       | 1.93       | 2.08       | 2.20       | 2.26       | 2.29 |
| 11.00                          | .46               | .86        | 1.22       | 1.54       | 1.80       | 2.02       | 2.18       | 2.31       | 2.36       | 2.40 |
| 11.30                          | .48               | .90        | 1.28       | 1.61       | 1.88       | 2.11       | 2.28       | 2.41       | 2.47       | 2.51 |
| 12.00                          | .50               | .94        | 1.34       | 1.68       | 1.97       | 2.20       | 2.38       | 2.52       | 2.57       | 2.62 |
| 12.30                          | .52               | .98        | 1.39       | 1.75       | 2.05       | 2.29       | 2.48       | 2.62       | 2.68       | 2.72 |
| 13.00                          | .54               | 1.02       | 1.45       | 1.82       | 2.13       | 2.38       | 2.58       | 2.73       | 2.78       | 2.84 |
| 13.30                          | .56               | 1.06       | 1.50       | 1.89       | 2.21       | 2.48       | 2.68       | 2.83       | 2.89       | 2.94 |
| 14.00                          | .58               | 1.10       | 1.56       | 1.96       | 2.29       | 2.57       | 2.78       | 2.93       | 3.00       | 3.05 |
| 14.30                          | .60               | 1.12       | 1.61       | 2.02       | 2.37       | 2.65       | 2.87       | 3.03       | 3.13       | 3.16 |

#### XIV. *Land Surveying with Compass and Chain.*

##### *To calculate the Area or Content of Land.*

If the sum of each adjacent pair of distances perpendicular to a meridian (*departures*) assumed without the survey, be multiplied by the northing or southing between them, in succession round the figure in the same order, the difference between the sum of the *north* products and the sum of the *south* products will be double the area of the tract.

The *meridian distance* of a course is the distance of the middle point of that course from an assumed meridian.

Hence—The double meridian distance of the first course is equal to its departure.

And the double meridian distance of any course is equal to the double meridian distance of the preceding course, plus its departure, plus the departure of the course itself, having regard to the algebraic sign of each.

Then to find the area—

1. Multiply the double meridian distance of each course by its northing or southing.
2. Place all the *plus* products in one column, and all the *minus* products in another.
3. Add up each column separately and take their difference. This difference will be *double* the area of the land.

In *balancing* the work, the error for each particular course is found by the proportion—

As the sum of the courses, is to the error of latitude, (or departure,) so is each particular course, to its correction.

When a bearing is due east or west, the error of latitude is nothing, and the course must be subtracted from the sum of the courses before balancing the columns of latitude. And so with the departures.

**EXAMPLE.**—It is required to find the content of a piece of land, of which the following are the field notes :

| Sta. | Course.                       | Dist.       | Sta. | Course.                       | Dist.         |
|------|-------------------------------|-------------|------|-------------------------------|---------------|
| 1.   | N. $46\frac{1}{2}^{\circ}$ W. | 20. chains. | 4.   | S. $56^{\circ}$ E.            | 27.60 chains. |
| 2.   | N. $51\frac{1}{2}^{\circ}$ E. | 13.80 "     | 5.   | S. $33\frac{1}{2}^{\circ}$ W. | 18.80 "       |
| 3.   | East                          | 21.25 "     | 6.   | N. $74\frac{1}{2}^{\circ}$ W. | 30.95 "       |

*Calculation.*

| Stations.                        | Courses.  | Diff. Lat. |                        | Departure. |             | Balanced. |         | D.M.D.  | Area<br>+ | Area<br>— |
|----------------------------------|-----------|------------|------------------------|------------|-------------|-----------|---------|---------|-----------|-----------|
|                                  |           | N.         | S.                     | E.         | W.          | Lat.      | Dep.    |         |           |           |
| 1                                | N. 46½ W. | 13.77      | -                      | -          | 14.51       | + 13.88   | —       | 14.56   | 202.0928  |           |
| 2                                | N. 51½ E. | 8.54       | -                      | 10.84      | -           | + 8.61    | + 10.81 | 10.81   | 93.0741   |           |
| 3                                | East      | 21.25      | -                      | 21.25      | -           | -         | + 21.20 | 42.82   | -         |           |
| 4                                | S. 56° E. | 27.60      | -                      | 15.44      | 22.88       | —         | 15.39   | + 22.82 | 86.84     | 1327.7836 |
| 5                                | S. 33½ W. | 18.80      | -                      | 15.72      | -           | 10.31     | —       | 15.63   | 99.30     | 1552.0590 |
| 6                                | N. 74½ W. | 30.95      | 8.97                   | -          | -           | 29.83     | + 8.43  | —       | 59.03     | 497.6929  |
| Sums                             |           | 132.40     | 31.16                  | 54.97      | 54.65       |           |         |         | 792.7898  | 9879.8426 |
|                                  |           | 30.58      | 54.65                  |            |             |           |         |         | 792.7898  |           |
| Error in Northing . . .          |           | 0.58       | Error in Westing . . . |            | 2)2087.0598 |           |         |         |           |           |
| Answer 104 A. 1 R. 16 P. . . . . |           | 1043.5264  |                        |            |             |           |         |         |           |           |

100,000 square links of Gunter's chain = 1 acre.

**XIII. Traverse Table,**  
*Showing differences of Latitude and the Departures.*

| Minutes. | Distance. | 0°      |         | 1°      |         | 2°      |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 1.00000 | 0.00000 | 0.99984 | 0.01745 | 0.99939 | 0.03490 | 1         | 60'      |
|          | 2         | 2.00000 | 0.00000 | 1.99969 | 0.03490 | 1.99878 | 0.06980 | 2         |          |
|          | 3         | 3.00000 | 0.00000 | 2.99954 | 0.05235 | 2.99817 | 0.10470 | 3         |          |
|          | 4         | 4.00000 | 0.00000 | 3.99939 | 0.06980 | 3.99756 | 0.13960 | 4         |          |
|          | 5         | 5.00000 | 0.00000 | 4.99923 | 0.08726 | 4.99695 | 0.17450 | 5         |          |
|          | 6         | 6.00000 | 0.00000 | 5.99908 | 0.10471 | 5.99634 | 0.20940 | 6         |          |
|          | 7         | 7.00000 | 0.00000 | 6.99893 | 0.12216 | 6.99573 | 0.24430 | 7         |          |
|          | 8         | 8.00000 | 0.00000 | 7.99878 | 0.13961 | 7.99512 | 0.27920 | 8         |          |
|          | 9         | 9.00000 | 0.00000 | 8.99862 | 0.15707 | 8.99451 | 0.31410 | 9         |          |
| 15'      | 1         | 0.99999 | 0.00436 | 0.99976 | 0.02181 | 0.99922 | 0.03925 | 1         | 45'      |
|          | 2         | 1.99998 | 0.00872 | 1.99952 | 0.04363 | 1.99845 | 0.07851 | 2         |          |
|          | 3         | 2.99997 | 0.01308 | 2.99928 | 0.06544 | 2.99768 | 0.11777 | 3         |          |
|          | 4         | 3.99996 | 0.01745 | 3.99904 | 0.08725 | 3.99691 | 0.15703 | 4         |          |
|          | 5         | 4.99995 | 0.02181 | 4.99881 | 0.10907 | 4.99614 | 0.19629 | 5         |          |
|          | 6         | 5.99994 | 0.02617 | 5.99857 | 0.13089 | 5.99537 | 0.23555 | 6         |          |
|          | 7         | 6.99993 | 0.03054 | 6.99833 | 0.15270 | 6.99460 | 0.27481 | 7         |          |
|          | 8         | 7.99992 | 0.03490 | 7.99809 | 0.17452 | 7.99383 | 0.31407 | 8         |          |
|          | 9         | 8.99991 | 0.03926 | 8.99785 | 0.19633 | 8.99306 | 0.35333 | 9         |          |
| 30'      | 1         | 0.99996 | 0.00872 | 0.99965 | 0.02617 | 0.99904 | 0.04361 | 1         | 30'      |
|          | 2         | 1.99992 | 0.01745 | 1.99931 | 0.05235 | 1.99809 | 0.08723 | 2         |          |
|          | 3         | 2.99988 | 0.02617 | 2.99897 | 0.07853 | 2.99714 | 0.13085 | 3         |          |
|          | 4         | 3.99984 | 0.03490 | 3.99862 | 0.10470 | 3.99619 | 0.17447 | 4         |          |
|          | 5         | 4.99981 | 0.04363 | 4.99828 | 0.13088 | 4.99524 | 0.21809 | 5         |          |
|          | 6         | 5.99977 | 0.05235 | 5.99794 | 0.15706 | 5.99428 | 0.26171 | 6         |          |
|          | 7         | 6.99973 | 0.06108 | 6.99760 | 0.18323 | 6.99333 | 0.30533 | 7         |          |
|          | 8         | 7.99969 | 0.06981 | 7.99725 | 0.20941 | 7.99238 | 0.34895 | 8         |          |
|          | 9         | 8.99965 | 0.07853 | 8.99691 | 0.23559 | 8.99143 | 0.39257 | 9         |          |
| 45'      | 1         | 0.99991 | 0.01308 | 0.99953 | 0.03053 | 0.99884 | 0.04797 | 1         | 15'      |
|          | 2         | 1.99982 | 0.02617 | 1.99906 | 0.06107 | 1.99769 | 0.09595 | 2         |          |
|          | 3         | 2.99974 | 0.03926 | 2.99860 | 0.09161 | 2.99654 | 0.14393 | 3         |          |
|          | 4         | 3.99965 | 0.05235 | 3.99813 | 0.12215 | 3.99539 | 0.19191 | 4         |          |
|          | 5         | 4.99957 | 0.06544 | 4.99766 | 0.15269 | 4.99424 | 0.23989 | 5         |          |
|          | 6         | 5.99948 | 0.07853 | 5.99720 | 0.18323 | 5.99309 | 0.28786 | 6         |          |
|          | 7         | 6.99940 | 0.09162 | 6.99673 | 0.21376 | 6.99193 | 0.33584 | 7         |          |
|          | 8         | 7.99931 | 0.10471 | 7.99626 | 0.24430 | 7.99078 | 0.38382 | 8         |          |
|          | 9         | 8.99922 | 0.11780 | 8.99580 | 0.27484 | 8.98963 | 0.43180 | 9         |          |
| Minutes. | Distance. | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Distance. | Minutes. |
|          |           | 89°     |         | 88°     |         | 87°     |         |           |          |



*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 3°      |         | 4°      |         | 5°      |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.99863 | 0.05233 | 0.99756 | 0.06975 | 0.99619 | 0.08715 | 1         | 60'      |
|          | 2         | 1.99726 | 0.10467 | 1.99519 | 0.13951 | 1.99238 | 0.17431 | 2         |          |
|          | 3         | 2.99589 | 0.15700 | 2.99269 | 0.20926 | 2.98858 | 0.26146 | 3         |          |
|          | 4         | 3.99452 | 0.20934 | 3.99025 | 0.27902 | 3.98477 | 0.34862 | 4         |          |
|          | 5         | 4.99315 | 0.26168 | 4.98782 | 0.34878 | 4.98097 | 0.43577 | 5         |          |
|          | 6         | 5.99178 | 0.31401 | 5.98538 | 0.41853 | 5.97716 | 0.52293 | 6         |          |
|          | 7         | 6.99041 | 0.36635 | 6.98294 | 0.48829 | 6.97336 | 0.61008 | 7         |          |
|          | 8         | 7.98904 | 0.41868 | 7.98051 | 0.55805 | 7.96955 | 0.69724 | 8         |          |
|          | 9         | 8.98767 | 0.47102 | 8.97807 | 0.62780 | 8.96575 | 0.78440 | 9         |          |
| 15'      | 1         | 0.99839 | 0.05669 | 0.99725 | 0.07410 | 0.99580 | 0.09150 | 1         | 45'      |
|          | 2         | 1.99678 | 0.11338 | 1.99450 | 0.14821 | 1.99160 | 0.18300 | 2         |          |
|          | 3         | 2.99517 | 0.17007 | 2.99175 | 0.22232 | 2.98741 | 0.27450 | 3         |          |
|          | 4         | 3.99356 | 0.22677 | 3.98900 | 0.29643 | 3.98321 | 0.36600 | 4         |          |
|          | 5         | 4.99195 | 0.28346 | 4.98625 | 0.37054 | 4.97902 | 0.45750 | 5         |          |
|          | 6         | 5.99035 | 0.34015 | 5.98350 | 0.44465 | 5.97482 | 0.54900 | 6         |          |
|          | 7         | 6.98874 | 0.39684 | 6.98075 | 0.51875 | 6.97063 | 0.64051 | 7         |          |
|          | 8         | 7.98713 | 0.45354 | 7.97800 | 0.59286 | 7.96643 | 0.73201 | 8         |          |
|          | 9         | 8.98552 | 0.51023 | 8.97525 | 0.66697 | 8.96224 | 0.82351 | 9         |          |
| 30'      | 1         | 0.99813 | 0.06104 | 0.99691 | 0.07845 | 0.99539 | 0.09584 | 1         | 30'      |
|          | 2         | 1.99626 | 0.12209 | 1.99383 | 0.15691 | 1.99079 | 0.19169 | 2         |          |
|          | 3         | 2.99440 | 0.18314 | 2.99075 | 0.23537 | 2.98618 | 0.28753 | 3         |          |
|          | 4         | 3.99253 | 0.24419 | 3.98766 | 0.31383 | 3.98158 | 0.38338 | 4         |          |
|          | 5         | 4.99067 | 0.30524 | 4.98458 | 0.39229 | 4.97698 | 0.47922 | 5         |          |
|          | 6         | 5.98880 | 0.36629 | 5.98150 | 0.47075 | 5.97237 | 0.57507 | 6         |          |
|          | 7         | 6.98694 | 0.42733 | 6.97842 | 0.54921 | 6.96777 | 0.67092 | 7         |          |
|          | 8         | 7.98507 | 0.48838 | 7.97533 | 0.62767 | 7.96316 | 0.76676 | 8         |          |
|          | 9         | 8.98321 | 0.54943 | 8.97225 | 0.70613 | 8.95856 | 0.86261 | 9         |          |
| 45'      | 1         | 9.99785 | 0.06540 | 0.99656 | 0.08280 | 0.99496 | 0.10018 | 1         | 15'      |
|          | 2         | 1.99571 | 0.13080 | 1.99313 | 0.16561 | 1.98993 | 0.20037 | 2         |          |
|          | 3         | 2.99357 | 0.19620 | 2.98969 | 0.24842 | 2.98490 | 0.30056 | 3         |          |
|          | 4         | 3.99143 | 0.26161 | 3.98626 | 0.33123 | 3.97987 | 0.40075 | 4         |          |
|          | 5         | 4.98929 | 0.32701 | 4.98282 | 0.41404 | 4.97484 | 0.50094 | 5         |          |
|          | 6         | 5.98715 | 0.39241 | 5.97939 | 0.49684 | 5.96981 | 0.60112 | 6         |          |
|          | 7         | 6.98501 | 0.45782 | 6.97595 | 0.57965 | 6.96477 | 0.70131 | 7         |          |
|          | 8         | 7.98287 | 0.52322 | 7.97252 | 0.66246 | 7.95974 | 0.80150 | 8         |          |
|          | 9         | 8.98073 | 0.58862 | 8.96908 | 0.74527 | 8.95471 | 0.90169 | 9         |          |
| Minutes. | Distance. | 86°     |         | 85°     |         | 84°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |

*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 6°      |         | 7°      |         | 8°      |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.99452 | 0.10452 | 0.99254 | 0.12186 | 0.99026 | 0.13917 | 1         | 60'      |
|          | 2         | 1.98904 | 0.20905 | 1.98509 | 0.24373 | 1.98053 | 0.27834 | 2         |          |
|          | 3         | 2.98356 | 0.31358 | 2.97763 | 0.36560 | 2.97080 | 0.41751 | 3         |          |
|          | 4         | 3.97808 | 0.41811 | 3.97018 | 0.48747 | 3.96107 | 0.55669 | 4         |          |
|          | 5         | 4.97261 | 0.52264 | 4.96273 | 0.60934 | 4.95134 | 0.69586 | 5         |          |
|          | 6         | 5.96713 | 0.62717 | 5.95519 | 0.73121 | 5.94160 | 0.83503 | 6         |          |
|          | 7         | 6.96165 | 0.73169 | 6.94782 | 0.85308 | 6.93187 | 0.97421 | 7         |          |
|          | 8         | 7.95617 | 0.83622 | 7.94038 | 0.97495 | 7.92214 | 0.11338 | 8         |          |
|          | 9         | 8.95069 | 0.94075 | 8.93291 | 0.09682 | 8.91241 | 0.25255 | 9         |          |
| 15'      | 1         | 0.99405 | 0.10886 | 0.99200 | 0.12619 | 0.98965 | 0.14349 | 1         | 45'      |
|          | 2         | 1.98811 | 0.21773 | 1.98400 | 0.25239 | 1.97930 | 0.28698 | 2         |          |
|          | 3         | 2.98216 | 0.32660 | 2.97601 | 0.37859 | 2.96995 | 0.43047 | 3         |          |
|          | 4         | 3.97622 | 0.43546 | 3.96801 | 0.50479 | 3.95860 | 0.57397 | 4         |          |
|          | 5         | 4.97028 | 0.54433 | 4.96002 | 0.63099 | 4.94825 | 0.71746 | 5         |          |
|          | 6         | 5.96433 | 0.65320 | 5.95202 | 0.75719 | 5.93790 | 0.86095 | 6         |          |
|          | 7         | 6.95839 | 0.76206 | 6.94403 | 0.88339 | 6.92755 | 1.00444 | 7         |          |
|          | 8         | 7.95245 | 0.87093 | 7.93603 | 1.00959 | 7.91721 | 1.14794 | 8         |          |
|          | 9         | 8.94650 | 0.97980 | 8.92804 | 1.13579 | 8.90686 | 1.29143 | 9         |          |
| 30'      | 1         | 0.99357 | 0.11320 | 0.99144 | 0.13052 | 0.98901 | 0.14780 | 1         | 30'      |
|          | 2         | 1.98714 | 0.22640 | 1.98288 | 0.26105 | 1.97803 | 0.29561 | 2         |          |
|          | 3         | 2.98071 | 0.33960 | 2.97433 | 0.39157 | 2.96704 | 0.44349 | 3         |          |
|          | 4         | 3.97428 | 0.45281 | 3.96577 | 0.52210 | 3.95606 | 0.59123 | 4         |          |
|          | 5         | 4.96786 | 0.56601 | 4.95722 | 0.65263 | 4.94508 | 0.73904 | 5         |          |
|          | 6         | 5.96143 | 0.67921 | 5.94866 | 0.78315 | 5.93409 | 0.88685 | 6         |          |
|          | 7         | 6.95500 | 0.79242 | 6.94011 | 0.91368 | 6.92311 | 1.03466 | 7         |          |
|          | 8         | 7.94857 | 0.90562 | 7.93155 | 1.04420 | 7.91212 | 1.18247 | 8         |          |
|          | 9         | 8.94214 | 1.01862 | 8.92300 | 1.17473 | 8.90114 | 1.33028 | 9         |          |
| 45'      | 1         | 0.99306 | 0.11753 | 0.99086 | 0.13485 | 0.98836 | 0.15212 | 1         | 15'      |
|          | 2         | 1.98613 | 0.23507 | 1.98173 | 0.26970 | 1.97672 | 0.30424 | 2         |          |
|          | 3         | 2.97920 | 0.35261 | 2.97259 | 0.40455 | 2.96508 | 0.45637 | 3         |          |
|          | 4         | 3.97227 | 0.47014 | 3.96346 | 0.53940 | 3.95344 | 0.60849 | 4         |          |
|          | 5         | 4.96534 | 0.58768 | 4.95432 | 0.67425 | 4.94180 | 0.76061 | 5         |          |
|          | 6         | 5.95841 | 0.70522 | 5.94519 | 0.80910 | 5.93016 | 0.91274 | 6         |          |
|          | 7         | 6.95147 | 0.82276 | 6.93606 | 0.94395 | 6.91853 | 1.06486 | 7         |          |
|          | 8         | 7.94454 | 0.94029 | 7.92692 | 1.07880 | 7.90689 | 1.21698 | 8         |          |
|          | 9         | 8.93761 | 1.05783 | 8.91779 | 1.21365 | 8.89525 | 1.36911 | 9         |          |
| Minutes. | Distance. | 83°     |         | 82°     |         | 81°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |

*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 9°      |         | 10°     |         | 11°     |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.98768 | 0.15643 | 0.98480 | 0.17364 | 0.98162 | 0.19081 | 1         | 60'      |
|          | 2         | 1.97537 | 0.31286 | 1.96961 | 0.34729 | 1.96325 | 0.38162 | 2         |          |
|          | 3         | 2.96306 | 0.46930 | 2.95442 | 0.52094 | 2.94488 | 0.57243 | 3         |          |
|          | 4         | 3.95075 | 0.62573 | 3.93923 | 0.69459 | 3.92650 | 0.76324 | 4         |          |
|          | 5         | 4.93844 | 0.78217 | 4.92403 | 0.86824 | 4.90813 | 0.95405 | 5         |          |
|          | 6         | 5.92612 | 0.93860 | 5.90884 | 1.04188 | 5.88976 | 1.14486 | 6         |          |
|          | 7         | 6.91381 | 1.09504 | 6.89365 | 1.21553 | 6.87139 | 1.33566 | 7         |          |
|          | 8         | 7.90150 | 1.25147 | 7.87846 | 1.38918 | 7.85301 | 1.52648 | 8         |          |
|          | 9         | 8.88919 | 1.40791 | 8.86327 | 1.56283 | 8.83464 | 1.71729 | 9         |          |
| 15'      | 1         | 0.98699 | 0.16074 | 0.98404 | 0.17794 | 0.98078 | 0.19509 | 1         | 45'      |
|          | 2         | 1.97399 | 0.32148 | 1.96808 | 0.35588 | 1.96157 | 0.39018 | 2         |          |
|          | 3         | 2.96098 | 0.48222 | 2.95212 | 0.53383 | 2.94235 | 0.58527 | 3         |          |
|          | 4         | 3.94798 | 0.64297 | 3.93616 | 0.71177 | 3.92314 | 0.78036 | 4         |          |
|          | 5         | 4.93493 | 0.80371 | 4.92020 | 0.88971 | 4.90392 | 0.97545 | 5         |          |
|          | 6         | 5.92197 | 0.96445 | 5.90424 | 1.06766 | 5.88471 | 1.17054 | 6         |          |
|          | 7         | 6.90897 | 1.12519 | 6.88828 | 1.24560 | 6.86549 | 1.36563 | 7         |          |
|          | 8         | 7.89597 | 1.28594 | 7.87232 | 1.42354 | 7.84628 | 1.56072 | 8         |          |
|          | 9         | 8.88296 | 1.44668 | 8.85636 | 1.60149 | 8.82706 | 1.75581 | 9         |          |
| 30'      | 1         | 0.98628 | 0.16504 | 0.98325 | 0.18223 | 0.97992 | 0.19936 | 1         | 30'      |
|          | 2         | 1.97257 | 0.33009 | 1.96650 | 0.36447 | 1.95984 | 0.39873 | 2         |          |
|          | 3         | 2.95885 | 0.49514 | 2.94976 | 0.54670 | 2.93977 | 0.59810 | 3         |          |
|          | 4         | 3.94514 | 0.66019 | 3.93301 | 0.72894 | 3.91969 | 0.79747 | 4         |          |
|          | 5         | 4.93142 | 0.82523 | 4.91627 | 0.91117 | 4.89962 | 0.99683 | 5         |          |
|          | 6         | 5.91771 | 0.99028 | 5.89952 | 1.09341 | 5.87954 | 1.19620 | 6         |          |
|          | 7         | 6.90399 | 1.15533 | 6.88278 | 1.27564 | 6.85947 | 1.39557 | 7         |          |
|          | 8         | 7.89028 | 1.32038 | 7.86603 | 1.45788 | 7.83939 | 1.59494 | 8         |          |
|          | 9         | 8.87657 | 1.48542 | 8.84929 | 1.64011 | 8.81932 | 1.79431 | 9         |          |
| 45'      | 1         | 0.98555 | 0.16935 | 0.98245 | 0.18652 | 0.97904 | 0.20364 | 1         | 15'      |
|          | 2         | 1.97111 | 0.33870 | 1.96490 | 0.37304 | 1.95809 | 0.40728 | 2         |          |
|          | 3         | 2.95666 | 0.50805 | 2.94735 | 0.55957 | 2.93713 | 0.61092 | 3         |          |
|          | 4         | 3.94222 | 0.67740 | 3.92980 | 0.74609 | 3.91618 | 0.81456 | 4         |          |
|          | 5         | 4.92778 | 0.84675 | 4.91225 | 0.93262 | 4.89522 | 1.01820 | 5         |          |
|          | 6         | 5.91333 | 1.01610 | 5.89470 | 1.11914 | 5.87427 | 1.22185 | 6         |          |
|          | 7         | 6.89889 | 1.18545 | 6.87715 | 1.30566 | 6.85331 | 1.42549 | 7         |          |
|          | 8         | 7.88444 | 1.35480 | 7.85960 | 1.49219 | 7.83236 | 1.62913 | 8         |          |
|          | 9         | 8.87000 | 1.52415 | 8.84205 | 1.67871 | 8.81140 | 1.83277 | 9         |          |
| Minutes. | Distance. | Uep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Distance. | Minutes. |
|          |           | 80°     |         | 79°     |         | 78°     |         |           |          |

*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 12°     |         | 13°     |         | 14°     |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.97814 | 0.20791 | 0.97437 | 0.22495 | 0.97029 | 0.24192 | 1         | 60'      |
|          | 2         | 1.95629 | 0.41582 | 1.94874 | 0.44990 | 1.94059 | 0.48384 | 2         |          |
|          | 3         | 2.93444 | 0.62373 | 2.92311 | 0.67485 | 2.91088 | 0.72576 | 3         |          |
|          | 4         | 3.91259 | 0.83164 | 3.89748 | 0.89980 | 3.88118 | 0.96768 | 4         |          |
|          | 5         | 4.89073 | 1.03955 | 4.87185 | 1.12475 | 4.85147 | 1.20961 | 5         |          |
|          | 6         | 5.86888 | 1.24747 | 5.84622 | 1.34970 | 5.82177 | 1.45153 | 6         |          |
|          | 7         | 6.84703 | 1.45538 | 6.82059 | 1.57465 | 6.79206 | 1.69345 | 7         |          |
|          | 8         | 7.82518 | 1.66329 | 7.79496 | 1.79960 | 7.76236 | 1.93537 | 8         |          |
|          | 9         | 8.80332 | 1.87120 | 8.76933 | 2.02455 | 8.73266 | 2.17729 | 9         |          |
| 15'      | 1         | 0.97723 | 0.21217 | 0.97337 | 0.22920 | 0.96923 | 0.24615 | 1         | 45'      |
|          | 2         | 1.95446 | 0.42435 | 1.94675 | 0.45840 | 1.93846 | 0.49230 | 2         |          |
|          | 3         | 2.93169 | 0.63653 | 2.92013 | 0.68760 | 2.90769 | 0.73845 | 3         |          |
|          | 4         | 3.90892 | 0.84871 | 3.89351 | 0.91680 | 3.87692 | 0.98461 | 4         |          |
|          | 5         | 4.88615 | 1.06088 | 4.86659 | 1.14600 | 4.84615 | 1.23076 | 5         |          |
|          | 6         | 5.86338 | 1.27306 | 5.84027 | 1.37520 | 5.81538 | 1.47691 | 6         |          |
|          | 7         | 6.84061 | 1.48524 | 6.81365 | 1.60440 | 6.78461 | 1.72307 | 7         |          |
|          | 8         | 7.81784 | 1.69742 | 7.78703 | 1.83360 | 7.75384 | 1.96922 | 8         |          |
|          | 9         | 8.79507 | 1.90959 | 8.76041 | 2.06280 | 8.72307 | 2.21537 | 9         |          |
| 30'      | 1         | 0.97629 | 0.21644 | 0.97237 | 0.23344 | 0.96814 | 0.25038 | 1         | 30'      |
|          | 2         | 1.95259 | 0.43288 | 1.94474 | 0.46689 | 1.93629 | 0.50076 | 2         |          |
|          | 3         | 2.92888 | 0.64932 | 2.91711 | 0.70033 | 2.90444 | 0.75114 | 3         |          |
|          | 4         | 3.90518 | 0.86576 | 3.88948 | 0.93378 | 3.87259 | 1.00152 | 4         |          |
|          | 5         | 4.88148 | 1.08220 | 4.86185 | 1.16722 | 4.84073 | 1.25190 | 5         |          |
|          | 6         | 5.85777 | 1.29864 | 5.83422 | 1.40067 | 5.80888 | 1.50228 | 6         |          |
|          | 7         | 6.83407 | 1.51508 | 6.80659 | 1.63411 | 6.77703 | 1.75566 | 7         |          |
|          | 8         | 7.81036 | 1.73152 | 7.77896 | 1.86756 | 7.74518 | 2.00304 | 8         |          |
|          | 9         | 8.78666 | 1.94796 | 8.75133 | 2.10100 | 8.71332 | 2.25342 | 9         |          |
| 45'      | 1         | 0.97534 | 0.22069 | 0.97134 | 0.23768 | 0.96704 | 0.25460 | 1         | 15'      |
|          | 2         | 1.95068 | 0.44139 | 1.94268 | 0.47537 | 1.93409 | 0.50920 | 2         |          |
|          | 3         | 2.92602 | 0.66209 | 2.91402 | 0.71305 | 2.90113 | 0.76380 | 3         |          |
|          | 4         | 3.90136 | 0.88278 | 3.88536 | 0.95074 | 3.86818 | 1.01840 | 4         |          |
|          | 5         | 4.87671 | 1.10348 | 4.85671 | 1.18843 | 4.83523 | 1.27301 | 5         |          |
|          | 6         | 5.85205 | 1.32418 | 5.82805 | 1.42611 | 5.80227 | 1.52761 | 6         |          |
|          | 7         | 6.82739 | 1.54488 | 6.79939 | 1.66380 | 6.76932 | 1.78221 | 7         |          |
|          | 8         | 7.80273 | 1.76557 | 7.77073 | 1.90148 | 7.73636 | 2.03681 | 8         |          |
|          | 9         | 8.77808 | 1.98627 | 8.74207 | 2.13917 | 8.70341 | 2.29141 | 9         |          |
| Minutes. | Distance. | 77°     |         | 76°     |         | 75°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |

*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 15°     |         | 16°     |         | 17°     |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.96592 | 0.25881 | 0.96126 | 0.27563 | 0.95630 | 0.29237 | 1         | 60'      |
|          | 2         | 1.93185 | 0.51763 | 1.92252 | 0.55127 | 1.91260 | 0.58474 | 2         |          |
|          | 3         | 2.89777 | 0.77645 | 2.88378 | 0.82691 | 2.86891 | 0.87711 | 3         |          |
|          | 4         | 3.86370 | 1.03527 | 3.84504 | 1.10254 | 3.82521 | 1.16948 | 4         |          |
|          | 5         | 4.82962 | 1.29409 | 4.80630 | 1.37818 | 4.78152 | 1.46185 | 5         |          |
|          | 6         | 5.79555 | 1.55291 | 5.76757 | 1.65382 | 5.73782 | 1.75423 | 6         |          |
|          | 7         | 6.76148 | 1.81173 | 6.72883 | 1.92946 | 6.69413 | 2.04660 | 7         |          |
|          | 8         | 7.72740 | 2.07055 | 7.69009 | 2.20509 | 7.65043 | 2.33897 | 8         |          |
|          | 9         | 8.69333 | 2.32937 | 8.65135 | 2.48073 | 8.60674 | 2.63134 | 9         |          |
| 15'      | 1         | 0.96478 | 0.26303 | 0.96005 | 0.27982 | 0.95502 | 0.29654 | 1         | 45'      |
|          | 2         | 1.92957 | 0.52606 | 1.92010 | 0.55965 | 1.91004 | 0.59308 | 2         |          |
|          | 3         | 2.89436 | 0.78903 | 2.88015 | 0.83948 | 2.86506 | 0.88962 | 3         |          |
|          | 4         | 3.85914 | 1.05212 | 3.84020 | 1.11931 | 3.82008 | 1.18616 | 4         |          |
|          | 5         | 4.82393 | 1.31515 | 4.80025 | 1.39914 | 4.77510 | 1.48270 | 5         |          |
|          | 6         | 5.78872 | 1.57818 | 5.76030 | 1.67897 | 5.73012 | 1.77924 | 6         |          |
|          | 7         | 6.75351 | 1.84121 | 6.72035 | 1.95880 | 6.68514 | 2.07579 | 7         |          |
|          | 8         | 7.71829 | 2.10424 | 7.68040 | 2.23863 | 7.64016 | 2.37233 | 8         |          |
|          | 9         | 8.68308 | 2.36728 | 8.64045 | 2.51846 | 8.59518 | 2.66887 | 9         |          |
| 30'      | 1         | 0.96363 | 0.26723 | 0.95882 | 0.28401 | 0.95371 | 0.30070 | 1         | 30'      |
|          | 2         | 1.92726 | 0.53447 | 1.91764 | 0.56803 | 1.90743 | 0.60141 | 2         |          |
|          | 3         | 2.89089 | 0.80171 | 2.87646 | 0.85204 | 2.86115 | 0.90211 | 3         |          |
|          | 4         | 3.85452 | 1.06895 | 3.83528 | 1.13606 | 3.81486 | 1.20282 | 4         |          |
|          | 5         | 4.81815 | 1.33619 | 4.79410 | 1.42007 | 4.76858 | 1.50352 | 5         |          |
|          | 6         | 5.78178 | 1.60343 | 5.75292 | 1.70409 | 5.72230 | 1.80423 | 6         |          |
|          | 7         | 6.74541 | 1.87066 | 6.71174 | 1.98810 | 6.67601 | 2.10494 | 7         |          |
|          | 8         | 7.70904 | 2.13790 | 7.67056 | 2.27212 | 7.62973 | 2.40564 | 8         |          |
|          | 9         | 8.67267 | 2.40514 | 8.62938 | 2.55613 | 8.58345 | 2.70635 | 9         |          |
| 45'      | 1         | 0.96245 | 0.27144 | 0.95757 | 0.28819 | 0.95239 | 0.30486 | 1         | 15'      |
|          | 2         | 1.92491 | 0.54288 | 1.91514 | 0.57639 | 1.90479 | 0.60972 | 2         |          |
|          | 3         | 2.88736 | 0.81432 | 2.87271 | 0.86458 | 2.85718 | 0.91459 | 3         |          |
|          | 4         | 3.84982 | 1.08576 | 3.83028 | 1.15278 | 3.80958 | 1.21945 | 4         |          |
|          | 5         | 4.81227 | 1.35720 | 4.78785 | 1.44098 | 4.76197 | 1.52432 | 5         |          |
|          | 6         | 5.77473 | 1.62864 | 5.74542 | 1.72917 | 5.71437 | 1.82918 | 6         |          |
|          | 7         | 6.73718 | 1.90008 | 6.70299 | 2.01737 | 6.66677 | 2.13405 | 7         |          |
|          | 8         | 7.69964 | 2.17152 | 7.66057 | 2.30557 | 7.61916 | 2.43891 | 8         |          |
|          | 9         | 8.66209 | 2.44296 | 8.61814 | 2.59376 | 8.57156 | 2.74377 | 9         |          |
| Minutes. | Distance. | 74°     |         | 73°     |         | 72°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |

*Differences of Latitude and Departures—Continued.*

| Minutes | Distance | 18°     |         | 19°     |         | 20°     |         | Distance | Minutes |
|---------|----------|---------|---------|---------|---------|---------|---------|----------|---------|
|         |          | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |          |         |
| 0'      | 1        | 0.95105 | 0.30901 | 0.94551 | 0.32556 | 0.93969 | 0.34202 | 1        | 60'     |
|         | 2        | 1.90211 | 0.61803 | 1.89103 | 0.65113 | 1.87938 | 0.68404 | 2        |         |
|         | 3        | 2.85316 | 0.92705 | 2.83655 | 0.97670 | 2.81907 | 1.02606 | 3        |         |
|         | 4        | 3.80422 | 1.23606 | 3.78207 | 1.30227 | 3.75877 | 1.36808 | 4        |         |
|         | 5        | 4.75528 | 1.54508 | 4.72759 | 1.62784 | 4.69846 | 1.71010 | 5        |         |
|         | 6        | 5.70633 | 1.85410 | 5.67311 | 1.95340 | 5.63815 | 2.05212 | 6        |         |
|         | 7        | 6.65739 | 2.16311 | 6.61863 | 2.27897 | 6.57784 | 2.39414 | 7        |         |
|         | 8        | 7.60845 | 2.47213 | 7.56414 | 2.60454 | 7.51754 | 2.73616 | 8        |         |
|         | 9        | 8.55950 | 2.78115 | 8.50966 | 2.93011 | 8.45723 | 3.07818 | 9        |         |
| 15'     | 1        | 0.94969 | 0.31316 | 0.94408 | 0.32969 | 0.93819 | 0.34611 | 1        | 45'     |
|         | 2        | 1.89939 | 0.62632 | 1.88817 | 0.65938 | 1.87638 | 0.69223 | 2        |         |
|         | 3        | 2.84909 | 0.93949 | 2.83226 | 0.98907 | 2.81457 | 1.03835 | 3        |         |
|         | 4        | 3.79879 | 1.25265 | 3.77635 | 1.31876 | 3.75276 | 1.38446 | 4        |         |
|         | 5        | 4.74849 | 1.56581 | 4.72044 | 1.64845 | 4.69095 | 1.73058 | 5        |         |
|         | 6        | 5.69819 | 1.87898 | 5.66453 | 1.97814 | 5.62914 | 2.07670 | 6        |         |
|         | 7        | 6.64789 | 2.19214 | 6.60862 | 2.30783 | 6.56733 | 2.44281 | 7        |         |
|         | 8        | 7.59759 | 2.50531 | 7.55271 | 2.63752 | 7.50553 | 2.76893 | 8        |         |
|         | 9        | 8.54729 | 2.81847 | 8.49680 | 2.96721 | 8.44372 | 3.11505 | 9        |         |
| 30'     | 1        | 0.94832 | 0.31730 | 0.94264 | 0.33380 | 0.93667 | 0.35020 | 1        | 30'     |
|         | 2        | 1.89664 | 0.63460 | 1.88528 | 0.66761 | 1.87334 | 0.70041 | 2        |         |
|         | 3        | 2.84497 | 0.95191 | 2.82792 | 1.00142 | 2.81001 | 1.05062 | 3        |         |
|         | 4        | 3.79329 | 1.26921 | 3.77056 | 1.33522 | 3.74668 | 1.40082 | 4        |         |
|         | 5        | 4.74161 | 1.58652 | 4.71320 | 1.66903 | 4.68336 | 1.75103 | 5        |         |
|         | 6        | 5.68994 | 1.90382 | 5.65584 | 2.00284 | 5.62003 | 2.10124 | 6        |         |
|         | 7        | 6.63826 | 2.22113 | 6.59849 | 2.33664 | 6.55670 | 2.45145 | 7        |         |
|         | 8        | 7.58658 | 2.53843 | 7.54113 | 2.67045 | 7.49337 | 2.80165 | 8        |         |
|         | 9        | 8.53491 | 2.85574 | 8.48377 | 3.00426 | 8.43004 | 3.15186 | 9        |         |
| 45'     | 1        | 0.94693 | 0.32143 | 0.94117 | 0.33791 | 0.93513 | 0.35429 | 1        | 15'     |
|         | 2        | 1.89386 | 0.64287 | 1.88235 | 0.67583 | 1.87027 | 0.70858 | 2        |         |
|         | 3        | 2.84079 | 0.96431 | 2.82352 | 1.01375 | 2.80540 | 1.06287 | 3        |         |
|         | 4        | 3.78772 | 1.28575 | 3.76470 | 1.35166 | 3.74054 | 1.41716 | 4        |         |
|         | 5        | 4.73465 | 1.60719 | 4.70588 | 1.68958 | 4.67567 | 1.77145 | 5        |         |
|         | 6        | 5.68158 | 1.92863 | 5.64705 | 2.02750 | 5.61081 | 2.12574 | 6        |         |
|         | 7        | 6.62851 | 2.25007 | 6.58823 | 2.36541 | 6.54594 | 2.48003 | 7        |         |
|         | 8        | 7.57544 | 2.57151 | 7.52940 | 2.70333 | 7.48108 | 2.83432 | 8        |         |
|         | 9        | 8.52237 | 2.89295 | 8.47058 | 3.04125 | 8.41621 | 3.18861 | 9        |         |
| Minutes | Distance | 71°     |         | 70°     |         | 69°     |         | Distance | Minutes |
|         |          | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |          |         |

*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 21°     |         | 22°     |         | 23°     |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.93358 | 0.35836 | 0.92718 | 0.37460 | 0.92050 | 0.39073 | 1         | 60'      |
|          | 2         | 1.86716 | 0.71673 | 1.85436 | 0.74921 | 1.84100 | 0.78146 | 2         |          |
|          | 3         | 2.80074 | 1.07510 | 2.78155 | 1.12381 | 2.76151 | 1.17219 | 3         |          |
|          | 4         | 3.73432 | 1.43347 | 3.70873 | 1.49842 | 3.68201 | 1.56292 | 4         |          |
|          | 5         | 4.66790 | 1.79183 | 4.63591 | 1.87303 | 4.60252 | 1.95365 | 5         |          |
|          | 6         | 5.60148 | 2.15020 | 5.56310 | 2.24763 | 5.52302 | 2.34438 | 6         |          |
|          | 7         | 6.53506 | 2.50857 | 6.49028 | 2.62224 | 6.44353 | 2.73511 | 7         |          |
|          | 8         | 7.46864 | 2.86694 | 7.41747 | 2.99685 | 7.36403 | 3.12584 | 8         |          |
|          | 9         | 8.40222 | 3.22531 | 8.34465 | 3.37145 | 8.28454 | 3.51657 | 9         |          |
| 15'      | 1         | 0.93200 | 0.36243 | 0.92554 | 0.37864 | 0.91879 | 0.39474 | 1         | 45'      |
|          | 2         | 1.86401 | 0.72487 | 1.85108 | 0.75729 | 1.83758 | 0.78948 | 2         |          |
|          | 3         | 2.79602 | 1.08731 | 2.77662 | 1.13594 | 2.75637 | 1.18423 | 3         |          |
|          | 4         | 3.72803 | 1.44975 | 3.70216 | 1.51459 | 3.67516 | 1.57897 | 4         |          |
|          | 5         | 4.66004 | 1.81219 | 4.62770 | 1.89324 | 4.59395 | 1.97372 | 5         |          |
|          | 6         | 5.59204 | 2.17462 | 5.55324 | 2.27189 | 5.51274 | 2.36846 | 6         |          |
|          | 7         | 6.52405 | 2.53706 | 6.47878 | 2.65054 | 6.43153 | 2.76320 | 7         |          |
|          | 8         | 7.45606 | 2.89950 | 7.40432 | 3.02918 | 7.35032 | 3.15795 | 8         |          |
|          | 9         | 8.38807 | 3.26194 | 8.32986 | 3.40783 | 8.26912 | 3.55269 | 9         |          |
| 30'      | 1         | 0.93041 | 0.36650 | 0.92388 | 0.38268 | 0.91706 | 0.39874 | 1         | 30'      |
|          | 2         | 1.86083 | 0.73300 | 1.84776 | 0.76536 | 1.83412 | 0.79749 | 2         |          |
|          | 3         | 2.79125 | 1.09950 | 2.77164 | 1.14805 | 2.75118 | 1.19624 | 3         |          |
|          | 4         | 3.72167 | 1.46600 | 3.69552 | 1.53073 | 3.66824 | 1.59499 | 4         |          |
|          | 5         | 4.65208 | 1.83250 | 4.61940 | 1.91341 | 4.58530 | 1.99374 | 5         |          |
|          | 6         | 5.58250 | 2.19900 | 5.54328 | 2.29610 | 5.50236 | 2.39249 | 6         |          |
|          | 7         | 6.51292 | 2.56550 | 6.46716 | 2.67878 | 6.41942 | 2.79124 | 7         |          |
|          | 8         | 7.44334 | 2.93206 | 7.39104 | 3.06146 | 7.33648 | 3.18999 | 8         |          |
|          | 9         | 8.37375 | 3.29851 | 8.31492 | 3.44415 | 8.25354 | 3.58874 | 9         |          |
| 45'      | 1         | 0.92881 | 0.37055 | 0.92220 | 0.38671 | 0.91531 | 0.40274 | 1         | 15'      |
|          | 2         | 1.85762 | 0.74111 | 1.84440 | 0.77342 | 1.83062 | 0.80549 | 2         |          |
|          | 3         | 2.78643 | 1.11167 | 2.76660 | 1.16013 | 2.74593 | 1.20824 | 3         |          |
|          | 4         | 3.71524 | 1.48222 | 3.68880 | 1.54684 | 3.66124 | 1.61098 | 4         |          |
|          | 5         | 4.64405 | 1.85278 | 4.61100 | 1.93355 | 4.57655 | 2.01373 | 5         |          |
|          | 6         | 5.57286 | 2.22334 | 5.53320 | 2.32026 | 5.49186 | 2.41648 | 6         |          |
|          | 7         | 6.50167 | 2.59390 | 6.45540 | 2.70637 | 6.40718 | 2.81922 | 7         |          |
|          | 8         | 7.43048 | 2.96445 | 7.37760 | 3.09368 | 7.32249 | 3.22197 | 8         |          |
|          | 9         | 8.35929 | 3.33501 | 8.29980 | 3.48039 | 8.23780 | 3.62472 | 9         |          |
| Minutes. | Distance. | 65°     |         | 67°     |         | 66°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |

*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 24°     |         | 25°     |         | 26°     |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.91354 | 0.40673 | 0.90630 | 0.42261 | 0.89879 | 0.43837 | 1         |          |
|          | 2         | 1.82709 | 0.81347 | 1.81261 | 0.84523 | 1.79758 | 0.87674 | 2         |          |
|          | 3         | 2.74063 | 1.22020 | 2.71892 | 1.26785 | 2.69638 | 1.31511 | 3         |          |
|          | 4         | 3.65418 | 1.62694 | 3.62523 | 1.69047 | 3.59517 | 1.75348 | 4         |          |
|          | 5         | 4.56772 | 2.03368 | 4.53153 | 2.11309 | 4.49397 | 2.19185 | 5         | 60'      |
|          | 6         | 5.48127 | 2.44041 | 5.43784 | 2.53570 | 5.39276 | 2.63022 | 6         |          |
|          | 7         | 6.39481 | 2.84715 | 6.34415 | 2.95832 | 6.29155 | 3.06859 | 7         |          |
|          | 8         | 7.30836 | 3.25389 | 7.25046 | 3.38094 | 7.19035 | 3.50696 | 8         |          |
|          | 9         | 8.22190 | 3.66062 | 8.15677 | 3.80356 | 8.08914 | 3.94533 | 9         |          |
| 15'      | 1         | 0.91176 | 0.41071 | 0.90445 | 0.42656 | 0.89687 | 0.44228 | 1         |          |
|          | 2         | 1.82352 | 0.82143 | 1.80891 | 0.85313 | 1.79374 | 0.88457 | 2         |          |
|          | 3         | 2.73529 | 1.23215 | 2.71336 | 1.27970 | 2.69061 | 1.32666 | 3         |          |
|          | 4         | 3.64704 | 1.64287 | 3.61782 | 1.70627 | 3.58749 | 1.76915 | 4         |          |
|          | 5         | 4.55881 | 2.05359 | 4.52227 | 2.13284 | 4.48436 | 2.21144 | 5         | 45'      |
|          | 6         | 5.47057 | 2.46431 | 5.42673 | 2.55941 | 5.38123 | 2.65373 | 6         |          |
|          | 7         | 6.38233 | 2.87503 | 6.33118 | 2.98598 | 6.27810 | 3.09602 | 7         |          |
|          | 8         | 7.29409 | 3.28575 | 7.23564 | 3.41254 | 7.17498 | 3.53830 | 8         |          |
|          | 9         | 8.20585 | 3.69647 | 8.14009 | 3.83911 | 8.07185 | 3.98059 | 9         |          |
| 30'      | 1         | 0.90996 | 0.41469 | 0.90258 | 0.43051 | 0.89493 | 0.44619 | 1         |          |
|          | 2         | 1.81992 | 0.82938 | 1.80517 | 0.86102 | 1.78986 | 0.89239 | 2         |          |
|          | 3         | 2.72988 | 1.24407 | 2.70775 | 1.29153 | 2.68480 | 1.33859 | 3         |          |
|          | 4         | 3.63984 | 1.65877 | 3.61034 | 1.72204 | 3.57973 | 1.78479 | 4         |          |
|          | 5         | 4.54980 | 2.07346 | 4.51292 | 2.15255 | 4.47467 | 2.23098 | 5         | 30'      |
|          | 6         | 5.45976 | 2.48815 | 5.41551 | 2.58306 | 5.36960 | 2.67718 | 6         |          |
|          | 7         | 6.36972 | 2.90285 | 6.31809 | 3.01357 | 6.26454 | 3.12338 | 7         |          |
|          | 8         | 7.27969 | 3.31754 | 7.22068 | 3.44408 | 7.15947 | 3.56958 | 8         |          |
|          | 9         | 8.18965 | 3.73223 | 8.12326 | 3.87459 | 8.05440 | 4.01578 | 9         |          |
| 45'      | 1         | 0.90814 | 0.41866 | 0.90069 | 0.43444 | 0.89297 | 0.45009 | 1         |          |
|          | 2         | 1.81628 | 0.83732 | 1.80139 | 0.86889 | 1.78595 | 0.90019 | 2         |          |
|          | 3         | 2.72442 | 1.25598 | 2.70209 | 1.30333 | 2.67893 | 1.35029 | 3         |          |
|          | 4         | 3.63257 | 1.67464 | 3.60279 | 1.73778 | 3.57191 | 1.80039 | 4         |          |
|          | 5         | 4.54071 | 2.09330 | 4.50349 | 2.17222 | 4.46489 | 2.25049 | 5         | 15'      |
|          | 6         | 5.44885 | 2.51196 | 5.40418 | 2.60667 | 5.35787 | 2.70059 | 6         |          |
|          | 7         | 6.35700 | 2.93062 | 6.30488 | 3.04111 | 6.25085 | 3.15068 | 7         |          |
|          | 8         | 7.26514 | 3.34928 | 7.20558 | 3.47556 | 7.14383 | 3.60078 | 8         |          |
|          | 9         | 8.17328 | 3.76794 | 8.10628 | 3.91000 | 8.03681 | 4.05088 | 9         |          |
| Minutes. | Distance. | 65°     |         | 64°     |         | 63°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |



*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 27°     |         | 28°     |         | 29°     |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.89100 | 0.45399 | 0.88294 | 0.46947 | 0.87462 | 0.48481 | 1         | 60'      |
|          | 2         | 1.78201 | 0.90798 | 1.76589 | 0.93894 | 1.74924 | 0.96962 | 2         |          |
|          | 3         | 2.67301 | 1.36197 | 2.64884 | 1.40841 | 2.62386 | 1.45443 | 3         |          |
|          | 4         | 3.56402 | 1.81596 | 3.53179 | 1.87788 | 3.49848 | 1.93924 | 4         |          |
|          | 5         | 4.45503 | 2.26995 | 4.41473 | 2.34735 | 4.37310 | 2.42405 | 5         |          |
|          | 6         | 5.34603 | 2.72394 | 5.29768 | 2.81682 | 5.24772 | 2.90886 | 6         |          |
|          | 7         | 6.23704 | 3.17793 | 6.18063 | 3.28630 | 6.12234 | 3.39367 | 7         |          |
|          | 8         | 7.12805 | 3.63193 | 7.06358 | 3.75577 | 6.99696 | 3.87848 | 8         |          |
|          | 9         | 8.01905 | 4.08591 | 7.94652 | 4.22524 | 7.87156 | 4.36329 | 9         |          |
| 15'      | 1         | 0.88901 | 0.45787 | 0.88089 | 0.47332 | 0.87249 | 0.48862 | 1         | 45'      |
|          | 2         | 1.77803 | 0.91574 | 1.76178 | 0.94664 | 1.74499 | 0.97724 | 2         |          |
|          | 3         | 2.66705 | 1.37362 | 2.64267 | 1.41996 | 2.61748 | 1.46566 | 3         |          |
|          | 4         | 3.55606 | 1.83149 | 3.52356 | 1.89328 | 3.48998 | 1.95448 | 4         |          |
|          | 5         | 4.44508 | 2.28937 | 4.40445 | 2.36660 | 4.36248 | 2.44310 | 5         |          |
|          | 6         | 5.33410 | 2.74724 | 5.28534 | 2.83992 | 5.23497 | 2.93172 | 6         |          |
|          | 7         | 6.22311 | 3.20511 | 6.16623 | 3.31324 | 6.10747 | 3.42034 | 7         |          |
|          | 8         | 7.11213 | 3.66299 | 7.04712 | 3.78656 | 6.97996 | 3.90896 | 8         |          |
|          | 9         | 8.00115 | 4.12086 | 7.92801 | 4.25988 | 7.85246 | 4.39759 | 9         |          |
| 30'      | 1         | 0.88701 | 0.46174 | 0.87881 | 0.47715 | 0.87035 | 0.49242 | 1         | 30'      |
|          | 2         | 1.77402 | 0.92349 | 1.75763 | 0.95431 | 1.74071 | 0.98484 | 2         |          |
|          | 3         | 2.66103 | 1.38524 | 2.63645 | 1.43147 | 2.61106 | 1.47727 | 3         |          |
|          | 4         | 3.54804 | 1.84699 | 3.51526 | 1.90863 | 3.48142 | 1.96969 | 4         |          |
|          | 5         | 4.43505 | 2.30874 | 4.39408 | 2.38579 | 4.35177 | 2.46211 | 5         |          |
|          | 6         | 5.32206 | 2.77049 | 5.27290 | 2.86295 | 5.22213 | 2.95454 | 6         |          |
|          | 7         | 6.20907 | 3.23224 | 6.15171 | 3.34011 | 6.09248 | 3.44696 | 7         |          |
|          | 8         | 7.09608 | 3.69398 | 7.03053 | 3.81727 | 6.96284 | 3.93938 | 8         |          |
|          | 9         | 7.98309 | 4.15573 | 7.90935 | 4.29442 | 7.83320 | 4.43181 | 9         |          |
| 45'      | 1         | 0.88498 | 0.46561 | 0.87672 | 0.48098 | 0.86819 | 0.49621 | 1         | 15'      |
|          | 2         | 1.76997 | 0.93122 | 1.75345 | 0.96197 | 1.73639 | 0.99243 | 2         |          |
|          | 3         | 2.65496 | 1.39684 | 2.63018 | 1.44296 | 2.60459 | 1.48864 | 3         |          |
|          | 4         | 3.53995 | 1.86245 | 3.50690 | 1.92395 | 3.47279 | 1.98486 | 4         |          |
|          | 5         | 4.42493 | 2.32807 | 4.38363 | 2.40494 | 4.34099 | 2.48108 | 5         |          |
|          | 6         | 5.30992 | 2.79368 | 5.26036 | 2.88593 | 5.20919 | 2.97729 | 6         |          |
|          | 7         | 6.19491 | 3.25930 | 6.13708 | 3.36632 | 6.07739 | 3.47351 | 7         |          |
|          | 8         | 7.07990 | 3.72491 | 7.01381 | 3.84791 | 6.94559 | 3.96973 | 8         |          |
|          | 9         | 7.96488 | 4.19053 | 7.89054 | 4.32889 | 7.81378 | 4.46594 | 9         |          |
| Minutes. | Distance. | 62°     |         | 61°     |         | 60°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |

*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 30°     |         | 31°     |         | 32°     |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.86602 | 0.50000 | 0.85716 | 0.51503 | 0.84804 | 0.52991 | 1         | 60'      |
|          | 2         | 1.73205 | 1.00000 | 1.71433 | 1.03007 | 1.69609 | 1.05983 | 2         |          |
|          | 3         | 2.59807 | 1.50000 | 2.57150 | 1.54511 | 2.54414 | 1.58975 | 3         |          |
|          | 4         | 3.46410 | 2.00000 | 3.42866 | 2.06015 | 3.39219 | 2.11967 | 4         |          |
|          | 5         | 4.33012 | 2.50000 | 4.28583 | 2.57519 | 4.24024 | 2.64959 | 5         |          |
|          | 6         | 5.19615 | 3.00000 | 5.14300 | 3.09022 | 5.08828 | 3.17951 | 6         |          |
|          | 7         | 6.06217 | 3.50000 | 6.00017 | 3.60526 | 5.93633 | 3.70943 | 7         |          |
|          | 8         | 6.92820 | 4.00000 | 6.85733 | 4.12030 | 6.78438 | 4.23935 | 8         |          |
|          | 9         | 7.79422 | 4.50000 | 7.71450 | 4.63534 | 7.63243 | 4.76927 | 9         |          |
| 15'      | 1         | 0.86383 | 0.50377 | 0.85491 | 0.51877 | 0.84572 | 0.53361 | 1         | 45'      |
|          | 2         | 1.72767 | 1.00754 | 1.70982 | 1.03754 | 1.69145 | 1.06722 | 2         |          |
|          | 3         | 2.59150 | 1.51132 | 2.56473 | 1.55631 | 2.53718 | 1.60084 | 3         |          |
|          | 4         | 3.45534 | 2.01509 | 3.41964 | 2.07509 | 3.38291 | 2.13445 | 4         |          |
|          | 5         | 4.31917 | 2.51887 | 4.27456 | 2.59386 | 4.22863 | 2.66807 | 5         |          |
|          | 6         | 5.18301 | 3.02264 | 5.12947 | 3.11263 | 5.07436 | 3.20168 | 6         |          |
|          | 7         | 6.04684 | 3.52641 | 5.98438 | 3.63141 | 5.92009 | 3.73530 | 7         |          |
|          | 8         | 6.91068 | 4.03019 | 6.83929 | 4.15018 | 6.76582 | 4.26891 | 8         |          |
|          | 9         | 7.77451 | 4.53396 | 7.69420 | 4.66895 | 7.61155 | 4.80253 | 9         |          |
| 30'      | 1         | 0.86162 | 0.50753 | 0.85264 | 0.52249 | 0.84339 | 0.53730 | 1         | 30'      |
|          | 2         | 1.72325 | 1.01507 | 1.70528 | 1.04499 | 1.68678 | 1.07460 | 2         |          |
|          | 3         | 2.58488 | 1.52261 | 2.55792 | 1.56749 | 2.53017 | 1.61190 | 3         |          |
|          | 4         | 3.44651 | 2.03015 | 3.41056 | 2.08999 | 3.37356 | 2.14920 | 4         |          |
|          | 5         | 4.30814 | 2.53769 | 4.26320 | 2.61249 | 4.21695 | 2.68650 | 5         |          |
|          | 6         | 5.16977 | 3.04523 | 5.11584 | 3.13499 | 5.06034 | 3.22380 | 6         |          |
|          | 7         | 6.03140 | 3.55276 | 5.96948 | 3.65749 | 5.90373 | 3.76110 | 7         |          |
|          | 8         | 6.89303 | 4.06030 | 6.82112 | 4.17998 | 6.74713 | 4.29840 | 8         |          |
|          | 9         | 7.75466 | 4.56784 | 7.67376 | 4.70248 | 7.59052 | 4.83570 | 9         |          |
| 45'      | 1         | 0.85940 | 0.51129 | 0.85035 | 0.52621 | 0.84103 | 0.54097 | 1         | 15'      |
|          | 2         | 1.71881 | 1.02258 | 1.70070 | 1.05242 | 1.68207 | 1.08194 | 2         |          |
|          | 3         | 2.57821 | 1.53387 | 2.55105 | 1.57864 | 2.52311 | 1.62292 | 3         |          |
|          | 4         | 3.43762 | 2.04517 | 3.40140 | 2.10485 | 3.36415 | 2.16389 | 4         |          |
|          | 5         | 4.29703 | 2.55646 | 4.25176 | 2.63107 | 4.20519 | 2.70487 | 5         |          |
|          | 6         | 5.15643 | 3.06775 | 5.10211 | 3.15728 | 5.04623 | 3.24584 | 6         |          |
|          | 7         | 6.01584 | 3.57905 | 5.95246 | 3.68349 | 5.88827 | 3.78682 | 7         |          |
|          | 8         | 6.87525 | 4.09034 | 6.80281 | 4.20971 | 6.72831 | 4.32779 | 8         |          |
|          | 9         | 7.73465 | 4.60163 | 7.65316 | 4.73592 | 7.56935 | 4.86877 | 9         |          |
| Minutes. | Distance. | 59°     |         | 58°     |         | 57°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |

*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 33°     |         | 34°     |         | 35°     |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.83867 | 0.54463 | 0.82903 | 0.55919 | 0.81915 | 0.57357 | 1         | 60'      |
|          | 2         | 1.67734 | 1.08927 | 1.65807 | 1.11838 | 1.63830 | 1.14715 | 2         |          |
|          | 3         | 2.51601 | 1.63391 | 2.48711 | 1.67757 | 2.45745 | 1.72072 | 3         |          |
|          | 4         | 3.35468 | 2.17855 | 3.31615 | 2.23677 | 3.27660 | 2.29430 | 4         |          |
|          | 5         | 4.19335 | 2.72319 | 4.14518 | 2.79596 | 4.09576 | 2.86788 | 5         |          |
|          | 6         | 5.03202 | 3.26783 | 4.97422 | 3.35515 | 4.91491 | 3.44145 | 6         |          |
|          | 7         | 5.87069 | 3.81247 | 5.80326 | 3.91435 | 5.73406 | 4.01503 | 7         |          |
|          | 8         | 6.70936 | 4.35711 | 6.63230 | 4.47354 | 6.55321 | 4.58861 | 8         |          |
|          | 9         | 7.54803 | 4.90175 | 7.46133 | 5.03473 | 7.37236 | 5.16218 | 9         |          |
| 15'      | 1         | 0.83628 | 0.54829 | 0.82659 | 0.56280 | 0.81664 | 0.57714 | 1         | 45'      |
|          | 2         | 1.67257 | 1.09658 | 1.65318 | 1.12560 | 1.63328 | 1.15429 | 2         |          |
|          | 3         | 2.50885 | 1.64487 | 2.47977 | 1.68841 | 2.44992 | 1.73143 | 3         |          |
|          | 4         | 3.34514 | 2.19317 | 3.30636 | 2.25121 | 3.26656 | 2.30858 | 4         |          |
|          | 5         | 4.18143 | 2.74146 | 4.13295 | 2.81402 | 4.08320 | 2.88572 | 5         |          |
|          | 6         | 5.01771 | 3.28975 | 4.95954 | 3.37682 | 4.89984 | 3.46287 | 6         |          |
|          | 7         | 5.85400 | 3.83805 | 5.78613 | 3.93963 | 5.71649 | 4.04001 | 7         |          |
|          | 8         | 6.69028 | 4.38634 | 6.61272 | 4.50243 | 6.53313 | 4.61716 | 8         |          |
|          | 9         | 7.52657 | 4.93463 | 7.43931 | 5.06524 | 7.34977 | 5.19430 | 9         |          |
| 30'      | 1         | 0.83388 | 0.55193 | 0.82412 | 0.56640 | 0.81411 | 0.58070 | 1         | 30'      |
|          | 2         | 1.66777 | 1.10387 | 1.64825 | 1.13281 | 1.62823 | 1.16140 | 2         |          |
|          | 3         | 2.50165 | 1.65581 | 2.47237 | 1.69921 | 2.44234 | 1.74210 | 3         |          |
|          | 4         | 3.33554 | 2.20774 | 3.29650 | 2.26562 | 3.25646 | 2.32281 | 4         |          |
|          | 5         | 4.16942 | 2.75968 | 4.12063 | 2.83203 | 4.07057 | 2.90351 | 5         |          |
|          | 6         | 5.00331 | 3.31162 | 4.94475 | 3.39843 | 4.88469 | 3.48421 | 6         |          |
|          | 7         | 5.83720 | 3.86355 | 5.76888 | 3.96484 | 5.69880 | 4.06492 | 7         |          |
|          | 8         | 6.67108 | 4.41549 | 6.59300 | 4.53124 | 6.51292 | 4.64562 | 8         |          |
|          | 9         | 7.50497 | 4.96743 | 7.41713 | 5.09765 | 7.32703 | 5.22632 | 9         |          |
| 45'      | 1         | 0.83147 | 0.55557 | 0.82164 | 0.56999 | 0.81157 | 0.58425 | 1         | 15'      |
|          | 2         | 1.66294 | 1.11114 | 1.64329 | 1.13999 | 1.62314 | 1.16850 | 2         |          |
|          | 3         | 2.49441 | 1.66671 | 2.46494 | 1.70999 | 2.43472 | 1.75275 | 3         |          |
|          | 4         | 3.32588 | 2.22226 | 3.28658 | 2.27998 | 3.24629 | 2.33700 | 4         |          |
|          | 5         | 4.15735 | 2.77785 | 4.10823 | 2.84998 | 4.05787 | 2.92125 | 5         |          |
|          | 6         | 4.98882 | 3.33342 | 4.92988 | 3.41998 | 4.86944 | 3.50550 | 6         |          |
|          | 7         | 5.82029 | 3.88899 | 5.75152 | 3.98997 | 5.68101 | 4.08975 | 7         |          |
|          | 8         | 6.65176 | 4.44456 | 6.57317 | 4.55997 | 6.49260 | 4.67400 | 8         |          |
|          | 9         | 7.48323 | 5.00013 | 7.39482 | 5.12997 | 7.30416 | 5.25825 | 9         |          |
| Minutes. | Distance. | 56°     |         | 55°     |         | 54°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |

*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 36°     |         | 37°     |         | 38°     |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
|          | 1         | 0.80901 | 0.58778 | 0.79863 | 0.60181 | 0.78801 | 0.61566 | 1         |          |
|          | 2         | 1.61803 | 1.17557 | 1.59727 | 1.20363 | 1.57602 | 1.23132 | 2         |          |
|          | 3         | 2.42705 | 1.76335 | 2.39590 | 1.80544 | 2.36403 | 1.84698 | 3         |          |
|          | 4         | 3.23606 | 2.35114 | 3.19454 | 2.40726 | 3.15204 | 2.46264 | 4         |          |
| 0'       | 5         | 4.04508 | 2.93892 | 3.99317 | 3.00907 | 3.94005 | 3.07830 | 5         | 60'      |
|          | 6         | 4.85410 | 3.52671 | 4.79181 | 3.61089 | 4.72806 | 3.69396 | 6         |          |
|          | 7         | 5.66311 | 4.11449 | 5.59044 | 4.21270 | 5.51607 | 4.30963 | 7         |          |
|          | 8         | 6.47213 | 4.70228 | 6.38908 | 4.81452 | 6.30408 | 4.92529 | 8         |          |
|          | 9         | 7.28115 | 5.29006 | 7.18771 | 5.41633 | 7.09209 | 5.54095 | 9         |          |
|          | 1         | 0.80644 | 0.59130 | 0.79600 | 0.60529 | 1.78531 | 0.61909 | 1         |          |
|          | 2         | 1.61288 | 1.18261 | 1.59200 | 1.21058 | 1.57063 | 1.23818 | 2         |          |
|          | 3         | 2.41933 | 1.77392 | 2.38800 | 1.81588 | 2.35595 | 1.85728 | 3         |          |
|          | 4         | 3.22577 | 2.36523 | 3.18400 | 2.42117 | 3.14126 | 2.47637 | 4         |          |
| 15'      | 5         | 4.03222 | 2.95654 | 3.98001 | 3.02647 | 3.92658 | 3.09547 | 5         | 45'      |
|          | 6         | 4.83866 | 3.54785 | 4.77601 | 3.63176 | 4.71190 | 3.71456 | 6         |          |
|          | 7         | 5.64511 | 4.13916 | 5.57201 | 4.23705 | 5.49721 | 4.33365 | 7         |          |
|          | 8         | 6.45155 | 4.73047 | 6.36801 | 4.84235 | 6.28253 | 4.95275 | 8         |          |
|          | 9         | 7.25800 | 5.32178 | 7.16401 | 5.44764 | 7.06785 | 5.57184 | 9         |          |
|          | 1         | 0.80385 | 0.59482 | 0.79335 | 0.60876 | 0.78260 | 0.62251 | 1         |          |
|          | 2         | 1.60771 | 1.18964 | 1.58670 | 1.21752 | 1.56521 | 1.24502 | 2         |          |
|          | 3         | 2.41157 | 1.78446 | 2.38005 | 1.82628 | 2.34782 | 1.86754 | 3         |          |
|          | 4         | 3.21542 | 2.37929 | 3.17341 | 2.43504 | 3.13043 | 2.49005 | 4         |          |
| 30'      | 5         | 4.01928 | 2.97411 | 3.96676 | 3.04380 | 3.91304 | 3.11257 | 5         | 30'      |
|          | 6         | 4.82314 | 3.56893 | 4.76011 | 3.65256 | 4.69564 | 3.73508 | 6         |          |
|          | 7         | 5.62699 | 4.16375 | 5.55347 | 4.26132 | 5.47825 | 4.35760 | 7         |          |
|          | 8         | 6.43085 | 4.75858 | 6.34682 | 4.87009 | 6.26086 | 4.98011 | 8         |          |
|          | 9         | 7.23471 | 5.35340 | 7.14017 | 5.47885 | 7.04347 | 5.60263 | 9         |          |
|          | 1         | 0.80125 | 0.59832 | 0.79068 | 0.61221 | 0.77988 | 0.62592 | 1         |          |
|          | 2         | 1.60250 | 1.19664 | 1.58137 | 1.22443 | 1.55946 | 1.25184 | 2         |          |
|          | 3         | 2.40376 | 1.79497 | 2.37206 | 1.83665 | 2.33965 | 1.87777 | 3         |          |
|          | 4         | 3.20501 | 2.39329 | 3.16275 | 2.44886 | 3.11953 | 2.50369 | 4         |          |
| 45'      | 5         | 4.00626 | 2.99162 | 3.95344 | 3.06108 | 3.89942 | 3.12961 | 5         | 15'      |
|          | 6         | 4.80752 | 3.58994 | 4.74413 | 3.67330 | 4.67930 | 3.75554 | 6         |          |
|          | 7         | 5.60877 | 4.18627 | 5.53482 | 4.28552 | 5.45919 | 4.38146 | 7         |          |
|          | 8         | 6.41003 | 4.78659 | 6.32551 | 4.89773 | 6.23907 | 5.00738 | 8         |          |
|          | 9         | 7.21128 | 5.38492 | 7.11620 | 5.50995 | 7.01896 | 5.63331 | 9         |          |
| Minutes. | Distance. | 53°     |         | 52°     |         | 51°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |

*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 39°     |         | 40°     |         | 41°     |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.77714 | 0.62932 | 0.76604 | 0.64278 | 0.75470 | 0.65605 | 1         | 60'      |
|          | 2         | 1.55429 | 1.25864 | 1.53208 | 1.28557 | 1.50941 | 1.31211 | 2         |          |
|          | 3         | 2.33143 | 1.88796 | 2.29813 | 1.92836 | 2.26419 | 1.96817 | 3         |          |
|          | 4         | 3.10858 | 2.51728 | 3.06417 | 2.57115 | 3.01883 | 2.62423 | 4         |          |
|          | 5         | 3.88573 | 3.14660 | 3.83022 | 3.21393 | 3.77354 | 3.28029 | 5         |          |
|          | 6         | 4.66287 | 3.77592 | 4.59626 | 3.85672 | 4.52825 | 3.93635 | 6         |          |
|          | 7         | 5.44002 | 4.40524 | 5.36231 | 4.49951 | 5.28296 | 4.59241 | 7         |          |
|          | 8         | 6.21716 | 5.03456 | 6.12835 | 5.14230 | 6.03767 | 5.24847 | 8         |          |
|          | 9         | 6.99431 | 5.66388 | 6.89439 | 5.78508 | 6.79236 | 5.90453 | 9         |          |
| 15'      | 1         | 0.77439 | 0.63270 | 0.76323 | 0.64612 | 0.75184 | 0.65934 | 1         | 45'      |
|          | 2         | 1.54878 | 1.26541 | 1.52646 | 1.29224 | 1.50368 | 1.31869 | 2         |          |
|          | 3         | 2.32317 | 1.89811 | 2.28969 | 1.93837 | 2.25552 | 1.97803 | 3         |          |
|          | 4         | 3.09757 | 2.53082 | 3.05293 | 2.58449 | 3.00736 | 2.63738 | 4         |          |
|          | 5         | 3.87196 | 3.16352 | 3.81616 | 3.23062 | 3.75920 | 3.29672 | 5         |          |
|          | 6         | 4.64635 | 3.79623 | 4.57939 | 3.87674 | 4.51104 | 3.95607 | 6         |          |
|          | 7         | 5.42074 | 4.42893 | 5.34262 | 4.52286 | 5.26288 | 4.61542 | 7         |          |
|          | 8         | 6.19514 | 5.06164 | 6.10586 | 5.16899 | 6.01472 | 5.27476 | 8         |          |
|          | 9         | 6.96953 | 5.69434 | 6.86909 | 5.81511 | 6.76656 | 5.93411 | 9         |          |
| 30'      | 1         | 0.77162 | 0.63607 | 0.76040 | 0.64944 | 0.74895 | 0.66262 | 1         | 30'      |
|          | 2         | 1.54324 | 1.27215 | 1.52081 | 1.29889 | 1.49791 | 1.32524 | 2         |          |
|          | 3         | 2.31487 | 1.90823 | 2.28121 | 1.94834 | 2.24686 | 1.98786 | 3         |          |
|          | 4         | 3.08649 | 2.54431 | 3.04162 | 2.59779 | 2.99582 | 2.65048 | 4         |          |
|          | 5         | 3.85812 | 3.18039 | 3.80203 | 3.24724 | 3.74477 | 3.31310 | 5         |          |
|          | 6         | 4.62974 | 3.81646 | 4.56243 | 3.89668 | 4.49373 | 3.97572 | 6         |          |
|          | 7         | 5.40137 | 4.45254 | 5.32284 | 4.54613 | 5.24268 | 4.63834 | 7         |          |
|          | 8         | 6.17299 | 5.08862 | 6.08324 | 5.19556 | 5.99164 | 5.30096 | 8         |          |
|          | 9         | 6.94462 | 5.72470 | 6.84365 | 5.84503 | 6.74060 | 5.96358 | 9         |          |
| 45'      | 1         | 0.76884 | 0.63943 | 0.75756 | 0.65276 | 0.74605 | 0.66588 | 1         | 15'      |
|          | 2         | 1.53768 | 1.27887 | 1.51513 | 1.30552 | 1.49211 | 1.33176 | 2         |          |
|          | 3         | 2.30652 | 1.91831 | 2.27269 | 1.95828 | 2.23817 | 1.99764 | 3         |          |
|          | 4         | 3.07536 | 2.55775 | 3.03026 | 2.61104 | 2.98422 | 2.66352 | 4         |          |
|          | 5         | 3.84420 | 3.19719 | 3.78782 | 2.26380 | 3.73028 | 3.32940 | 5         |          |
|          | 6         | 4.61305 | 3.83663 | 4.54539 | 3.91656 | 4.47634 | 3.99529 | 6         |          |
|          | 7         | 5.38189 | 4.47607 | 5.30295 | 4.56932 | 5.22240 | 4.66117 | 7         |          |
|          | 8         | 6.15073 | 5.11551 | 6.06052 | 5.22208 | 5.96845 | 5.32705 | 8         |          |
|          | 9         | 6.91957 | 5.75495 | 6.81808 | 5.87484 | 6.71451 | 5.99293 | 9         |          |
| Minutes. | Distance. | 50°     |         | 49°     |         | 48°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |

*Differences of Latitude and Departures—Continued.*

| Minutes. | Distance. | 42°     |         | 43°     |         | 44°     |         | Distance. | Minutes. |
|----------|-----------|---------|---------|---------|---------|---------|---------|-----------|----------|
|          |           | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    |           |          |
| 0'       | 1         | 0.74314 | 0.66913 | 0.73135 | 0.68199 | 0.71933 | 0.69465 | 1         |          |
|          | 2         | 1.48628 | 1.33826 | 1.46270 | 1.36399 | 1.43867 | 1.38931 | 2         |          |
|          | 3         | 2.22943 | 2.00739 | 2.19406 | 2.04599 | 2.15801 | 2.08397 | 3         |          |
|          | 4         | 2.97257 | 2.67652 | 2.92541 | 2.72799 | 2.87735 | 2.77863 | 4         |          |
|          | 5         | 3.71572 | 3.34565 | 3.65676 | 3.40999 | 3.59669 | 3.47329 | 5         | 60'      |
|          | 6         | 4.45886 | 4.01478 | 4.38812 | 4.09199 | 4.31603 | 4.16795 | 6         |          |
|          | 7         | 5.20201 | 4.68391 | 5.11947 | 4.77398 | 5.03537 | 4.86260 | 7         |          |
|          | 8         | 5.94515 | 5.35304 | 5.85082 | 5.45598 | 5.75471 | 5.55726 | 8         |          |
|          | 9         | 6.68830 | 6.02217 | 6.58218 | 6.13798 | 6.47405 | 6.25192 | 9         |          |
| 15'      | 1         | 0.74021 | 0.67236 | 0.72837 | 1.68518 | 0.71630 | 0.69779 | 1         |          |
|          | 2         | 1.48043 | 1.34473 | 1.45674 | 0.37036 | 1.43260 | 1.39558 | 2         |          |
|          | 3         | 2.22065 | 2.01710 | 2.18511 | 2.05554 | 2.14890 | 2.09337 | 3         |          |
|          | 4         | 2.96087 | 2.68946 | 2.91348 | 2.74073 | 2.86520 | 2.79116 | 4         |          |
|          | 5         | 3.70109 | 3.36183 | 3.64185 | 3.42591 | 3.58151 | 3.48895 | 5         | 45'      |
|          | 6         | 4.44130 | 4.03420 | 4.37022 | 4.11109 | 4.29781 | 4.18674 | 6         |          |
|          | 7         | 5.18152 | 4.70656 | 5.09859 | 4.79628 | 5.01411 | 4.88453 | 7         |          |
|          | 8         | 5.92174 | 5.37893 | 5.82696 | 5.48146 | 5.73041 | 5.58232 | 8         |          |
|          | 9         | 6.66196 | 6.05130 | 6.55533 | 6.16664 | 6.44671 | 6.28C11 | 9         |          |
| 30'      | 1         | 0.73727 | 0.67559 | 0.72537 | 0.68835 | 0.71325 | 0.70090 | 1         |          |
|          | 2         | 1.47455 | 1.35118 | 1.45074 | 1.37670 | 1.42650 | 1.40181 | 2         |          |
|          | 3         | 2.21183 | 2.02677 | 2.17612 | 2.06506 | 2.13975 | 2.10272 | 3         |          |
|          | 4         | 2.94910 | 2.70236 | 2.90149 | 2.75341 | 2.85300 | 2.80363 | 4         |          |
|          | 5         | 3.68638 | 3.37795 | 3.62687 | 3.44177 | 3.56625 | 3.50454 | 5         | 30'      |
|          | 6         | 4.42366 | 4.05354 | 4.35224 | 4.13012 | 4.27950 | 4.20545 | 6         |          |
|          | 7         | 5.16094 | 4.72913 | 5.07762 | 4.81848 | 5.09275 | 4.90636 | 7         |          |
|          | 8         | 5.89821 | 5.40472 | 5.80299 | 5.50683 | 5.70600 | 5.60727 | 8         |          |
|          | 9         | 6.63549 | 6.08031 | 6.52836 | 6.19519 | 6.41925 | 6.30818 | 9         |          |
| 45'      | 1         | 0.73432 | 0.67880 | 0.72236 | 0.69151 | 0.71018 | 0.70401 | 1         |          |
|          | 2         | 1.46864 | 1.35760 | 1.44472 | 1.38302 | 1.42037 | 1.40802 | 2         |          |
|          | 3         | 2.20296 | 2.03640 | 2.16709 | 2.07453 | 2.13055 | 2.11204 | 3         |          |
|          | 4         | 2.93729 | 2.71520 | 2.88945 | 2.76605 | 2.84074 | 2.81605 | 4         |          |
|          | 5         | 3.67161 | 3.39400 | 3.61182 | 3.45756 | 3.55092 | 3.52607 | 5         | 15'      |
|          | 6         | 4.40593 | 4.07280 | 4.33418 | 4.14907 | 4.26111 | 4.22408 | 6         |          |
|          | 7         | 5.14025 | 4.75160 | 5.05654 | 4.84059 | 4.97129 | 4.92810 | 7         |          |
|          | 8         | 5.87458 | 5.43040 | 5.77891 | 5.53210 | 5.68148 | 5.63211 | 8         |          |
|          | 9         | 6.60890 | 6.10920 | 6.50127 | 6.22361 | 6.39166 | 6.33613 | 9         |          |
| Minutes. | Distance. | 47°     |         | 46°     |         | 45°     |         | Distance. | Minutes. |
|          |           | Dep.    | Lat.    | Dep.    | Lat.    | Dep.    | Lat.    |           |          |

*Differences of Latitude and Departure—Continued.*

| 45°  |         |         |   |  |
|------|---------|---------|---|--|
| Lat. |         | Dep.    |   |  |
| 1    | 0.70710 | 0.70710 | 1 |  |
| 2    | 1.41421 | 1.41421 | 2 |  |
| 3    | 2.12132 | 2.12132 | 3 |  |
| 4    | 2.82842 | 2.82842 | 4 |  |
| 5    | 3.53553 | 3.53553 | 5 |  |
| 6    | 4.24264 | 4.24264 | 6 |  |
| 7    | 4.94974 | 4.94974 | 7 |  |
| 8    | 5.65685 | 5.65685 | 8 |  |
| 9    | 6.36396 | 6.36396 | 9 |  |
| Dep. |         | Lat.    |   |  |
| 45°  |         |         |   |  |

*Chains, Yards, and Feet,*

WITH THEIR RECIPROCAL EQUIVALENTS.

Link = 7.92 inches. Chain = 66 feet = 792 inches.

| CHAINS INTO FEET. |        |       | FEET INTO CHAINS. |        |        |
|-------------------|--------|-------|-------------------|--------|--------|
| Chains.<br>Links. | Yards. | Feet. | Feet.             | Yards. | Links. |
| 0.1               | 0.22   | 0.66  | 0.10              | .033   | 0.15   |
| 0.2               | 0.44   | 1.32  | 0.20              | .066   | 0.30   |
| 0.3               | 0.66   | 1.98  | 0.25              | .082   | 0.38   |
| 0.4               | 0.88   | 2.64  | 0.30              | .101   | 0.45   |
| 0.5               | 1.10   | 3.30  | 0.40              | .133   | 0.60   |
| 0.6               | 1.32   | 3.96  | 0.50              | .166   | 0.76   |
| 0.7               | 1.54   | 4.62  | 0.60              | .200   | 0.91   |
| 0.8               | 1.76   | 5.28  | 0.70              | .233   | 1.06   |
| 0.9               | 1.98   | 5.94  | 0.75              | .250   | 1.13   |
| 0.10              | 2.20   | 6.60  | 0.80              | .266   | 1.21   |

*Chains, Yards, and Feet—Continued.*

| CHAINS INTO FEET. |        |       | FEET INTO CHAINS. |        |        |
|-------------------|--------|-------|-------------------|--------|--------|
| Chains.<br>Links. | Yards. | Feet. | Feet.             | Yards. | Links. |
| 0 . 20            | 4.40   | 13.20 | 0.90              | .300   | 1.36   |
| 0 . 30            | 6.60   | 19.80 | 1.00              | .330   | 1.51   |
| 0 . 40            | 8.80   | 26.40 | 2.0               | .660   | 3.0    |
| 0 . 50            | 11.00  | 33.00 | 3.0               | 1.000  | 4.5    |
| 0 . 60            | 13.20  | 39.60 | 4.0               | 1.330  | 6.0    |
| 0 . 70            | 15.40  | 46.20 | 5.0               | 1.66   | 7.5    |
| 0 . 80            | 17.60  | 52.80 | 6.0               | 2.00   | 9.1    |
| 0 . 90            | 19.80  | 59.40 | 7.0               | 2.33   | 10.6   |
| 1 . 00            | 22.00  | 66.00 | 8.0               | 2.66   | 12.1   |
| 2 . 00            | 44.00  | 132   | 9.0               | 3.00   | 13.6   |
| 3                 | 66.00  | 198   | 10.0              | 3.33   | 15.1   |
| 4                 | 88.00  | 264   | 15.0              | 5.00   | 22.7   |
| 5                 | 110    | 330   | 20                | 6.66   | 30.3   |
| 6                 | 132    | 396   | 24                | 8.00   | 36.3   |
| 7                 | 154    | 462   | 27                | 9.00   | 40.9   |
| 8                 | 176    | 528   | 30                | 10.00  | 45.4   |
| 9                 | 198    | 594   | 33                | 11.00  | 50.0   |
| 10                | 220    | 660   | 36                | 12.00  | 54.5   |
| 20                | 440    | 1320  | 39                | 13.00  | 59.1   |
| 30                | 660    | 1980  | 40                | 13.33  | 60.6   |
| 35                | 770    | 2310  | 42                | 14.00  | 63.3   |
| 40                | 880    | 2640  | 45                | 15.00  | 68.2   |
| 45                | 990    | 2970  | 48                | 16.00  | 72.7   |
| 50                | 1100   | 3300  | 50                | 16.66  | 75.7   |
| 55                | 1210   | 3630  | 51                | 17.00  | 77.3   |
| 60                | 1320   | 3960  | 54                | 18.00  | 81.8   |
| 65                | 1430   | 4290  | 57                | 19.00  | 86.3   |
| 70                | 1540   | 4620  | 60                | 20.00  | 90.9   |
| 75                | 1650   | 4950  | 63                | 21.00  | 95.4   |
| 80                | 1760   | 5280  | 66                | 22.00  | 100    |



*The Army Ration.**Table showing the weight and bulk of 1000 rations.*

| One thousand rations of | Nett weight in pounds. | Gross weight in pounds. | Bulk in barrels. | 100 rations consist of  |
|-------------------------|------------------------|-------------------------|------------------|-------------------------|
| Pork - -                | 750.                   | 1218.75                 | 3.75             | 75 lbs. or }            |
| Bacon - -               | 750.                   | 903.19                  | 4.90             | 75 lbs. }               |
| Flour - -               | 1125.                  | 1234.06                 | 5.74             | 112.5 lbs. or }         |
| Pilot bread -           | 750.                   | 921.69                  | 9.03             | 75 lbs. or }            |
| Do. - - -               | 1000.                  | 1228.91                 | 12.05            | 100 lbs. in the field } |
| Beans - -               | 155.                   | 177.32                  | 0.71             | 8 quarts, or }          |
| Rice - - -              | 100.                   | 114.50                  | 0.46             | 10 lbs. }               |
| Coffee - -              | 60.                    | 70.90                   | 0.35             | 6 lbs.                  |
| Sugar - -               | 120.                   | 135.62                  | 0.50             | 12 lbs.                 |
| Vinegar -               | 92.5                   | 107.50                  | 0.33             | 4 quarts.               |
| Candles -               | 15.                    | 17.50                   | 0.09             | 1½ lb.                  |
| Soap - -                | 40.                    | 46.89                   | 0.19             | 4 lbs.                  |
| Salt - - -              | 33.75                  | 38.63                   | 0.16             | 2 quarts.               |

*Forage.*

14 lbs. hay or fodder } per horse { when pressed 11 lbs. to cub. foot.  
 12 quarts oats, or } per day. { 40 lbs. to bus., 33.14 lbs. cub. foot  
 8 quarts corn } { 55 lbs. to bus., 45.65 lbs. cub. foot

Daily allowance of water for a horse, 4 gallons.

Average mule pack, New Mexico, 175 lbs.

Average load to mule team across the Prairies, 2000 lbs.

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**TABLES AND FORMULÆ.**

**PART II.**

**GEODESY.**

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## GEODESY.

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### I. *Reduction to centre of station.*

Call P the place of the instrument,

C the centre of the station,

O the angle at P, between two objects A and B,

y the angle at P, between C and the *left* hand object B,

r the distance CP,

C the unknown angle at C,

D the distance AC,

G the distance BC,

$$C = O + \frac{r \sin (O + y)}{D \sin 1''} - \frac{r \sin y}{G \sin 1''}$$

In the use of this formula proper attention should be paid to the signs of  $\sin (O + y)$  and  $\sin y$ ; for the first term will be *positive* when  $(O + y)$  is less than  $180^\circ$ , (the reverse with  $\sin y$ ); D being the distance of the *right* hand object, the graduation of the instrument running from left to right.

r being small, the lengths of D and G are computed with the angle O.

### II. *Reduction to centre of signal observed, or correction for phase in tin cones used as signals.*

$$\text{Correction} = \pm \frac{r \cos^2 \frac{1}{2} Z}{D \sin 1''}$$

Where r = radius of the signal

Z = angle at the point of observation between  
the Sun and the signal,

D = the distance.

III. *Spherical Excess.*

$$E = \frac{S}{r^2 \sin 1''} = \frac{a b \sin C}{2 r^2 \sin 1''}$$

$S$ , being the area of the triangle.  $r$  = the radius of the Earth

$$S = \frac{a b \sin c}{2}$$

$$= \sqrt{s(s-a)(s-b)(s-c)}, s \text{ being } = \frac{a+b+c}{2}$$

Between latitudes  $45^\circ$  and  $25^\circ$  the spherical excess amounts to about  $1''$  for an area of 75.5 square miles.

Hence, if the area in square miles be known, a close approximation to the spherical excess will be had by dividing the area by 75.5.

Log. mean radius of the Earth in yards = 6.8427917.

If the three angles of a triangle are assumed to have been equally well determined, the previous determination of the spherical excess is not necessary for the calculation of the sides, though it will be required for estimating the relative accuracy of the observations. For the sides of a spherical triangle may be computed as if they were rectilinear, when  $\frac{1}{3}$  the excess of the sum of the three angles above  $180^\circ$  is deducted from each of the three observed angles;

then side  $b = \text{side } a \sin (B - \frac{1}{3} E) \div \sin (A - \frac{1}{3} E)$ .

IV. *To reduce the length of an inclined base to horizontal measure.*

Let  $B$  be the length of the base on the inclined plane,  
 $b$  that reduced to the horizontal plane,  
 $\theta$  the inclination,

$$b = B \cos \theta$$

But as  $\theta$  is generally a small angle and need not be known with extreme precision, it is better to compute the excess of  $B$  above  $b$ , and supposing  $\theta$  to be given in minutes.

$$B - b = B (1 - \cos \theta) = 2 B \sin^2 \frac{\theta}{2} = \frac{1}{2} B \theta^2 \sin^2 1' = \frac{\sin^2 1'}{2} \theta^2 B,$$

$$\text{or } B - b = 0.00000004231 \theta^2 B$$

or by logarithms,

$$\text{Log } (B - b) = \text{const. log } 2.626422 + 2 \log \theta + \log B$$

V. *To reduce a broken base to a straight line.*

Let  $a$  and  $b$  be the given sides, and  $C$  the contained angle, very nearly  $180^\circ$ .

make  $C = 180^\circ - \theta$ ,  $\theta$  being small, and  $\cos \theta = 1 - \frac{1}{2} \theta^2$

$$\text{then, sine } c = a + b - \frac{\sin^2 1'}{2} \cdot \frac{a b \theta^2}{a + b},$$

$$= a + b - 0.00000004231 \times \frac{a b \theta^2}{a + b}$$

$\theta$  being expressed in minutes.

$$\text{log. } 0.00000004231 = 2.626422$$

VI. To find the length,  $BD = x$ , of a portion of a straight line  $AH$ , knowing the two other portions  $AB = a$ ;  $DH = b$ ; and also the angles  $\alpha, \beta, \gamma$ , from any exterior station  $C$ , between  $B$  and  $A$ ,  $D$  and  $A$ , and  $H$  and  $A$ .

The problem being intended to supply by observation any portion of a base which cannot be directly measured.

$$\tan^2 \phi = \frac{4ab}{(a-b)^2} \frac{\sin \beta \sin (\gamma - \alpha)}{\sin \alpha \sin (\gamma - \beta)}$$

$$x = -\frac{a+b}{2} \pm \frac{a-b}{2 \cos \phi}$$

VII. To reduce a measured base to the level of the sea.

Let  $r$  represent the radius of the Earth (or better, the normal  $N$ ), corresponding to the base  $b$  at the level of the sea, and  $r+a$  the radius referred to the level of the measured base  $B$ ,

$$\text{then } r+a : r :: B : b = B \times \frac{r}{r+a}$$

$$\text{and } B-b = B-B \frac{r}{r+a} = B \times \left( \frac{a}{r} - \frac{a^2}{r^2} + \text{etc.} \right)$$

But the radius of the Earth being very great in comparison to the difference of level  $a$ , we have the correction  $\delta$  sufficiently accurate by retaining only the first term. Hence,

$$\delta = \frac{Ba}{r}$$

VIII. *Correction for temperature in metallic rods.*

Let  $e$  = the linear expansion for  $1^\circ$  of Fahrenheit,  
 $l$  = the length of the rod before expansion,  
 $l'$  = the length of the rod after expansion,  
 $t$  = the number of degrees, Fahrenheit,

$$\text{Total expansion} = e t$$

$$\text{and} \quad l' = l (1 + e t)$$

The following expansions were adopted by Mr. Hassler in his comparisons of weights and measures, (Report of 1832.)

| Expansion for $1^\circ$ Fahr. = $e$ | For $1^\circ$ in a yard's length. |
|-------------------------------------|-----------------------------------|
| Platinum = 0.0000051344 ;           | = 0.0001848384 Eng. In.           |
| Brass Bar = 0.00001050903;          | = 0.00037832508 “                 |
| Iron Bar = 0.000006963535;          | = 0.000250687260 “                |

Other authorities :

| Expansion for $1^\circ$ Fahr. = $e$ | For $1^\circ$ in a yard's length. |
|-------------------------------------|-----------------------------------|
| Brass bar 0.000010480               | 0.0003772800 Eng. In. Bailey.     |
| Brass rod 0.0000105155              | 0.0003785580 “ Roy.               |
| — 106666                            | 0.0003839976 “ Troughton.         |
| Brass wire 107407                   | 0.0003866652 “ Smeaton.           |
| Iron bar 0.0000069907               | 0.0002516652 “ Smeaton.           |
| Steel rod 63596                     | 0.0002289456 “ Roy.               |
| Glass, Barom. tubes 43119           | 0.0001552284 “ Roy.               |
| White Norway pine 22685             | 0.0000816660 “ Kater.             |



### IX. *Measurement of distances by sound.*

The *velocity of Sound*, in one second of time at 32° Fahrenheit in dry air, is about 1090 English feet. For any higher temperature, add 1 foot for every degree of the Thermometer above 32°.

The measurement of distances by sound should always be made, if possible, in calm, *dry* weather. In cases of wind, the velocity per second must be corrected by the quantity,  $f \cos d$ ;  $f$  being the force of the wind in feet per second, and  $d$  the angle which its direction makes with that of the sound.

Or, in general, in dry air,

$$v = 1090 \text{ feet} + (t^\circ - 32^\circ) \pm f \cos d.$$

### *Velocity and force of winds.*

| Velocity in miles per hour. | A wind, when it does not exceed the velocity opposite to it, may be denominated | Velocity per sec <sup>nd</sup> . | Force on a square feet. |
|-----------------------------|---------------------------------------------------------------------------------|----------------------------------|-------------------------|
|                             |                                                                                 | feet.                            | lbs.                    |
| 6.8                         | a gentle, pleasant wind.....                                                    | 10                               | 0.129                   |
| 13.6                        | a brisk gale.....                                                               | 20                               | 0.915                   |
| 19.5                        | a very brisk gale.....                                                          | 30                               | 2.059                   |
| 34.1                        | a high wind.....                                                                | 50                               | 5.718                   |
| 47.7                        | a very high wind.....                                                           | 70                               | 11.207                  |
| 54.5                        | a storm or tempest.....                                                         | 80                               | 14.638                  |
| 68.2                        | a great storm .....                                                             | 100                              | 22.872                  |
| 81.8                        | a hurricane .....                                                               | 120                              | 32.926                  |
| 102.3                       | a violent hurricane, that tears up trees, etc.                                  | 150                              | 51.426                  |

### X. *For Reconnoissances.*

#### *“Three point problem.”*

At a point P, from whence are to be seen three points A, C, B, forming a triangle, the elements (i. e. the angles and sides) of which are known, measure the angles A P C, and C P B; then, required to determine the direction and distance of the point P from each object.

Make A C =  $a$ ; B C =  $b$ ; B C A =  $C$ ; A P C =  $P$ , and C P B =  $P'$ ; also, make  $R = 360^\circ - P - P' - C$ ;  $x = C A P$ ;  $y = P B C$ .

Then will

$$\text{Cot } x = \text{cot } R \left( \frac{a \sin P'}{b \sin P \cos R} + 1 \right)$$

$$y = R - x$$

The use of these formulæ need not be embarrassing if care is taken in properly applying the sign of cos. and cot. R. When R is less than  $90^\circ$  both cos. and cot. are plus; between  $90$  and  $180^\circ$  both are minus; between  $180^\circ$  and  $270^\circ$  the cos. is minus and the cot. plus; between  $270$  and  $360^\circ$ , cos. is plus and the cot. minus.

This problem is indeterminate when P falls upon the circumference of the circle passing through A, B, C. A case of this nature is of rare occurrence, however, in practice.

**XI.** *For computing the principal Geodetic quantities depending on the spheroidal figure of the earth, at any given latitude.*

Eccentricity of the Earth =  $e =$

$$= \left( \frac{a^2 - b^2}{a^2} \right)^{\frac{1}{2}} = \left( 1 - \frac{b^2}{a^2} \right)^{\frac{1}{2}} = 2 E - E^2$$

$$\text{Ellipticity} = E = \frac{a - b}{a} = 1 - \frac{b}{a}$$

$$\text{or, very nearly } e^2 = 2 E; \quad E = \frac{e^2}{2}$$

Normal ending at minor axis (or radius of curvature of a section perpendicular to the meridian)

$$= N = \frac{a}{(1 - e^2 \sin^2 L)^{\frac{1}{2}}}$$

Normal ending at major axis =  $N' = N (1 - e^2)$

$$= \frac{a (1 - e^2)}{(1 - e^2 \sin^2 L)^{\frac{1}{2}}}$$

Tangent ending at minor axis =  $t = N \cot L$

Tangent ending at major axis =  $T = N \tan L (1 - e^2)$

Radius of the parallel =  $\rho = N \cos L$

Radius of curvature of the merid. =  $R = \frac{N^3}{a^2} (1 - e^2)$

$$= \frac{a (1 - e^2)}{(1 - e^2 \sin^2 L)^{\frac{3}{2}}}$$

Radius of curvature of a section making an angle  $Z$  with

$$\text{the meridian,} = R^Z = \frac{N R}{N^2 \cos^2 Z + R^2 \sin^2 Z}$$

Radius of the earth =  $r = a \left( 1 - \frac{e^2 (1 - e^2) \sin^2 L}{1 - e^2 \sin^2 L} \right)^{\frac{1}{2}}$

$a$  = Equatorial Radius,

$b$  = Polar Radius,

$L$  = the given Latitude.

XII. *Numerical values of some of the preceding quantities, from a discussion by BESSEL in the "Astronomische Nachrichten, No. 438."*

$a = \text{Eq. Rad.} = 3272077.14 \text{ toises; } \log = 6.5148235337$

$b = \text{Polar Rad.} = 3261139.33 \text{ toises; } \log = 6.5133693539$

Ratio of the Toise to the Metre—law of France, Dec. 10, 1799.

$$T = 1.9490363^M \quad \text{Log} = 0.2898199300$$

whence in metres

$$a = 6377397.15^M; \quad \text{Log} = 6.8046434637$$

$$b = 6356078.96^M; \quad \text{Log} = 6.8031892839$$

Ratio of the axes,  $a : b :: 299.1528 : 298.1528$ ;

mean uncertainty  $\pm 4.667$  units.

Length of the Earth's quad.  $= 5131179.81^T = 10000855.76^M$ ;

mean uncertainty  $= \pm 498.23$  metres.

$$e = \text{Eccentricity} = \left(1 - \frac{b^2}{a^2}\right)^{\frac{1}{2}} = 0.0816967;$$

$$\text{Log} = 8.9122052271$$

$$E = \text{Ellipticity} = \frac{1}{2} e^2 \quad \text{Log} = 7.5233789824$$

Length, in toises, of a meridional degree whose middle latitude is  $\phi$ .

$$Dm = 57013.109^T - 286.337^T \cos 2\phi + 0.611^T \cos 4\phi \left. \vphantom{Dm} \right\} \\ + 0.001^T \cos 6\phi \left. \vphantom{Dm} \right\}$$

Length of a degree of the parallel, in toises,

$$Dp = 57156.285 \cos \phi - 47.825 \cos 3\phi + 0.060 \cos 5\phi$$

or making  $\sin \psi = e \sin \phi$

$$\text{Log } Dp = 4.7567009.0 + \log \cos \phi - \log \cos \psi$$

### XIII. *Ratio of the Metre to the English Yard.*

The value of the French metre in English imperial inches, in general use in this country and in Europe, is that derived from Kater's Experiments in 1818, viz: 39.37079 inches of Sir G. Shuckburg's scale at 62° Faht., the metre being at 32° Faht.

From the more recent and accurate comparisons of Mr. Baily in 1835, when engaged in constructing a new standard scale for the Royal Astronomical Society (Mem. R. A. S., vol. ix); 39.369678 inches is the value of the standard metre, in mean inches of the centre yard of the Astronomical Society's scale, each being reduced to its standard temperature, namely, the platina metre to 32° and the brass scale to 62° of Fahrenheit's Thermometer. This very change of temperature, however, involves the result in some degree of uncertainty.

The centre yard of the Astronomical Society's scale exceeds the imperial standard yard by 0.000377 inches.

Whence, according to these experiments 39.370092 inches is the value of the standard metre in imperial standard inches, both being at their respective standard temperatures.

The value of the metre, as reported to Congress by Mr. Hassler in his report on Weights and Measures in 1832, is 39.38091714 inches of the English imperial standard at 32° Fht., the comparisons having been made at that temperature upon an 82 inches scale by Troughton, said to be *identical* with the English standard; or, correcting for expansion = 39.36850154 imperial standard inches at 62° Fht., a value materially smaller than the two preceding. According to Baily this discordance has probably

arisen from inaccuracy in the length of the copy of Troughton's scale employed by Mr. Hassler.

This 82 inches scale is the standard of the United States, but in the absence of a direct comparison between it and the English standard, and not to add to a confusion already too great, it is as well to adhere for the present to the old value of Kater, as being that which is still most in use. To recapitulate :

1 metre = 39.3707900 English imperial inches, according to Kater, (1818,) Log = 1.5951741293  
 = 39.3700920 English imperial inches, according to Baily, (1835,) Log = 1.5951664297  
 = 39.36850154, American std'd inches, according to Hassler, (1832,) being the ratio, for the present, in use upon the Survey of the Coast, - - - - Log = 1.5951489169

The metre being at 32°, and the inches at 62° Fht.

*XIV. Numerical values of Bessel's terrestrial elements in English yards, adopting Kater's value of the metre,*

viz: 39.37079 English inches; Log 1.5951741293

Log to reduce toises to yards = 0.3286915586

Log to reduce metres to yards = 0.0388716286

Log . 3 = 0.4771212547

Log . 12 = 1.0791812460

Log 5280 = 3.7226339225

$a$  = Equat. Rad. = 6 974 532.339; Log = 6.8435150923

$b$  = Polar Rad. = 6 951 218.059; Log = 6.8420609125

Length, in yards, of a Meridional degree, whose middle latitude is  $\phi$ .

$$Dm = 121525.183 - 610.336 \cos 2\phi + 1.302 \cos 4\phi + 0.002 \cos 6\phi$$

Length, in yards, of a degree of the parallel.

$$Dp = 121830.366 \cos \phi - 101.941 \cos 3\phi + 0.128 \cos 5\phi$$

or, making  $\sin \psi = e \sin \phi$

$$\text{Log } Dp = 5.0853925 + \log \cos \phi - \log \cos \psi$$

or, using the logarithms of the numerical co-efficients,

$$Dm = 121525.183 - (2.7855691) \cos 2\phi + (0.1147) \cos 4\phi + (7.3287) \cos 6\phi$$

$$Dp = (5.0857556) \cos \phi - (2.00835) \cos 3\phi + (9.1069) \cos 5\phi$$

$$\text{or, } Dp = \frac{(5.0853925) \cos \phi}{\cos \psi}$$

### XV. Constant Logarithms.

$$e^2 = 0.00667435 \quad \text{Log} = 7.8244104542$$

$$\frac{1}{2} e^2 = E = \text{Ellipticity} = \frac{1}{299.66} = 7.5233789824$$

$$\sin 1'' = 4.6855748668$$

$$\frac{1}{2} \sin 1'' = 4.3845448711$$

$$\frac{3e^2}{2} \sin 1'' = 2.6860751039$$

$$(1 - e^2) = 0.99332565 = 9.9970916404$$

$$a(1 - e^2) = 6.8406067325$$

$$a \sin 1'' = 1.5290899591$$

$$a \sin 1'' (\text{arith. comp.}) = 8.4709100409$$

**XVI.** *For computing the Geodetic Latitudes, Longitudes, and Azimuths of points of a Triangulation.*

**1.** In terms of the sides of the Triangles.\*

$$w'' = \frac{K}{N \sin 1''} = \frac{K (1 - e^2 \sin^2 L)_\frac{1}{2}}{a \sin 1''}$$

$$\left. \begin{aligned} L' &= L - (1 + e^2 \cos^2 L) w'' \cos Z \\ &- (1 + e^2 \cos^2 L) (w'' \sin Z)^2 \tan L \times \frac{1}{2} \sin 1'' \end{aligned} \right\}$$

$$M' = M + \frac{w'' \sin Z}{\cos L'}$$

$$Z' = 180^\circ + Z - \frac{w'' \sin Z}{\cos L'} \sin \frac{1}{2} (L + L') \text{ or}$$

$$Z' = 180^\circ + Z - (w'' \sin Z \tan L + w''^2 \sin Z \cos Z \frac{1}{2} \sin 1'')$$

**2.** In terms of the co-ordinates of rectangular axes referred to one of the points of the triangulation, the latitude and longitude of which are known;  $y$  being the ordinate in the direction of the meridian, and  $x$  the ordinate perpendicular to it.

\*This is an abridgement of the following formulæ of Puissant, page 335, vol. 1, 3d edit.

$$\left. \begin{aligned} L' - L &= - \frac{K \cos Z}{N \sin 1''} \cdot \frac{N}{R} - \frac{1}{2} \frac{K^2 \sin^2 Z}{N^2 \sin 1''} \tan L \cdot \frac{N}{R} \\ &+ \frac{1}{6} \frac{K^3 \sin^2 Z \cos Z}{N^3 \sin 1''} (1 + 3 \tan^2 L) \cdot \frac{N}{R} \end{aligned} \right\}$$

$$\text{And } \frac{N}{R} = 1 + e^2 \cos^2 L + e^4 \cos^4 L + \frac{2}{3} e^2 \frac{K}{N} \cos Z \sin L \cos L$$



$$L' = L \pm \frac{y}{R \sin 1''} - \frac{1}{2} \sin 1'' \left( \frac{x}{N \sin 1''} \right)^2 \times \left\{ \begin{array}{l} \\ \text{tang} \left( L \pm \frac{y}{R \sin 1''} \right) \end{array} \right\}$$

$$M' = M \pm \left( \frac{x}{N \sin 1''} \right) \times \frac{1}{\cos L'}$$

$$Z' = 270^\circ \pm \frac{x}{N \sin 1''} \text{ tang } L'$$

$K$  = distance in yards between two stations, the latitude and longitude of one of which is known, and  $w''$  this same distance converted to seconds of arc.

$L$  = latitude of 1st station.

$M$  = longitude of 1st station, + if west.

$Z$  = azimuth of 2d station at 1st, counted from the south round by the west, from  $0^\circ$  to  $360^\circ$ .

The algebraic signs of the sine and cosine of this angle must be carefully attended to.

$L'$ ,  $M'$ ,  $Z'$ , the same things at 2d station, or quantities required.

$a$  = the equatorial radius ;  $e$  = the eccentricity.

$R$  = the radius of curvature of the meridian.

$N$  = the radius of curvature of a section perpendicular to the meridian.

The quantity  $\frac{w'' \sin Z}{\cos L'} \sin \frac{1}{2} (L + L')$ ,

or  $(M' - M) \sin \frac{1}{2} (L + L')$ , by which the azimuth at one end of a line exceeds the azimuth at the other, is called *the convergence of the meridians*.

**XVII.** *To compute the length and direction of a line joining two points, the latitudes and longitudes of which are known, or measurement of a base by astronomical observations.*

$$\frac{\beta}{2} = \frac{e^2 (L - L') \cos^2 \frac{1}{2} (L + L')}{2}$$

$$N = \frac{a}{\sqrt{1 - e^2 \sin^2 \frac{1}{2} (L + L')}}^{\frac{1}{2}}$$

$$l = L - \frac{\beta}{2} \qquad x'' = (M' - M) \cos l'$$

$$l' = L' + \frac{\beta}{2} \qquad y'' = (l - l') - \frac{1}{2} \sin 1'' x''^{\frac{2}{3}} \tan l$$

$$\tan Z = \frac{x''}{y''} \qquad x = x'' N \sin 1''$$

$$u'' = \frac{x''}{\sin Z} = \frac{y''}{\cos Z} \qquad y = y'' N \sin 1''$$

$$K = u'' N \sin 1''$$

In which  $L, L', M, M'$ , represent the latitudes and longitudes of the two points.

$u''$  = the distance between these points in seconds of arc.

$K$  = the distance between these points in linear units.

$x''$  = the number of seconds in the arc passing through the point of which  $L'$  is the latitude, and perpendicular to the meridian of the point of which  $L$  is the latitude.

$y''$  = the seconds in the portion of this meridian between  $L$  and the foot of this perpendicular.

$x, y$  = the same quantities in linear units.

$Z$  = the azimuth of the second point  $L'$ , from the first  $L$ .

$N$  = the normal at the middle latitude.

Particular attention must be paid to the sign ( $L - L'$ ) for upon this depends the sign of  $\frac{\beta}{2}$ , and also to that of ( $l - l'$ ) in the value of  $y''$ , so as to know whether the small quantity ( $-\frac{1}{2} \sin 1'' x'' \tan l$ ) is to be added to or subtracted from ( $l - l'$ ).

The azimuth  $Z$  is counted from the south round by the west, from  $0^\circ$  to  $360^\circ$ .

The azimuth  $Z'$ , (if required,) is to be computed from  $Z$ , as on page 65.

**XVIII.** *To compute the distance between two points, knowing their latitudes and the azimuth of one from the other.*

$$\frac{\beta}{2} = \frac{e^2 (L - L') \cos^2 \frac{1}{2} (L + L')}{2}$$

$$N = \frac{a}{\sqrt{1 - e^2 \sin^2 \frac{1}{2} (L + L')}}^{\frac{1}{2}}$$

$$l = L - \frac{\beta}{2} \quad \tan \phi = \frac{\tan l}{\cos Z}$$

$$l' = L' + \frac{\beta}{2} \quad \sin (\phi - u'') = \frac{\sin l'}{\sin l} \sin \phi$$

$$K = u'' N \sin 1''$$

See the note to the preceding formulæ. The algebraic sign of the azimuth  $Z$  will determine the sign of  $\phi$ , and consequently whether the quantity  $u''$  is to be added to or subtracted from  $\phi$ .

XIX. *To compute the distance between two points, knowing the latitude of one, the azimuth from this to the other, and the difference of their longitudes.*

$$\tan \phi = \sin L \tan Z \quad \tan L' = \frac{\tan L \sin (\phi - m)}{\sin \phi}$$

$$\beta = e^2 (L - L') \cos^2 \frac{1}{2} (L + L'); \quad L' = L' - \beta$$

$$l = L - \frac{\beta}{2} \quad l' = L' + \frac{\beta}{2}$$

$$w'' = \frac{m \cos l'}{\sin Z} \quad K = w'' N \sin 1''$$

$m$  = the difference of longitude. The azimuth  $Z$  is, as before, counted from the south round by the west; its algebraic sign will determine the sign of  $\phi$ , and consequently whether it is to be increased or diminished by  $m$ .

The formulæ on page 67 can be presented in a different form, thus :

From the formulæ on page 65,

$$(M' - M) \cos L' = w' \sin Z$$

and,

$$w'' \cos Z = \frac{(L - L') - \frac{1}{2} w'^2 \sin^2 Z \cos^2 L' \tan L \sin 1'' (1 + e^2 \cos^2 L)}{1 + e^2 \cos^2 L}$$

Substituting, in this last, the value of  $w' \sin Z$ , and dividing one by the other;

$$\tan Z = \frac{(M' - M) \cos L' (1 + e^2 \cos^2 L)}{(L - L') - \frac{1}{2} (M' - M)^2 \cos^2 L' \tan L \sin 1'' (1 + e^2 \cos^2 L)}$$

Then knowing  $Z$ ;

$$w'' = \frac{(M' - M) \cos L'}{\sin Z}$$

and,

$$K = w'' N \sin 1''$$

$N$ , being the normal for the mean latitude.

## XX. Forms for record

## Survey of

| No. of Tri-<br>angle. | Position.        | Names of<br>Stations. | No. of Obs. | Observed<br>Angles. | Errors and<br>their dis-<br>tribution. | Spherical<br>Angles. | Spherical<br>Excess. | Final plane<br>Angles. |
|-----------------------|------------------|-----------------------|-------------|---------------------|----------------------------------------|----------------------|----------------------|------------------------|
|                       |                  |                       |             | O' / "              | "                                      | "                    | "                    | O' / "                 |
|                       | Sought           | Cedar Point           | 18          | 66 34 04.80         | -0.36                                  | 04.44                | 1.58                 | 66 34 02.86            |
| XIII                  | Right.           | Buck Hill             | 18          | 64 08 37.78         | -0.36                                  | 37.42                | 1.58                 | 64 08 35.84            |
|                       | (Known<br>Side.) |                       |             |                     |                                        |                      |                      |                        |
|                       | Left.            | Fort Flats            | 18          | 49 17 23.24         | -0.36                                  | 22.88                | 1.58                 | 47 17 21.30            |
|                       |                  |                       |             |                     |                                        |                      |                      | 180 00 00.00           |

## Example of

## Survey of

| NAMES OF<br>STATIONS. | LATITUDES.                                                                                                           |                                         |
|-----------------------|----------------------------------------------------------------------------------------------------------------------|-----------------------------------------|
|                       | $L' = L - u'' \cdot (1 + e^2 \cos^2 L) \cos Z$ $- \frac{1}{2} \sin. 1'' \sin. Z u''^2 (1 + e^2 \cos^2 L) \tan g. L.$ |                                         |
| <b>Fort Flats</b>     | Latitude $L = 45^\circ 39' 13''.89$                                                                                  |                                         |
|                       | Log. K (yards) = 4.7295212                                                                                           | $\frac{1}{2} \sin. 1'' = 4.38454$       |
|                       | Log. $\frac{1}{N \sin. 1''} = 8.4701676$                                                                             | 2 Log. Sin. Z = 9.09522                 |
|                       | Log. $u'' = 3.1996888$                                                                                               | 2 Log. $u'' = 6.39936$                  |
|                       | Log. $(1 + e^2 \cos^2 L) = 0.0014140$                                                                                | ..... = 0.00141                         |
|                       | Log. Cos. Z (-) = 9.9711240                                                                                          | Log. tang. L = 0.00991                  |
|                       | Log. 1st term = 3.1722268                                                                                            | Log. 2d term = 9.89034                  |
|                       | 1st term (+) = +1486''.71                                                                                            | 2d term = 0''.77                        |
|                       | 2d term (-) = - 0.77                                                                                                 |                                         |
|                       | $\frac{1}{2} L = 0^\circ 24' 45''.94$                                                                                |                                         |
|                       | $L = 45^\circ 39' 13.89$                                                                                             | $L + L' = 91^\circ 43' 13''.72$         |
|                       |                                                                                                                      | $\frac{L + L'}{2} = 45^\circ 51' 36.86$ |
| <b>Cedar Point</b>    | Latitude $L' = 46^\circ 03' 59''.83$                                                                                 |                                         |

and computation.

Calculations of Triangles of the first order.

| Computing Letter. | Logarithms of their Sines. | Calculation of the Sides.                                                                      | Sides in Yards. | Designation.                 |
|-------------------|----------------------------|------------------------------------------------------------------------------------------------|-----------------|------------------------------|
| S                 | 9.9626198                  | Log. RL = 4.7379524<br>Comp. Log. Sin. S = 0.0373802<br>Log. Sin. R = 9.9541886                | = 54695.61      | { Buck Hill—<br>Fort Flat.   |
| R                 | 9.9541886                  | Log. LS = 4.7295212<br>Log. RL +<br>Comp. Log. Sin. S } = 4.7753326<br>Log. Sin. L = 9.8796760 | = 53644.00      | { Fort Flat—<br>Cedar Point. |
| L                 | 9.8796760                  | Log. RS = 4.6550086                                                                            | = 45186.49      | { Buck Hill—<br>Cedar Point. |

Method 1, (page 65.)

Geodetic Determination of Positions.

(Secondary.)

| LONGITUDES                              |  | AZIMUTHS                                                 |  | REMARKS. |
|-----------------------------------------|--|----------------------------------------------------------|--|----------|
| $M' = M + \frac{u'' \sin. Z}{\cos. L'}$ |  | $Z' = 180^\circ + Z - (\delta M) \sin. \frac{L + L'}{2}$ |  |          |
| Lon. M = 84° 42' 22".19                 |  | Azim. Z = 159° 20' 13".62                                |  |          |
| Log. Sin. Z = (+) 9.5476117             |  | 180°                                                     |  |          |
| Log u'' = 3.1996888                     |  | 180° + Z = 339 20 13.62                                  |  |          |
|                                         |  | 20 39 46.38                                              |  |          |
| Log. Cos. L' = 9.8412474                |  | Log. Sin. $\frac{L + L'}{2} = 9.8559089$                 |  |          |
| Log. $\delta M = 2.9060529$             |  | ..... (+) = 2.9060529                                    |  |          |
|                                         |  | Log. $\delta Z = 2.7619618$                              |  |          |
|                                         |  | — 578".05                                                |  |          |
| $\delta M = 0^\circ 13' 25''.48$        |  | $\delta Z = 0^\circ 09' 38''.05$                         |  |          |
| M = 84 42 22.19                         |  | 180° + Z = 339 20 13.62                                  |  |          |
| Lon. M' = 84° 55' 47".67                |  | Azim. Z' = 339° 10' 35".57                               |  |          |

Ellipticity =  $\frac{1}{300}$ , Equat. Rad. = 6974532 yds. Log = 6.8435151

| Latitude. | Normal or Radius of Curvature of the perpendicular to the Meridian. |                        | Log. (1 + e <sup>2</sup> cos <sup>2</sup> L) |                 |
|-----------|---------------------------------------------------------------------|------------------------|----------------------------------------------|-----------------|
|           | $N = \frac{a}{(1 - e^2 \sin^2 L)^{\frac{3}{2}}}$                    |                        |                                              |                 |
|           | Log. N.                                                             | Com. differ'ce for 10' | Log. $\frac{1}{N \sin 1''}$                  | Differ. for 10' |
| 0         |                                                                     |                        |                                              |                 |
| 20 0      | 6.8436847                                                           | 27.3                   | 8.4707404                                    | 0.0025521       |
| 15        | 6868                                                                | 27.6                   | 7363                                         | 5439            |
| 30        | 6929                                                                | 27.8                   | 7322                                         | 5356            |
| 45        | 6971                                                                | 28.1                   | 7280                                         | 5274            |
| 21 0      | 7013                                                                | 28.4                   | 7238                                         | 5191            |
| 15        | 7056                                                                | 28.7                   | 7196                                         | 5106            |
| 30        | 7099                                                                | 29.0                   | 7153                                         | 5021            |
| 45        | 7142                                                                | 29.3                   | 7109                                         | 4934            |
| 22 0      | 7186                                                                | 29.5                   | 7066                                         | 4847            |
| 15        | 7230                                                                | 29.7                   | 7021                                         | 4760            |
| 30        | 7274                                                                | 29.9                   | 6977                                         | 4671            |
| 45        | 7319                                                                | 30.2                   | 6932                                         | 4582            |
| 23 0      | 7365                                                                | 30.5                   | 6887                                         | 4492            |
| 15        | 7410                                                                | 30.7                   | 6841                                         | 4401            |
| 30        | 7457                                                                | 31.0                   | 6795                                         | 4309            |
| 45        | 7503                                                                | 31.2                   | 6748                                         | 4217            |
| 24 0      | 7550                                                                | 31.5                   | 6701                                         | 4124            |
| 15        | 7597                                                                | 31.7                   | 6654                                         | 4030            |
| 30        | 7645                                                                | 32.0                   | 6607                                         | 3935            |
| 45        | 7693                                                                | 32.2                   | 6559                                         | 3840            |
| 25 0      | 7741                                                                | 32.5                   | 6510                                         | 3744            |
| 15        | 7790                                                                | 32.7                   | 6462                                         | 3648            |
| 30        | 7839                                                                | 32.9                   | 6413                                         | 3550            |
| 45        | 7888                                                                | 33.2                   | 6363                                         | 3452            |
| 26 0      | 7938                                                                | 33.4                   | 6313                                         | 3353            |
| 15        | 7988                                                                | 33.6                   | 6263                                         | 3254            |
| 30        | 8038                                                                | 33.8                   | 6213                                         | 3154            |
| 45        | 8089                                                                | 34.0                   | 6162                                         | 3053            |
| 27 0      | 8140                                                                | 34.3                   | 6111                                         | 2951            |
| 15        | 8192                                                                | 34.5                   | 6060                                         | 2849            |
| 30        | 8243                                                                | 34.7                   | 6008                                         | 2746            |
| 45        | 8295                                                                | 34.9                   | 5956                                         | 2643            |
| 28 0      | 8348                                                                | 35.1                   | 5904                                         | 2539            |
| 15        | 8400                                                                | 35.3                   | 5851                                         | 2434            |
| 30        | 8453                                                                | 35.5                   | 5798                                         | 2329            |
| 45        | 6.8438507                                                           | 35.7                   | 8.4705745                                    | 0.0022223       |
|           |                                                                     |                        |                                              | 71              |

| Latitude. | Log N.    | Com.<br>differ.<br>for 10' | Log $\frac{1}{N \sin 1''}$ | Log $(1 + e^2 \cos^2 L)$ | Differ.<br>for 10' |
|-----------|-----------|----------------------------|----------------------------|--------------------------|--------------------|
| 29 0      | 6.8438560 | 35.9                       | 8.4705691                  | 0.0022117                |                    |
| 15        | 8614      | 36.1                       | 5637                       | 2010                     | 71                 |
| 30        | 8668      | 36.3                       | 5583                       | 1902                     | 72                 |
| 45        | 8723      | 36.5                       | 5529                       | 1794                     | 72                 |
| 30 0      | 8777      | 36.7                       | 5474                       | 1686                     | 73                 |
| 15        | 8832      | 36.9                       | 5419                       | 1576                     | 73                 |
| 30        | 8888      | 37.1                       | 5364                       | 1466                     | 73                 |
| 45        | 8943      | 37.2                       | 5308                       | 1356                     | 74                 |
| 31 0      | 8999      | 37.4                       | 5252                       | 1245                     | 74                 |
| 15        | 9055      | 37.6                       | 5196                       | 1134                     | 75                 |
| 30        | 9111      | 37.7                       | 5140                       | 1022                     | 75                 |
| 45        | 9168      | 37.9                       | 5084                       | 0910                     | 75                 |
| 32 0      | 9225      | 38.1                       | 5027                       | 0797                     | 75                 |
| 15        | 9282      | 38.2                       | 4970                       | 0684                     | 76                 |
| 30        | 9339      | 38.4                       | 4912                       | 0570                     | 77                 |
| 45        | 9397      | 38.5                       | 4855                       | 0455                     | 77                 |
| 33 0      | 9454      | 38.7                       | 4797                       | 0340                     | 77                 |
| 15        | 9512      | 38.9                       | 4737                       | 0225                     | 77                 |
| 30        | 9571      | 39.0                       | 4681                       | .0020109                 | 77                 |
| 45        | 9629      | 39.1                       | 4622                       | .0019993                 | 77                 |
| 34 0      | 9688      | 39.2                       | 4564                       | 9877                     | 78                 |
| 15        | 9747      | 39.4                       | 4505                       | 9760                     | 78                 |
| 30        | 9806      | 39.5                       | 4446                       | 9643                     | 79                 |
| 45        | 9865      | 39.7                       | 4387                       | 9525                     | 79                 |
| 35 0      | 9924      | 39.8                       | 4327                       | 9407                     | 80                 |
| 15        | .8439984  | 40.0                       | 4267                       | 9288                     | 80                 |
| 30        | .8440044  | 40.0                       | 4208                       | 9169                     | 80                 |
| 45        | 0104      | 40.1                       | 4148                       | 9050                     | 80                 |
| 36 0      | 0164      | 40.3                       | 4087                       | 8931                     | 80                 |
| 15        | 0224      | 40.3                       | 4027                       | 8811                     | 81                 |
| 30        | 0285      | 40.5                       | 3966                       | 8690                     | 80                 |
| 45        | 0346      | 40.6                       | 3906                       | 8570                     | 81                 |
| 37 0      | 0406      | 40.7                       | 3845                       | 8449                     | 81                 |
| 15        | 0467      | 40.7                       | 3784                       | 8328                     | 81                 |
| 30        | 0529      | 40.9                       | 3723                       | 8206                     | 81                 |
| 45        | 0590      | 41.0                       | 3661                       | 8084                     | 81                 |
| 38 0      | 0651      | 41.1                       | 3600                       | 7963                     | 82                 |
| 15        | 0713      | 41.1                       | 3538                       | 7840                     | 82                 |
| 30        | 0775      | 41.2                       | 3477                       | 7717                     | 82                 |
| 45        | 0837      | 41.4                       | 3415                       | 7594                     | 82                 |
| 39 0      | 0898      | 41.4                       | 3353                       | 7471                     | 82                 |
| 15        | 0961      | 41.4                       | 3291                       | 7348                     | 83                 |
| 30        | 1023      | 41.5                       | 3229                       | 7224                     | 82                 |
| 45        | 6.8441085 | 41.6                       | 8.4703166                  | 0.0017101                | 83                 |



| Latitude. | Log N.    | Com.<br>diff.<br>for 10' | Log $\frac{1}{N \sin 1''}$ | Log<br>( $1 + e^2 \cos^2 L$ ) | Differ.<br>for 10' |
|-----------|-----------|--------------------------|----------------------------|-------------------------------|--------------------|
| ° /       |           |                          |                            |                               |                    |
| 40 0      | 6.8441147 |                          | 8.4703104                  | 0.0016977                     |                    |
| 15        | 1210      | 41.7                     | 3041                       | 6853                          | 83                 |
| 30        | 1273      | 41.8                     | 2979                       | 6728                          | 84                 |
| 45        | 1335      | 41.8                     | 2916                       | 6604                          | 83                 |
|           |           | 41.9                     |                            |                               | 84                 |
| 41 0      | 1398      |                          | 2853                       | 6479                          |                    |
| 15        | 1461      | 41.9                     | 2791                       | 6354                          | 84                 |
| 30        | 1524      | 41.9                     | 2728                       | 6229                          | 84                 |
| 45        | 1587      | 42.0                     | 2665                       | 6104                          | 84                 |
|           |           | 42.1                     |                            |                               | 84                 |
| 42 0      | 1650      |                          | 2602                       | 5979                          |                    |
| 15        | 1713      | 42.1                     | 2539                       | 5853                          | 84                 |
| 30        | 1776      | 42.1                     | 2475                       | 5728                          | 84                 |
| 45        | 1839      | 42.2                     | 2412                       | 5602                          | 84                 |
|           |           | 42.1                     |                            |                               | 84                 |
| 43 0      | 1903      |                          | 2349                       | 5477                          |                    |
| 15        | 1967      | 42.2                     | 2286                       | 5351                          | 84                 |
| 30        | 2029      | 42.2                     | 2222                       | 5225                          | 84                 |
| 45        | 2093      | 42.3                     | 2159                       | 5099                          | 84                 |
|           |           | 42.3                     |                            |                               | 84                 |
| 44 0      | 2156      |                          | 2095                       | 4973                          |                    |
| 15        | 2219      | 42.3                     | 2032                       | 4847                          | 84                 |
| 30        | 2283      | 42.3                     | 1969                       | 4721                          | 84                 |
| 45        | 2346      | 42.3                     | 1905                       | 4595                          | 84                 |
|           |           | 42.3                     |                            |                               | 84                 |
| 45 0      | 2410      |                          | 1842                       | 4469                          |                    |
| 15        | 2473      | 42.3                     | 1778                       | 4343                          | 84                 |
| 30        | 2537      | 42.3                     | 1715                       | 4217                          | 84                 |
| 45        | 2600      | 42.3                     | 1651                       | 4091                          | 84                 |
|           |           | 42.3                     |                            |                               | 84                 |
| 46 0      | 2663      |                          | 1588                       | 3965                          |                    |
| 15        | 2727      | 42.3                     | 1525                       | 3839                          | 84                 |
| 30        | 2790      | 42.3                     | 1461                       | 3713                          | 84                 |
| 45        | 2854      | 42.3                     | 1398                       | 3587                          | 84                 |
|           |           | 42.2                     |                            |                               | 84                 |
| 47 0      | 2917      |                          | 1334                       | 3461                          |                    |
| 15        | 2980      | 42.2                     | 1271                       | 3336                          | 84                 |
| 30        | 3043      | 42.1                     | 1208                       | 3210                          | 84                 |
| 45        | 3107      | 42.1                     | 1145                       | 3084                          | 84                 |
|           |           | 42.1                     |                            |                               | 84                 |
| 48 0      | 3170      |                          | 1082                       | 2959                          |                    |
| 15        | 3233      | 42.1                     | 1018                       | 2833                          | 84                 |
| 30        | 3296      | 42.0                     | 0955                       | 2708                          | 84                 |
| 45        | 3359      | 42.0                     | 0892                       | 2583                          | 84                 |
|           |           | 41.9                     |                            |                               | 84                 |
| 49 0      | 3422      |                          | 0830                       | 2458                          |                    |
| 15        | 3485      | 41.9                     | 0767                       | 2333                          | 84                 |
| 30        | 3547      | 41.9                     | 0704                       | 2209                          | 83                 |
| 45        | 3610      | 41.8                     | 0641                       | 2084                          | 84                 |
|           |           | 41.8                     |                            |                               | 83                 |
| 50 0      | 6.8443673 |                          | 8.4700579                  | 0.0011960                     |                    |

Ellipticity =  $\frac{1}{300}$ , Equatorial Radius = 6974532 Yards.

| Latitude. |    | Radius of curvature of Meridian.                      |                             |                            |
|-----------|----|-------------------------------------------------------|-----------------------------|----------------------------|
|           |    | $R = \frac{a(1-e^2)}{(1-e^2 \sin^2 L)^{\frac{3}{2}}}$ |                             |                            |
|           |    | Log R                                                 | Com.<br>differ.<br>for 10'. | Log $\frac{1}{R \sin 1''}$ |
| 20        | 0  | 6.8411155                                             |                             | 8.4733096                  |
|           | 15 | 1278                                                  | 81.9                        | 2973                       |
|           | 30 | 1402                                                  | 82.7                        | 2849                       |
|           | 45 | 1527                                                  | 83.5                        | 2724                       |
|           |    |                                                       | 84.3                        |                            |
| 21        | 0  | 1654                                                  | 85.1                        | 2598                       |
|           | 15 | 1781                                                  | 86.0                        | 2470                       |
|           | 30 | 1910                                                  | 86.8                        | 2341                       |
|           | 45 | 2040                                                  | 87.5                        | 2211                       |
| 22        | 0  | 2172                                                  | 88.4                        | 2080                       |
|           | 15 | 2304                                                  | 89.1                        | 1947                       |
|           | 30 | 2438                                                  | 90.0                        | 1813                       |
|           | 45 | 2573                                                  | 91.0                        | 1679                       |
| 23        | 0  | 2709                                                  | 91.5                        | 1543                       |
|           | 15 | 2846                                                  | 92.3                        | 1405                       |
|           | 30 | 2984                                                  | 93.0                        | 1267                       |
|           | 45 | 3124                                                  | 93.6                        | 1128                       |
| 24        | 0  | 3264                                                  | 94.6                        | 0987                       |
|           | 15 | 3406                                                  | 95.2                        | 0845                       |
|           | 30 | 3549                                                  | 96.0                        | 0702                       |
|           | 45 | 3693                                                  | 96.7                        | 0559                       |
| 25        | 0  | 3838                                                  | 97.4                        | 0414                       |
|           | 15 | 3984                                                  | 98.1                        | 0268                       |
|           | 30 | 4131                                                  | 98.8                        | .4730120                   |
|           | 45 | 4279                                                  | 99.4                        | .4729972                   |
| 26        | 0  | 4428                                                  | 100.1                       | 9823                       |
|           | 15 | 4578                                                  | 100.9                       | 9673                       |
|           | 30 | 4730                                                  | 101.5                       | 9522                       |
|           | 45 | 4882                                                  | 102.1                       | 9370                       |
| 27        | 0  | 5035                                                  | 102.8                       | 9216                       |
|           | 15 | 5189                                                  | 103.4                       | 9062                       |
|           | 30 | 5344                                                  | 104.1                       | 8907                       |
|           | 45 | 5500                                                  | 104.7                       | 8751                       |
| 28        | 0  | 5657                                                  | 105.3                       | 8594                       |
|           | 15 | 5815                                                  | 106.0                       | 8436                       |
|           | 30 | 5974                                                  | 106.5                       | 8277                       |
|           | 45 | 6.8416134                                             | 107.1                       | 8.4728117                  |

| Latitude.  |    | Log R.    | Com.<br>differ.<br>for 10'. | Log $\frac{1}{R \sin 1''}$ |
|------------|----|-----------|-----------------------------|----------------------------|
| $^{\circ}$ | '  |           |                             |                            |
| 29         | 0  | 6.8416295 |                             | 8.4727956                  |
|            | 15 | 6456      | 107.1                       | 7795                       |
|            | 30 | 6619      | 108.2                       | 7632                       |
|            | 45 | 6782      | 108.6                       | 7469                       |
| 30         | 0  | 6946      | 109.4                       | 7305                       |
|            | 15 | 7111      | 110.0                       | 7140                       |
|            | 30 | 7277      | 110.5                       | 6974                       |
|            | 45 | 7444      | 111.1                       | 6808                       |
| 31         | 0  | 7611      | 111.6                       | 6640                       |
|            | 15 | 7779      | 112.2                       | 6472                       |
|            | 30 | 7948      | 112.7                       | 6303                       |
|            | 45 | 8118      | 113.1                       | 6133                       |
| 32         | 0  | 8288      | 113.7                       | 5963                       |
|            | 15 | 8460      | 114.1                       | 5792                       |
|            | 30 | 8632      | 114.6                       | 5620                       |
|            | 45 | 8804      | 115.1                       | 5447                       |
| 33         | 0  | 8973      | 115.6                       | 5274                       |
|            | 15 | 9152      | 116.0                       | 5100                       |
|            | 30 | 9326      | 116.5                       | 4925                       |
|            | 45 | 9502      | 116.9                       | 4750                       |
| 34         | 0  | 9678      | 117.3                       | 4574                       |
|            | 15 | .8419854  | 117.7                       | 4397                       |
|            | 30 | .8420031  | 118.1                       | 4220                       |
|            | 45 | 0209      | 118.5                       | 4042                       |
| 35         | 0  | 0387      | 119.1                       | 3864                       |
|            | 15 | 0566      | 119.3                       | 3685                       |
|            | 30 | 0746      | 119.7                       | 3506                       |
|            | 45 | 0926      | 120.0                       | 3325                       |
| 36         | 0  | 1107      | 120.4                       | 3145                       |
|            | 15 | 1288      | 120.7                       | 2964                       |
|            | 30 | 1469      | 121.1                       | 2782                       |
|            | 45 | 1651      | 121.4                       | 2600                       |
| 37         | 0  | 1834      | 121.7                       | 2417                       |
|            | 15 | 2017      | 122.0                       | 2234                       |
|            | 30 | 2200      | 122.3                       | 2051                       |
|            | 45 | 2384      | 122.7                       | 1867                       |
| 38         | 0  | 2569      | 122.9                       | 1683                       |
|            | 15 | 2753      | 123.1                       | 1498                       |
|            | 30 | 2939      | 123.5                       | 1313                       |
|            | 45 | 3124      | 123.7                       | 1127                       |
| 39         | 0  | 3310      | 124.0                       | 0941                       |
|            | 15 | 3496      | 124.1                       | 0755                       |
|            | 30 | 3683      | 124.4                       | 0568                       |
|            | 45 | 3870      | 124.6                       | 0382                       |
|            |    |           | 124.8                       |                            |

| Latitude. | Log R     | Com.<br>differ.<br>for 10' | Log $\frac{1}{R \sin 1''}$ |
|-----------|-----------|----------------------------|----------------------------|
| 0         |           |                            |                            |
| 40 0      | 6.8424057 | 125.0                      | 8.4720194                  |
| 15        | 4244      | 125.1                      | .4720007                   |
| 30        | 4432      | 125.3                      | .4719819                   |
| 45        | 4620      | 125.5                      | 9631                       |
| 41 0      | 4808      | 125.7                      | 9443                       |
| 15        | 4997      | 125.8                      | 9254                       |
| 30        | 5186      | 126.0                      | 9066                       |
| 45        | 5375      | 126.2                      | 8877                       |
| 42 0      | 5564      | 126.2                      | 8687                       |
| 15        | 5753      | 126.3                      | 8498                       |
| 30        | 5943      | 126.4                      | 8309                       |
| 45        | 6132      | 126.6                      | 8119                       |
| 43 0      | 6322      | 126.6                      | 7929                       |
| 15        | 6512      | 126.7                      | 7739                       |
| 30        | 6702      | 126.7                      | 7549                       |
| 45        | 6892      | 126.8                      | 7359                       |
| 44 0      | 7082      | 126.8                      | 7169                       |
| 15        | 7273      | 126.9                      | 6979                       |
| 30        | 7463      | 127.0                      | 6788                       |
| 45        | 7653      | 126.9                      | 6598                       |
| 45 0      | 7844      | 127.0                      | 6408                       |
| 15        | 8034      | 126.9                      | 6217                       |
| 30        | 8224      | 126.9                      | 6027                       |
| 45        | 8415      | 126.9                      | 5837                       |
| 46 0      | 8605      | 126.8                      | 5647                       |
| 15        | 8795      | 126.8                      | 5456                       |
| 30        | 8985      | 126.7                      | 5266                       |
| 45        | 9175      | 126.7                      | 5076                       |
| 47 0      | 9365      | 126.6                      | 4886                       |
| 15        | 9555      | 126.6                      | 4696                       |
| 30        | 9745      | 126.4                      | 4506                       |
| 45        | .8429934  | 126.3                      | 4317                       |
| 48 0      | .8430124  | 126.2                      | 4127                       |
| 15        | 0313      | 126.1                      | 3938                       |
| 30        | 0502      | 126.0                      | 3749                       |
| 45        | 0691      | 125.8                      | 3560                       |
| 49 0      | 0880      | 125.7                      | 3371                       |
| 15        | 1068      | 125.5                      | 3183                       |
| 30        | 1257      | 125.3                      | 2995                       |
| 45        | 1445      | 125.0                      | 2807                       |
| 50 0      | 6.8431632 |                            | 8.4712619                  |

### XXI. *Trigonometrical Levelling.*

In the following formulæ let:

$\Delta$   $\Delta'$  represent the observed zenith distance of which  $\Delta$  is the smaller.

$d$   $A$ ,  $d$   $A'$  the height of each signal above the telescope of the instrument.

$K$  the distance in linear units between the two stations.

$a$  the known altitude of the station from which the zenith distance  $\Delta$  was measured.

$N$  the normal for the mean latitude of the two stations.

$M$  the modulus of common logarithms, having for its log 9.6377843.

1st. To compute the difference of level of two points by reciprocal zenith distances.

If possible, the zenith distances should be simultaneously taken, that the results may be independent of refraction.

$$\delta = \Delta + \frac{d A \sin \Delta}{K \sin 1''} \qquad \delta' = \Delta' + \frac{d A' \sin \Delta'}{K \sin 1''}$$

$$\begin{aligned} \text{Log diff. of level} = & \log \left\{ K \tan \frac{1}{2} (\delta' - \delta) \right\} + \frac{M}{N} a \quad \left. \vphantom{\log} \right\} \\ & \pm \frac{M}{2N} K \tan \frac{1}{2} (\delta' - \delta) + \frac{M}{12 N^3} K^3 \quad \left. \vphantom{\log} \right\} \end{aligned}$$

The third term of this formula will be positive, if  $a$  is the altitude of the point from which the smallest zenith distance, *always represented by*  $\Delta$ , has been observed; otherwise negative.

2d. To compute the difference of level of two points by a single zenith distance:

$$\delta = \Delta + \frac{d A \sin \Delta}{K \sin 1''}$$

$$\begin{aligned} \text{Log diff. of level} = & \log \left\{ \frac{K}{\tan \left( \delta - \frac{1-2r}{2N \sin 1''} K \right)} \right\} \\ & + \frac{M}{N}^a \pm \frac{M}{2N} \left\{ \frac{K}{\tan \left( \delta - \frac{1-2r}{2N \sin 1''} K \right)} \right\} + \frac{M}{12N^2} K^2 \end{aligned}$$

The third term will be positive when  $\Delta$  is less than  $90^\circ$ , which will be the case when  $\Delta$  is observed from the lowest point.

In this formula  $r$  represents the coefficient of terrestrial refraction, a variable quantity; its mean value is generally stated to be 0.08 with variation of 0.02 less in summer and more in winter.

If we assume  $r=0.08$ , the factor  $\frac{1-2r}{2N \sin 1''} = 0''004133$ ;

assuming also  $N$  to be constant and = to the normal at latitude  $45^\circ$ ,

$$\log N \text{ (in English feet)} = 7.3213623;$$

$$\log \frac{M}{N} = 2.3164220;$$

$$\log \frac{M}{2N} = 2.0153920;$$

$$\log \frac{M}{12N^2} = 3.9158785.$$

In ordinary cases, as an approximation, we may take:

$$\text{difference of level} = K \cot (\Delta - 0.004133 K.)$$

$K$  being in English feet and  $(0.004133 K)$  seconds of arc.

$$\text{Log } 0.004133 = 7.6163121.$$

3d. The method of reciprocal zenith distances gives the means of obtaining the coefficient of refraction  $r$ , which, using the same notation as before, is :

$$r = \left\{ \frac{180^\circ + \frac{K}{N \sin 1''} - (\delta + \delta')}{2 \frac{K}{N \sin 1''}} \right.$$

In the trigonometrical survey of Massachusetts, Mr. Borden used 0.0784 as a mean coefficient for the sea coast, and 0.0697 for the interior of the State.

4th. To compute the altitude of a station from the observed zenith distance of the sea horizon ; using the same notation as before :

$$\begin{aligned} \log \text{Alt.} = \log \frac{N}{2} \left( \frac{\sin 1''}{1-r} \right)^2 + \log (\delta - 90^\circ)^2 \\ + \frac{M}{4} \left( \frac{\sin 1''}{1-r} \right)^2 (\delta - 90^\circ)^2 \end{aligned}$$

It would be as well, to ensure greater accuracy, to observe the zenith distance of points of the horizon on several days, taking a mean of the whole; and also to note the state of the tide at the time of observation.

Should  $r$  be assumed = 0.08

$$\log \frac{1}{2} \left( \frac{\sin 1''}{1-r} \right)^2 = 9.1425441$$

$$\log \frac{M}{4} \left( \frac{\sin 1''}{1-r} \right)^2 = 8.4792985$$

The last term can generally be neglected, and  $N$  may be assumed as the Normal of latitude  $45^\circ$ .

*Corrections for Curvature and Refraction, showing the difference of the apparent and true level, in feet and decimals of a foot, for distances in feet and miles.*

| Distances<br>in feet. | CORRECTION IN FEET. |                      |                                      | Distances<br>in miles. | CORRECTION IN FEET. |                      |                                       |
|-----------------------|---------------------|----------------------|--------------------------------------|------------------------|---------------------|----------------------|---------------------------------------|
|                       | For cur-<br>vature. | For re-<br>fraction. | For curva-<br>ture and<br>refract'n. |                        | For curva-<br>ture. | For refrac-<br>tion. | For curva-<br>ture and<br>refraction. |
| 100                   | .00024              | .00004               | .00020                               |                        | .0417               | .0060                | .0357                                 |
| 150                   | .00054              | .00008               | .00046                               |                        | .1668               | .0238                | .1430                                 |
| 200                   | .00094              | .00013               | .00083                               |                        | .3752               | .0536                | .3216                                 |
| 250                   | .00149              | .00021               | .00128                               | 1                      | .6670               | .0953                | .5717                                 |
| 300                   | .00215              | .00031               | .00184                               | 1½                     | 1.5008              | .2144                | 1.2864                                |
| 350                   | .00293              | .00042               | .00251                               | 2                      | 2.6680              | .3811                | 2.2869                                |
| 400                   | .00383              | .00055               | .00328                               | 2½                     | 4.1688              | .5855                | 3.5733                                |
| 450                   | .00484              | .00069               | .00415                               | 3                      | 6.0030              | .8561                | 5.1469                                |
| 500                   | .00598              | .00085               | .00513                               | 3½                     | 8.1708              | 1.1673               | 7.0035                                |
| 550                   | .00724              | .00103               | .00621                               | 4                      | 10.6720             | 1.5246               | 9.1474                                |
| 600                   | .00861              | .00123               | .00738                               | 4½                     | 13.5468             | 1.9295               | 11.5773                               |
| 650                   | .01010              | .00144               | .00866                               | 5                      | 16.6750             | 2.3821               | 14.2929                               |
| 700                   | .01172              | .00167               | .01005                               | 5½                     | 20.1769             | 2.8824               | 17.2945                               |
| 750                   | .01345              | .00192               | .01153                               | 6                      | 24.0120             | 3.4303               | 20.5817                               |
| 800                   | .01531              | .00219               | .01312                               | 6½                     | 28.1809             | 4.0258               | 24.1551                               |
| 850                   | .01728              | .00247               | .01481                               | 7                      | 32.6830             | 4.6690               | 28.0143                               |
| 900                   | .01938              | .00277               | .01661                               | 7½                     | 37.5190             | 5.3599               | 32.1591                               |
| 950                   | .02159              | .00308               | .01851                               | 8                      | 42.6880             | 6.0997               | 36.5883                               |
| 1000                  | .02392              | .00333               | .02059                               | 8½                     | 48.1910             | 6.8844               | 41.3066                               |
| 1050                  | .02638              | .00377               | .02261                               | 9                      | 54.0270             | 7.7181               | 46.3089                               |
| 1100                  | .02895              | .00414               | .02481                               | 9½                     | 60.1971             | 8.5996               | 51.5975                               |
| 1150                  | .03164              | .00452               | .02712                               | 10                     | 66.7000             | 9.5286               | 57.1714                               |
| 1200                  | .03445              | .00492               | .02953                               | 11                     | 80.7070             | 11.5296              | 69.1774                               |
| 1250                  | .03738              | .00534               | .03204                               | 12                     | 96.0480             | 13.7211              | 82.3269                               |
| 1300                  | .04043              | .00578               | .03465                               | 13                     | 112.7230            | 16.1033              | 96.6197                               |
| 1350                  | .04361              | .00623               | .03738                               | 14                     | 130.7320            | 18.6760              | 112.0560                              |
| 1400                  | .04689              | .00670               | .04019                               | 15                     | 150.0750            | 21.4393              | 128.6357                              |
| 1450                  | .05030              | .00719               | .04311                               | 16                     | 170.7520            | 24.3931              | 146.3589                              |
| 1500                  | .05383              | .00769               | .04614                               | 17                     | 192.7630            | 27.5376              | 165.2254                              |
| 1550                  | .05748              | .00821               | .04927                               | 18                     | 216.1086            | 30.8727              | 185.2359                              |
| 1600                  | .06125              | .00875               | .05250                               | 19                     | 240.7870            | 34.3981              | 206.3889                              |
| 1650                  | .06514              | .00931               | .05583                               | 20                     | 266.8000            | 38.1143              | 228.6857                              |
| 1700                  | .06914              | .00988               | .05926                               |                        |                     |                      |                                       |
| 1750                  | .07327              | .01047               | .06280                               |                        |                     |                      |                                       |
| 1800                  | .07792              | .01107               | .06645                               |                        |                     |                      |                                       |
| 1850                  | .08188              | .01170               | .07018                               |                        |                     |                      |                                       |
| 1900                  | .08637              | .01234               | .07403                               |                        |                     |                      |                                       |
| 1950                  | .09098              | .01300               | .07798                               |                        |                     |                      |                                       |
| 2000                  | .09570              | .01367               | .08203                               |                        |                     |                      |                                       |

For a very close approximation,  
 correc'n for curvature, in ft., =  $\frac{2 D^2}{3}$   
 D being the distance in miles.



*Reduction, in feet and decimals, upon 100 feet, for the following vertical angles.*

| Angle. | Reduct. | Angle. | Reduct. | Angle. | Reduct. | Angle. | Reduct. |
|--------|---------|--------|---------|--------|---------|--------|---------|
| 0 /    |         | 0 /    |         | 0 /    |         | 0 /    |         |
| 3 0    | .137    | 7 30   | .856    | 12 0   | 2.185   | 16 30  | 4.118   |
| 3 15   | .161    | 7 45   | .913    | 12 15  | 2.277   | 16 45  | 4.243   |
| 3 30   | .187    | 8 0    | .973    | 12 30  | 2.370   | 17 0   | 4.370   |
| 3 45   | .214    | 8 15   | 1.035   | 12 45  | 2.466   | 17 15  | 4.498   |
| 4 0    | .244    | 8 30   | 1.098   | 13 0   | 2.553   | 17 30  | 4.628   |
| 4 15   | .275    | 8 45   | 1.164   | 13 15  | 2.662   | 17 45  | 4.760   |
| 4 30   | .308    | 9 0    | 1.231   | 13 30  | 2.763   | 18 0   | 4.894   |
| 4 45   | .343    | 9 15   | 1.300   | 13 45  | 2.866   | 18 15  | 5.030   |
| 5 0    | .381    | 9 30   | 1.371   | 14 0   | 2.970   | 18 30  | 5.168   |
| 5 15   | .420    | 9 45   | 1.444   | 14 15  | 2.077   | 18 45  | 5.307   |
| 5 30   | .460    | 10 0   | 1.519   | 14 30  | 3.185   | 19 0   | 5.448   |
| 5 45   | .503    | 10 15  | 1.596   | 14 45  | 3.295   | 19 15  | 5.591   |
| 6 0    | .548    | 10 30  | 1.675   | 15 0   | 3.407   | 19 30  | 5.736   |
| 6 15   | .594    | 10 45  | 1.755   | 15 15  | 3.521   | 19 45  | 5.882   |
| 6 30   | .643    | 11 0   | 1.837   | 15 30  | 3.637   | 20 0   | 6.031   |
| 6 45   | .663    | 11 15  | 1.921   | 15 45  | 3.754   |        |         |
| 7 0    | .745    | 11 30  | 2.008   | 16 0   | 3.874   |        |         |
| 7 15   | .800    | 11 45  | 2.095   | 16 15  | 3.995   |        |         |

*Ratio of Slopes for the following vertical angles.*

| Angle. | To one perpen-<br>dicular. | Angle. | To one perpen-<br>dicular. | Angle. | To one perpen-<br>dicular. | Angle. | To one perpen-<br>dicular. |
|--------|----------------------------|--------|----------------------------|--------|----------------------------|--------|----------------------------|
| 0 /    |                            | 0 /    |                            | 0 /    |                            | 0 /    |                            |
| 0 15   | 229                        | 3 35   | 16                         | 8 8    | 7                          | 18 26  | 3                          |
| 0 30   | 115                        | 3 49   | 15                         | 8 45   | 6½                         | 19 59  | 2½                         |
| 0 45   | 76                         | 4 6    | 14                         | 9 27   | 6                          | 21 48  | 2½                         |
| 1 0    | 57                         | 4 24   | 13                         | 9 52   | 5½                         | 23 58  | 2½                         |
| 1 15   | 46                         | 4 45   | 12                         | 10 18  | 5½                         | 26 34  | 2                          |
| 1 30   | 39                         | 5 0    | 11½                        | 10 47  | 5½                         | 29 44  | 1½                         |
| 1 45   | 33                         | 5 12   | 11                         | 11 19  | 5                          | 33 42  | 1½                         |
| 2 0    | 28                         | 5 27   | 10½                        | 11 53  | 4½                         | 38 40  | 1½                         |
| 2 15   | 25                         | 5 42   | 10                         | 12 32  | 4½                         | 45 0   | 1                          |
| 2 30   | 23                         | 6 0    | 9½                         | 13 15  | 4½                         | 53 8   | ¾                          |
| 2 45   | 21                         | 6 21   | 9                          | 14 2   | 4                          | 63 28  | ¾                          |
| 3 0    | 19                         | 6 43   | 8½                         | 14 55  | 3½                         | 75 58  | ¾                          |
| 3 15   | 18                         | 7 7    | 8                          | 15 56  | 3½                         | 78 41  | ½                          |
| 3 28   | 17                         | 7 36   | 7½                         | 17 6   | 3½                         |        |                            |

XXII. *Barometrical Measurement of Heights.*

For computing the difference in the heights of two places, by means of the Barometer.

$$x = 60345.51 \{ 1 + .001111 (t + t' - 64^\circ) \}$$

$$\times \log \text{ of } \left\{ \frac{\beta}{\beta'} \times \frac{1}{1 + .0001 (\tau - \tau')} \right\} \\ \times \{ 1 + .002695 \cos 2\phi \}$$

Where  $\phi$  = the latitude of the place.

|                                                            |                         |
|------------------------------------------------------------|-------------------------|
| $\beta$ = the height of the barometer,                     | } at the lower station. |
| $\tau$ = the temperature (Faht.) of the mercury, . . . . . |                         |
| $t$ = the temperature (Faht.) of the air, . . . . .        |                         |

|                                                             |                         |
|-------------------------------------------------------------|-------------------------|
| $\beta'$ = the height of the barometer,                     | } at the upper station. |
| $\tau'$ = the temperature (Faht.) of the mercury, . . . . . |                         |
| $t'$ = the temperature (Faht.) of the air, . . . . .        |                         |

Make  $A$  = the log of the first term, in English feet.

$B$  = the log of  $1 + .0001 (\tau - \tau')$

$C$  = the log of the last term.

$D = \log \beta - (\log \beta' + B)$

Then, by the tables which follow, the logarithm of the difference of altitude in English feet,

$$= A + C + \log D$$

TABLE I.—*Thermometers in the open air.*

| $t+t'$ | A.      | $t+t'$ | A.      | $t+t'$ | A.      | $t+t'$ | A.      |
|--------|---------|--------|---------|--------|---------|--------|---------|
| °      |         | °      |         | °      |         | °      |         |
| 1      | 4.74914 | 46     | 4.77187 | 91     | 4.79348 | 136    | 4.81407 |
| 2      | .74966  | 47     | .77236  | 92     | .79395  | 137    | .81452  |
| 3      | .75017  | 48     | .77285  | 93     | .79442  | 138    | .81496  |
| 4      | .75069  | 49     | .77334  | 94     | .79488  | 139    | .81541  |
| 5      | .75120  | 50     | .77383  | 95     | .79535  | 140    | .81585  |
| 6      | .75172  | 51     | .77432  | 96     | .79582  | 141    | .81630  |
| 7      | .75223  | 52     | .77481  | 97     | .79629  | 142    | .81675  |
| 8      | .75274  | 53     | .77530  | 98     | .79675  | 143    | .81719  |
| 9      | .75326  | 54     | .77579  | 99     | .79722  | 144    | .81763  |
| 10     | .75377  | 55     | .77628  | 100    | .79768  | 145    | .81807  |
| 11     | .75428  | 56     | .77677  | 101    | .79814  | 146    | .81851  |
| 12     | .75479  | 57     | .77726  | 102    | .79860  | 147    | .81895  |
| 13     | .75531  | 58     | .77774  | 103    | .79907  | 148    | .81939  |
| 14     | .75582  | 59     | .77823  | 104    | .79953  | 149    | .81983  |
| 15     | .75633  | 60     | .77871  | 105    | .79999  | 150    | .82027  |
| 16     | .75684  | 61     | .77919  | 106    | .80045  | 151    | .82071  |
| 17     | .75735  | 62     | .77968  | 107    | .80091  | 152    | .82115  |
| 18     | .75786  | 63     | .78016  | 108    | .80137  | 153    | .82159  |
| 19     | .75837  | 64     | .78065  | 109    | .80183  | 154    | .82203  |
| 20     | .75888  | 65     | .78113  | 110    | .80229  | 155    | .82247  |
| 21     | .75938  | 66     | .78161  | 111    | .80275  | 156    | .82291  |
| 22     | .75989  | 67     | .78209  | 112    | .80321  | 157    | .82335  |
| 23     | .76039  | 68     | .78257  | 113    | .80367  | 158    | .82379  |
| 24     | .76090  | 69     | .78305  | 114    | .80412  | 159    | .82423  |
| 25     | .76140  | 70     | .78352  | 115    | .80458  | 160    | .82466  |
| 26     | .76190  | 71     | .78400  | 116    | .80504  | 161    | .82510  |
| 27     | .76241  | 72     | .78449  | 117    | .80550  | 162    | .82553  |
| 28     | .76291  | 73     | .78497  | 118    | .80595  | 163    | .82596  |
| 29     | .76342  | 74     | .78544  | 119    | .80641  | 164    | .82640  |
| 30     | .76392  | 75     | .78592  | 120    | .80687  | 165    | .82683  |
| 31     | .76442  | 76     | .78640  | 121    | .80732  | 166    | .82727  |
| 32     | .76492  | 77     | .78688  | 122    | .80777  | 167    | .82770  |
| 33     | .76542  | 78     | .78735  | 123    | .80822  | 168    | .82813  |
| 34     | .76592  | 79     | .78783  | 124    | .80867  | 169    | .82857  |
| 35     | .76642  | 80     | .78830  | 125    | .80912  | 170    | .82900  |
| 36     | .76692  | 81     | .78878  | 126    | .80957  | 171    | .82943  |
| 37     | .76742  | 82     | .78925  | 127    | .81002  | 172    | .82986  |
| 38     | .76792  | 83     | .78972  | 128    | .81047  | 173    | .83030  |
| 39     | .76842  | 84     | .79019  | 129    | .81092  | 174    | .83073  |
| 40     | .76891  | 85     | .79066  | 130    | .81137  | 175    | .83116  |
| 41     | .76941  | 86     | .79113  | 131    | .81182  | 176    | .83159  |
| 42     | .76990  | 87     | .79160  | 132    | .81227  | 177    | .83201  |
| 43     | .77039  | 88     | .79207  | 133    | .81272  | 178    | .83244  |
| 44     | .77089  | 89     | .79254  | 134    | .81317  | 179    | .83287  |
| 45     | 4.77138 | 90     | 4.79301 | 135    | 4.81362 | 180    | 4.83329 |

TABLE II.—*Attached Thermometer.*

TABLE III.  
*Latitude of the place.*

| $\tau - \tau'$ | B.      | $\tau - \tau'$ | B.      | $\tau - \tau'$ | B.      | $\phi$ | C.      |
|----------------|---------|----------------|---------|----------------|---------|--------|---------|
| 0              |         | 0              |         | 0              |         |        |         |
| 0              | 0.00000 | 20             | 0.00087 | 40             | 0.00174 | 0      | 0.00117 |
| 1              | .00004  | 21             | .00091  | 41             | .00178  | 5      | 0.00115 |
| 2              | .00009  | 22             | .00096  | 42             | .00182  | 10     | 0.00110 |
| 3              | .00013  | 23             | .00100  | 43             | .00187  | 15     | 0.00100 |
| 4              | .00017  | 24             | .00104  | 44             | .00191  | 20     | 0.00090 |
| 5              | .00022  | 25             | .00109  | 45             | .00195  | 25     | 0.00075 |
| 6              | .00026  | 26             | .00113  | 46             | .00200  | 30     | 0.00058 |
| 7              | .00030  | 27             | .00117  | 47             | .00204  | 35     | 0.00040 |
| 8              | .00035  | 28             | .00122  | 48             | .00208  | 40     | 0.00020 |
| 9              | .00039  | 29             | .00126  | 49             | .00213  | 45     | 0.00000 |
| 10             | .00043  | 30             | .00130  | 50             | .00217  | 50     | 9.99980 |
| 11             | .00048  | 31             | .00135  | 51             | .00221  | 55     | 9.99960 |
| 12             | .00052  | 32             | .00139  | 52             | .00226  | 60     | 9.99942 |
| 13             | .00056  | 33             | .00143  | 53             | .00230  | 65     | 9.99925 |
| 14             | .00061  | 34             | .00148  | 54             | .00234  | 70     | 0.99910 |
| 15             | .00065  | 35             | .00152  | 55             | .00239  | 75     | 9.99900 |
| 16             | .00069  | 36             | .00156  | 56             | .00243  | 80     | 9.99890 |
| 17             | .00074  | 37             | .00161  | 57             | .00247  | 85     | 9.99885 |
| 18             | .00078  | 38             | .00165  | 58             | .00252  | 90     | 9.99883 |
| 19             | 0.00083 | 39             | 0.00169 | 59             | 0.00256 |        |         |

Example, latitude  $21^\circ$ .

|                                     | Upper Station.            | Lower Station. |
|-------------------------------------|---------------------------|----------------|
| Thermometer in open air $t' = 70.4$ | $t = 77.6$                |                |
| Attached Thermometer $\tau' = 70.4$ | $\tau = 77.6$             |                |
| Barometer $\beta' = 23.66$          | $\beta = 30.05$           |                |
| $B = 0.00031$                       | $\text{Log } D = 9.01502$ |                |
| $\text{Log } \beta' = 1.37401$      | $C = 0.00087$             |                |
|                                     | $A = 4.81939$             |                |
| $1.37432$                           |                           |                |
| $\text{Log } \beta = 1.47784$       | $3.83528$                 |                |
| $D = 0.10352$                       | $= 6843.7 \text{ feet.}$  |                |

*Table of comparison of Fahrenheit's Thermometer with  
Reaumur's and the Centesimal.*

| Fah. | Reaum. | Centes. | Fah. | Reaum. | Centes. | Fah. | Reaum. | Centes. |
|------|--------|---------|------|--------|---------|------|--------|---------|
| 0    | 0      | 0       | 33   | + 0.4  | + 0.6   | 67   | + 15.6 | + 19.4  |
| 0    | - 14.2 | - 17.8  | 34   | 0.9    | 1.1     | 68   | 16.0   | 20.0    |
| 1    | 13.8   | 17.2    | 35   | 1.3    | 1.7     | 69   | 16.4   | 20.6    |
| 2    | 13.3   | 16.7    | 36   | 1.8    | 2.2     | 70   | 16.9   | 21.1    |
| 3    | 12.9   | 16.1    | 37   | 2.2    | 2.8     | 71   | 17.3   | 21.7    |
| 4    | 12.4   | 15.6    | 38   | 2.7    | 3.3     | 72   | 17.8   | 22.2    |
| 5    | 12.0   | 15.0    | 39   | 3.1    | 3.9     | 73   | 18.2   | 22.8    |
| 6    | 11.6   | 14.4    | 40   | 3.6    | 4.4     | 74   | 18.7   | 23.3    |
| 7    | 11.1   | 13.9    | 41   | 4.0    | 5.0     | 75   | 19.1   | 23.9    |
| 8    | 10.7   | 13.3    | 42   | 4.4    | 5.6     | 76   | 19.6   | 24.4    |
| 9    | 10.2   | 12.8    | 43   | 4.9    | 6.1     | 77   | 20.0   | 25.0    |
| 10   | 9.8    | 12.2    | 44   | 5.3    | 6.7     | 78   | 20.4   | 25.6    |
| 11   | 9.3    | 11.7    | 45   | 5.8    | 7.2     | 79   | 20.9   | 26.1    |
| 12   | 8.9    | 11.1    | 46   | 6.2    | 7.8     | 80   | 21.3   | 26.7    |
| 13   | 8.4    | 10.6    | 47   | 6.7    | 8.3     | 81   | 21.8   | 27.2    |
| 14   | 8.0    | 10.0    | 48   | 7.1    | 8.9     | 82   | 22.2   | 27.8    |
| 15   | 7.6    | 9.4     | 49   | 7.6    | 9.4     | 83   | 22.7   | 28.3    |
| 16   | 7.1    | 8.9     | 50   | 8.0    | 10.0    | 84   | 23.1   | 28.9    |
| 17   | 6.7    | 8.3     | 51   | 8.4    | 10.6    | 85   | 23.6   | 29.4    |
| 18   | 6.2    | 7.8     | 52   | 8.9    | 11.1    | 86   | 24.0   | 30.0    |
| 19   | 5.8    | 7.2     | 53   | 9.3    | 11.7    | 87   | 24.4   | 30.6    |
| 20   | 5.3    | 6.7     | 54   | 9.8    | 12.2    | 88   | 24.9   | 31.1    |
| 21   | 4.9    | 6.1     | 55   | 10.2   | 12.8    | 89   | 25.3   | 31.7    |
| 22   | 4.4    | 5.6     | 56   | 10.7   | 13.3    | 90   | 25.8   | 32.2    |
| 23   | 4.0    | 5.0     | 57   | 11.1   | 13.9    | 91   | 26.2   | 32.8    |
| 24   | 3.6    | 4.4     | 58   | 11.6   | 14.4    | 92   | 26.7   | 33.3    |
| 25   | 3.1    | 3.9     | 59   | 12.0   | 15.0    | 93   | 27.1   | 33.9    |
| 26   | 2.7    | 3.3     | 60   | 12.4   | 15.6    | 94   | 27.6   | 34.4    |
| 27   | 2.2    | 2.8     | 61   | 12.9   | 16.1    | 95   | 28.0   | 35.0    |
| 28   | 1.8    | 2.8     | 62   | 13.3   | 16.7    | 96   | 28.4   | 35.6    |
| 29   | 1.3    | 1.7     | 63   | 13.8   | 17.2    | 97   | 28.9   | 36.1    |
| 30   | 0.9    | 1.1     | 64   | 14.2   | 17.8    | 98   | 29.3   | 36.7    |
| 31   | - 0.4  | - 0.6   | 65   | 14.7   | 18.3    | 99   | 29.8   | 37.2    |
| 32   | 0.0    | 0.0     | 66   | + 15.1 | + 18.9  | 100  | + 30.2 | + 37.8  |

$$x^{\circ} \text{ Reaumur} = (32^{\circ} + \frac{2}{5} x^{\circ}) \text{ Fah.} = \frac{4}{5} x^{\circ} \text{ Centes.}$$

$$x^{\circ} \text{ Centes.} = (32^{\circ} + \frac{2}{5} x^{\circ}) \text{ Fah.} = \frac{5}{4} x^{\circ} \text{ Reaum.}$$

$$x^{\circ} \text{ Fah.} = (x^{\circ} - 32^{\circ}) \frac{5}{9} \text{ Reau.} = (x^{\circ} - 32^{\circ}) \frac{5}{9} \text{ Cen.}$$

*Table for the comparison of French and English  
Barometers.*

| Milli-<br>metres. | English inches. | Milli-<br>metres. | English inches. | Milli-<br>metres. | English inches. |
|-------------------|-----------------|-------------------|-----------------|-------------------|-----------------|
| 501               | 19.725          | 531               | 20.906          | 561               | 22.087          |
| 502               | .764            | 532               | .945            | 562               | .126            |
| 503               | .803            | 533               | 20.985          | 563               | .166            |
| 504               | .843            | 534               | 21.024          | 564               | .205            |
| 505               | .882            | 535               | .063            | 565               | .244            |
| 506               | .921            | 536               | .103            | 566               | .284            |
| 507               | 19.961          | 537               | .142            | 567               | .323            |
| 508               | 20.000          | 538               | .181            | 568               | .363            |
| 509               | .040            | 539               | .221            | 569               | .402            |
| 510               | .079            | 540               | .266            | 570               | .441            |
| 511               | .118            | 541               | .300            | 571               | .481            |
| 512               | .158            | 542               | .339            | 572               | .520            |
| 513               | .197            | 543               | .378            | 573               | .559            |
| 514               | .236            | 544               | .417            | 574               | .599            |
| 515               | .276            | 545               | .457            | 575               | .638            |
| 516               | .315            | 546               | .496            | 576               | .678            |
| 517               | .354            | 547               | .536            | 577               | .717            |
| 518               | .394            | 548               | .575            | 578               | .756            |
| 519               | .433            | 549               | .614            | 579               | .796            |
| 520               | .473            | 550               | .654            | 580               | .835            |
| 521               | .512            | 551               | .693            | 581               | .875            |
| 522               | .551            | 552               | .733            | 582               | .914            |
| 523               | .591            | 553               | .772            | 583               | .953            |
| 524               | .630            | 554               | .811            | 584               | 22.993          |
| 525               | .670            | 555               | .851            | 585               | 23.032          |
| 526               | .709            | 556               | .890            | 586               | .071            |
| 527               | .748            | 557               | .930            | 587               | .111            |
| 528               | .788            | 558               | 21.969          | 588               | .150            |
| 529               | .827            | 559               | 22.009          | 589               | .189            |
| 530               | 20.867          | 560               | 22.048          | 590               | 23.229          |

*Table for the comparison of French and English  
Barometers.*

| Millime-<br>tres. | English inches. | Millime-<br>tres. | English inches. | Millime-<br>tres. | English inches. |
|-------------------|-----------------|-------------------|-----------------|-------------------|-----------------|
| 591               | 23.268          | 621               | 24.449          | 651               | 25.630          |
| 592               | .308            | 622               | .489            | 652               | .670            |
| 593               | .347            | 623               | .528            | 653               | .709            |
| 594               | .386            | 624               | .567            | 654               | .748            |
| 595               | .426            | 625               | .607            | 655               | .788            |
| 596               | .465            | 626               | .646            | 656               | .827            |
| 597               | .504            | 627               | .685            | 657               | .867            |
| 598               | .544            | 628               | .725            | 658               | .906            |
| 599               | .583            | 629               | .764            | 659               | .945            |
| 600               | .622            | 630               | .804            | 660               | 25.985          |
| 601               | .662            | 631               | .843            | 661               | 26.024          |
| 602               | .701            | 632               | .882            | 662               | .063            |
| 603               | .741            | 633               | .922            | 663               | .103            |
| 604               | .780            | 634               | .961            | 664               | .142            |
| 605               | .819            | 635               | 25.000          | 665               | .181            |
| 606               | .859            | 636               | .040            | 666               | .221            |
| 607               | .898            | 637               | .079            | 667               | .260            |
| 608               | .937            | 638               | .118            | 668               | .300            |
| 609               | 23.977          | 639               | .158            | 669               | .339            |
| 610               | 24.016          | 640               | .197            | 670               | .378            |
| 611               | .056            | 641               | .237            | 671               | .418            |
| 612               | .095            | 642               | .276            | 672               | .457            |
| 613               | .134            | 643               | .315            | 673               | .496            |
| 614               | .174            | 644               | .355            | 674               | .536            |
| 615               | .213            | 645               | .394            | 675               | .575            |
| 616               | .252            | 646               | .433            | 676               | .615            |
| 617               | .292            | 647               | .473            | 677               | .654            |
| 618               | .331            | 648               | .512            | 678               | .693            |
| 619               | .371            | 649               | .552            | 679               | .733            |
| 620               | 24.410          | 650               | 25.591          | 680               | 26.772          |

*Table for the comparison of French and English  
Barometers.*

| Millime-<br>tres. | English inches. | Millime-<br>tres. | English inches. | Millime-<br>tres. | English inches. |
|-------------------|-----------------|-------------------|-----------------|-------------------|-----------------|
| 681               | 26.811          | 711               | 27.992          | 741               | 29.173          |
| 682               | .851            | 712               | 28.032          | 742               | .213            |
| 683               | .890            | 713               | .071            | 743               | .252            |
| 684               | .930            | 714               | .110            | 744               | .292            |
| 685               | 26.969          | 715               | .150            | 745               | .331            |
| 686               | 27.008          | 716               | .189            | 746               | .370            |
| 687               | .048            | 717               | .229            | 747               | .410            |
| 688               | .087            | 718               | .268            | 748               | .449            |
| 689               | .126            | 719               | .307            | 749               | .488            |
| 690               | .166            | 720               | .347            | 750               | .528            |
| 691               | .205            | 721               | .386            | 751               | .567            |
| 692               | .245            | 722               | .425            | 752               | .606            |
| 693               | .284            | 723               | .465            | 753               | .646            |
| 694               | .323            | 724               | .504            | 754               | .685            |
| 695               | .363            | 725               | .543            | 755               | .725            |
| 696               | .402            | 726               | .583            | 756               | .764            |
| 697               | .441            | 727               | .622            | 757               | .803            |
| 698               | .481            | 728               | .662            | 758               | .843            |
| 699               | .520            | 729               | .701            | 759               | .882            |
| 700               | .559            | 730               | .740            | 760               | .921            |
| 701               | .599            | 731               | .780            | 761               | 29.961          |
| 702               | .638            | 732               | .819            | 762               | 30.000          |
| 703               | .677            | 733               | .858            | 763               | .040            |
| 704               | .717            | 734               | .898            | 764               | .079            |
| 705               | .756            | 735               | .937            | 765               | .118            |
| 706               | .795            | 736               | 28.977          | 766               | .158            |
| 707               | .835            | 737               | 29.016          | 767               | .197            |
| 708               | .874            | 738               | .055            | 768               | .236            |
| 709               | .914            | 739               | .095            | 769               | .276            |
| 710               | 27.953          | 740               | 29.134          | 770               | 30.315          |



*Table for the comparison of French and English  
Barometers.*

| Millime-<br>tres. | English inches. | Millime-<br>tres. | English inches. | PROPORTIONAL PARTS. |                 |
|-------------------|-----------------|-------------------|-----------------|---------------------|-----------------|
|                   |                 |                   |                 | Millim.             | English inches. |
| 771               | 30.255          | 781               | 30.748          | 0.1                 | 0.0039          |
| 772               | .394            | 782               | .788            | .2                  | .0079           |
| 773               | .433            | 783               | .827            | .3                  | .0118           |
| 774               | .473            | 784               | .866            | .4                  | .0157           |
| 775               | .512            | 785               | .906            | .5                  | .0197           |
| 776               | .551            | 786               | .945            | .6                  | .0236           |
| 777               | .591            | 787               | 30.984          | .7                  | .0276           |
| 778               | .630            | 788               | 31.024          | .8                  | .0315           |
| 779               | .670            | 789               | .063            | 0.9                 | .0354           |
| 780               | 30.709          | 790               | 31.103          | 1.0                 | 0.0394          |

1 Metre = 39.3707 English inches = 443.296 Paris lines.

1 English foot = 0.304794 metre = 135.114 Paris lines.

1 French foot = 1.0658 English feet = 0.32484 metre.

| French inches |  | English inches. |  | French lines. |  | English inches. |  |
|---------------|--|-----------------|--|---------------|--|-----------------|--|
| 1             |  | 1.0658          |  | 1             |  | 0.0888          |  |
| 2             |  | 2.1315          |  | 2             |  | .1776           |  |
| 3             |  | 3.1973          |  | 3             |  | .2664           |  |
| 4             |  | 4.2631          |  | 4             |  | .3553           |  |
| 5             |  | 5.3288          |  | 5             |  | .4441           |  |
| 6             |  | 6.3946          |  | 6             |  | .5329           |  |
| 7             |  | 7.4604          |  | 7             |  | .6217           |  |
| 8             |  | 8.5261          |  | 8             |  | .7105           |  |
| 9             |  | 9.5919          |  | 9             |  | .7993           |  |
| 10            |  | 10.6577         |  | 10            |  | .8881           |  |
| 11            |  | 11.7234         |  | 11            |  | .9770           |  |
| 12            |  | 12.7890         |  | 12            |  | 1.0658          |  |

*Table for the comparison of French and English  
Barometers.*

| English<br>inches<br>and<br>tenths. | Hundredths of an inch. |        |        |        |        |
|-------------------------------------|------------------------|--------|--------|--------|--------|
|                                     | 0                      | 2      | 4      | 6      | 8      |
|                                     | Millimetres.           |        |        |        |        |
| 21.0                                | 533.39                 | 533.90 | 534.41 | 534.91 | 535.42 |
| .1                                  | 535.93                 | 536.44 | 536.95 | 537.45 | 537.96 |
| .2                                  | 538.47                 | 538.98 | 539.49 | 539.99 | 540.50 |
| .3                                  | 541.01                 | 541.52 | 542.03 | 542.53 | 543.04 |
| .4                                  | 543.55                 | 544.06 | 544.57 | 545.07 | 545.58 |
| .5                                  | 546.09                 | 546.60 | 547.11 | 547.61 | 548.12 |
| .6                                  | 548.63                 | 549.14 | 549.65 | 550.15 | 550.66 |
| .7                                  | 551.17                 | 551.68 | 552.19 | 552.69 | 553.20 |
| .8                                  | 553.71                 | 554.22 | 554.73 | 555.23 | 555.74 |
| .9                                  | 556.25                 | 556.76 | 557.27 | 557.77 | 558.28 |
| 22.0                                | 558.79                 | 559.30 | 559.81 | 560.31 | 560.82 |
| .1                                  | 561.33                 | 561.84 | 562.35 | 562.85 | 563.36 |
| .2                                  | 563.87                 | 564.38 | 564.89 | 565.39 | 565.90 |
| .3                                  | 566.41                 | 566.92 | 567.43 | 567.93 | 568.44 |
| .4                                  | 568.95                 | 569.46 | 569.97 | 570.47 | 570.98 |
| .5                                  | 571.49                 | 572.00 | 572.51 | 573.01 | 573.55 |
| .6                                  | 574.03                 | 574.54 | 575.05 | 575.55 | 576.06 |
| .7                                  | 576.57                 | 577.08 | 577.59 | 578.09 | 578.60 |
| .8                                  | 579.11                 | 579.62 | 580.13 | 580.63 | 581.14 |
| .9                                  | 581.65                 | 582.16 | 582.67 | 583.17 | 583.68 |
| 23.0                                | 584.19                 | 584.70 | 585.21 | 585.71 | 586.22 |
| .1                                  | 586.73                 | 587.24 | 587.75 | 588.25 | 588.76 |
| .2                                  | 589.27                 | 589.78 | 590.29 | 590.79 | 591.30 |
| .3                                  | 591.81                 | 592.32 | 592.83 | 593.33 | 593.84 |
| .4                                  | 594.35                 | 594.86 | 595.37 | 595.87 | 596.38 |
| .5                                  | 596.89                 | 597.40 | 597.91 | 598.41 | 598.92 |
| .6                                  | 599.43                 | 599.94 | 600.45 | 600.95 | 601.46 |
| .7                                  | 601.97                 | 602.48 | 602.99 | 603.49 | 604.00 |
| .8                                  | 604.51                 | 605.02 | 605.53 | 606.03 | 606.54 |
| .9                                  | 607.05                 | 607.56 | 608.07 | 608.57 | 609.08 |

*Table for the comparison of French and English  
Barometers.*

| English<br>inches<br>and<br>tenths. | Hundredths of an inch. |        |        |        |        |
|-------------------------------------|------------------------|--------|--------|--------|--------|
|                                     | 0                      | 2      | 4      | 6      | 8      |
|                                     | Millimetres.           |        |        |        |        |
| 24.0                                | 609.59                 | 610.10 | 610.61 | 611.11 | 611.62 |
| .1                                  | 612.13                 | 612.64 | 613.15 | 613.65 | 614.16 |
| .2                                  | 614.67                 | 615.18 | 615.69 | 616.19 | 616.70 |
| .3                                  | 617.21                 | 617.72 | 618.23 | 618.73 | 619.24 |
| .4                                  | 619.75                 | 620.26 | 620.77 | 621.27 | 621.78 |
| .5                                  | 622.29                 | 622.80 | 623.31 | 623.81 | 624.32 |
| .6                                  | 624.83                 | 625.34 | 625.85 | 626.34 | 626.86 |
| .7                                  | 627.37                 | 627.88 | 628.39 | 628.89 | 629.40 |
| .8                                  | 629.91                 | 630.42 | 630.93 | 631.43 | 631.94 |
| .9                                  | 632.45                 | 632.96 | 633.47 | 633.97 | 634.48 |
| 25.0                                | 634.99                 | 635.50 | 636.01 | 636.51 | 637.02 |
| .1                                  | 637.53                 | 638.04 | 638.55 | 639.05 | 639.56 |
| .2                                  | 640.07                 | 640.58 | 641.09 | 641.59 | 642.10 |
| .3                                  | 642.61                 | 643.12 | 643.63 | 644.13 | 644.64 |
| .4                                  | 645.15                 | 645.66 | 646.17 | 646.67 | 647.18 |
| .5                                  | 647.69                 | 648.20 | 648.71 | 649.21 | 649.72 |
| .6                                  | 650.23                 | 650.74 | 651.25 | 651.75 | 652.26 |
| .7                                  | 652.77                 | 653.28 | 653.79 | 654.29 | 654.80 |
| .8                                  | 655.31                 | 655.82 | 656.33 | 656.83 | 657.34 |
| .9                                  | 657.85                 | 658.36 | 658.87 | 659.37 | 659.88 |
| 26.0                                | 660.39                 | 660.90 | 661.41 | 661.91 | 662.42 |
| .1                                  | 662.93                 | 663.44 | 663.95 | 664.45 | 664.96 |
| .2                                  | 665.47                 | 665.98 | 666.49 | 666.99 | 667.50 |
| .3                                  | 668.01                 | 668.52 | 669.03 | 669.53 | 670.04 |
| .4                                  | 670.55                 | 671.06 | 671.57 | 672.07 | 672.58 |
| .5                                  | 673.09                 | 673.60 | 674.11 | 674.61 | 675.12 |
| .6                                  | 675.63                 | 676.14 | 676.65 | 677.15 | 677.66 |
| .7                                  | 678.17                 | 678.68 | 679.19 | 679.69 | 680.20 |
| .8                                  | 680.71                 | 681.22 | 681.73 | 682.23 | 682.74 |
| .9                                  | 683.25                 | 683.76 | 684.27 | 684.77 | 685.28 |

*Table for the comparison of French and English  
Barometers.*

| English<br>inches and<br>tenths. | Hundredths of an inch. |        |        |        |        |
|----------------------------------|------------------------|--------|--------|--------|--------|
|                                  | 0                      | 2      | 4      | 6      | 8      |
|                                  | Millimetres.           |        |        |        |        |
| 27.0                             | 685.79                 | 686.30 | 686.81 | 687.31 | 687.82 |
| .1                               | 688.33                 | 688.84 | 689.35 | 689.85 | 690.36 |
| .2                               | 690.87                 | 691.38 | 691.89 | 692.39 | 692.90 |
| .3                               | 693.41                 | 693.92 | 694.43 | 694.93 | 695.44 |
| .4                               | 695.95                 | 696.46 | 696.97 | 697.47 | 697.98 |
| .5                               | 698.49                 | 699.00 | 699.51 | 700.01 | 700.52 |
| .6                               | 701.03                 | 701.54 | 702.05 | 702.55 | 703.06 |
| .7                               | 703.57                 | 704.08 | 704.59 | 705.09 | 705.60 |
| .8                               | 706.11                 | 706.62 | 707.13 | 707.63 | 708.14 |
| .9                               | 708.65                 | 709.16 | 709.67 | 710.17 | 710.68 |
| 28.0                             | 711.19                 | 711.70 | 712.21 | 712.71 | 713.22 |
| .1                               | 713.73                 | 714.24 | 714.75 | 715.25 | 715.77 |
| .2                               | 716.27                 | 716.78 | 717.29 | 717.79 | 718.30 |
| .3                               | 718.81                 | 719.32 | 719.83 | 720.33 | 720.84 |
| .4                               | 721.35                 | 721.86 | 722.37 | 722.87 | 723.38 |
| .5                               | 723.89                 | 724.40 | 724.91 | 725.41 | 725.92 |
| .6                               | 726.43                 | 726.94 | 727.45 | 727.95 | 728.46 |
| .7                               | 728.97                 | 729.48 | 729.99 | 730.49 | 731.00 |
| .8                               | 731.51                 | 732.02 | 732.53 | 733.03 | 733.54 |
| .9                               | 734.05                 | 734.56 | 735.07 | 735.57 | 736.08 |
| 29.0                             | 736.59                 | 737.10 | 737.61 | 738.11 | 738.62 |
| .1                               | 739.13                 | 739.64 | 740.15 | 740.65 | 740.16 |
| .2                               | 741.67                 | 742.18 | 742.69 | 743.19 | 743.70 |
| .3                               | 744.21                 | 744.72 | 745.23 | 745.73 | 746.24 |
| .4                               | 746.75                 | 747.26 | 747.77 | 748.27 | 748.78 |
| .5                               | 749.29                 | 749.80 | 750.31 | 750.81 | 751.32 |
| .6                               | 751.83                 | 752.34 | 752.85 | 753.35 | 753.86 |
| .7                               | 754.37                 | 754.88 | 755.39 | 755.89 | 756.40 |
| .8                               | 756.91                 | 757.42 | 757.93 | 758.43 | 758.94 |
| .9                               | 759.45                 | 759.96 | 760.47 | 760.97 | 761.48 |

*Table for the comparison of French and English  
Barometers.*

| English<br>inches and<br>tenths. | Hundredths of an inch. |        |        |        |        |
|----------------------------------|------------------------|--------|--------|--------|--------|
|                                  | 0                      | 2      | 4      | 6      | 8      |
|                                  | Millimetres.           |        |        |        |        |
| 30.0                             | 761.99                 | 762.50 | 763.01 | 763.51 | 764.02 |
| .1                               | 764.53                 | 765.04 | 765.55 | 766.05 | 766.56 |
| .2                               | 767.07                 | 767.58 | 768.09 | 768.59 | 769.10 |
| .3                               | 769.61                 | 770.12 | 770.63 | 771.13 | 771.64 |
| .4                               | 772.15                 | 772.66 | 773.17 | 773.67 | 774.18 |
| .5                               | 774.69                 | 775.20 | 775.71 | 776.21 | 776.72 |
| .6                               | 777.23                 | 777.74 | 778.25 | 778.75 | 779.26 |
| .7                               | 779.77                 | 780.28 | 780.79 | 781.29 | 781.80 |
| .8                               | 782.31                 | 782.82 | 783.33 | 783.83 | 784.34 |
| .9                               | 784.85                 | 785.36 | 785.87 | 786.37 | 786.88 |

*Table of corrections for capillary action to be added to  
English Barometers.*

| Diameter of<br>tube. | Ivory.  | Young.  | Laplace. | Com. of Physics, &c.<br>Royal Soc., 1840. |               |
|----------------------|---------|---------|----------|-------------------------------------------|---------------|
|                      |         |         |          | Unboiled<br>tubes.                        | Boiled tubes. |
| Inches.              | Inches. | Inches. | Inches.  | Inches.                                   | Inches.       |
| 0.05                 | 0.2949  | 0.2964  | 0.       |                                           |               |
| .10                  | .1404   | .1424   | .1394    | 0.142                                     | 0.070         |
| .15                  | .0865   | .0880   | .0854    | .088                                      | .044          |
| .20                  | .0583   | .0589   | .0580    | .060                                      | .029          |
| .25                  | .0409   | .0404   | .0412    | .040                                      | .020          |
| .30                  | .0293   | .0280   | .0296    | .028                                      | .014          |
| .35                  | .0212   | .0196   | .0216    | .020                                      | .010          |
| .40                  | .0154   | .0139   | .0159    | .014                                      | .007          |
| .45                  | .0112   | .0100   | .0117    | .010                                      | .005          |
| .50                  | .0082   | .0074   | .0087    | .007                                      | .003          |
| .60                  | .0043   | .0045   | .0046    | 0.004                                     | 0.002         |
| .70                  | .0023   | .....   | .0024    |                                           |               |
| 0.80                 | 0.0012  | .....   | 0.0013   |                                           |               |

XXIII. *Thermometrical Measurement of Heights.*

*Table of Barometric pressures corresponding to temperatures of boiling water.*

| Degrees of<br>Fahrenheit. | TENTHS OF A DEGREE OF FAHRENHEIT. |        |        |        |        |
|---------------------------|-----------------------------------|--------|--------|--------|--------|
|                           | 0.                                | 2.     | 4.     | 6.     | 8.     |
| 185                       | 17.048                            | 17.123 | 17.199 | 17.274 | 17.350 |
| 186                       | .425                              | .502   | .578   | .655   | .731   |
| 187                       | .808                              | .886   | .964   | 18.042 | 18.120 |
| 188                       | 18.198                            | 18.277 | 18.357 | .436   | .516   |
| 189                       | .595                              | .676   | .756   | .837   | .918   |
| 190                       | .999                              | 19.081 | 19.163 | 19.245 | 19.328 |
| 191                       | 19.410                            | .493   | .577   | .661   | .744   |
| 192                       | .828                              | .913   | .998   | 20.083 | 20.169 |
| 193                       | 20.254                            | 20.341 | 20.427 | .514   | .601   |
| 194                       | .688                              | .776   | .864   | .952   | 21.041 |
| 195                       | 21.129                            | 21.219 | 21.309 | 21.398 | .488   |
| 196                       | .578                              | .669   | .761   | .853   | .944   |
| 197                       | 22.036                            | 22.129 | 22.222 | 22.315 | 22.409 |
| 198                       | .502                              | .597   | .692   | .786   | .881   |
| 199                       | .976                              | 23.072 | 23.169 | 23.265 | 23.362 |
| 200                       | 23.458                            | .556   | .654   | .752   | .850   |
| 201                       | .948                              | 24.047 | 24.147 | 24.247 | 24.346 |
| 202                       | 24.446                            | .547   | .648   | .750   | 851    |
| 203                       | .952                              | 25.055 | 25.158 | 25.261 | 25.364 |
| 204                       | 25.467                            | .572   | .677   | .781   | .886   |
| 205                       | .991                              | 26.097 | 26.204 | 26.311 | 26.417 |
| 206                       | 26.524                            | .632   | .741   | .849   | .957   |
| 207                       | 27.066                            | 27.176 | 27.286 | 27.397 | 27.507 |
| 208                       | .617                              | .729   | .841   | .954   | 28.066 |
| 209                       | 28.178                            | 28.292 | 28.406 | 28.521 | .635   |
| 210                       | .749                              | .865   | .981   | 29.098 | 29.214 |
| 211                       | 29.330                            | 29.448 | 29.566 | .685   | .803   |
| 212                       | .921                              | 30.041 | 30.161 | 30.281 | 30.402 |

**XXIV. Formulae for computing the elements for the projection of Maps.**

1. For surfaces of not more than four degrees of latitude and longitude, the formulae being approximate.

$$1. \text{ Normal} = N = \frac{a}{(1 - e^2 \sin^2 L)^{\frac{1}{2}}}$$

$$2. \text{ Tangent} = T = N \cot L$$

$$3. \text{ Radius of the parallel} = (Rp) = N \cos L$$

$$4. \text{ Degree of the parallel} = (Dp) = \frac{(Rp) \pi}{180^\circ}$$

5. Number of minutes of the parallel

$$= (n') p = (n') p \frac{Dp}{60}$$

6. Angle between the tangent and the chord

$$= \sin \frac{1}{2} Z = \frac{(n') p}{2 T}$$

Then,

$$\begin{aligned} \text{difference of parallels} = y = \delta p &= (n') p \sin \frac{1}{2} z \\ &= \frac{[(n') p]^2}{2 T} \end{aligned}$$

$$\text{difference of meridians} = x = \delta m = (n') p \cos \frac{1}{2} z$$

The values  $\delta m$  and  $\delta p$  will be found in the following tables.

*Example of their use.*—Let it be required to make a projection containing 40' of longitude between the parallels of 41° 30' and 42° 10', to be subdivided to 5'.

Assume the centre of the sheet to be the intersection of the middle parallel with the middle meridian of the proposed map, which point call A; in this case a point in the parallel of 41° 50'.

Through A draw the central meridian and a line at right angles to it.

Beginning at A, lay off above and below, on the central meridian, the values of  $Dm$  from  $41^{\circ} 50'$  to  $41^{\circ} 55'$ ;  $41^{\circ} 55'$  to  $42^{\circ}$ ;  $42^{\circ}$  to  $42^{\circ} 5'$ , etc.; and from  $41^{\circ} 50'$  to  $41^{\circ} 45'$ ;  $41^{\circ} 45'$  to  $41^{\circ} 40'$ , etc. These values to be taken from the table of *Meridional arcs—values of  $Dm$  in yards*, by interpolation from the values there given for the middle latitudes of  $41^{\circ}$  and  $42^{\circ}$ .

Through each of the points ....A".A'.A.A<sub>1</sub>A<sub>11</sub>... thus found, lay off perpendiculars to the central meridian.

Now turn to the table of *Co-ordinates  $\delta m$  and  $\delta p$  in yards* and lay off, from each of the points ....A".A'.A.A<sub>1</sub>A<sub>11</sub>... to the right and left of the central meridian, the values of  $\delta m$  for successively  $5'$ ,  $10'$ ,  $15'$  and  $20'$ , corresponding (by interpolation from the columns of  $41^{\circ} 30'$  and  $42^{\circ}$ ) to each parallel of latitude required; and, from the points thus found, the corresponding values of  $\delta p$  at right angles to the lines already drawn.

Lines passing through the extremities of  $\delta p$  will be the required meridians and parallels.

The projection being made, any point whose latitude and longitude is known will be projected on the map from elements taken from the table of values of  $Dm$  and  $Dp$ , which are measured from the *meridians* and *parallels*, and not from the axes of co-ordinates used in making the projection.

2. *When the map extends over several degrees of latitude and longitude*, the preceding approximate formulæ will not answer; a middle latitude is assumed where the developing cone is tangent, and the projection made as follows:

Through the centre of the map, A, two lines are drawn, Ay representing the central meridian, and the other, Ax,



a line perpendicular to it; from the point A, along the line Ay (above and below A) the lengths  $s, s_1, s_2, s_3, \dots, s_r$  (in miles or yards) of degrees or minutes, as the case may be, of the meridian are laid down, and the remaining intersections of meridians and parallels are projected by means of co-ordinates  $y$  and  $x$  from the central point A, as follows:

$$x = dm = \text{difference of meridians} = \rho \sin \theta$$

$$y = dp = \text{difference of parallels} = s + x \tan \frac{1}{2} \theta$$

$$\theta = (n')p \frac{Rp}{T} \quad \cdot \quad \rho = T \pm S$$

where  $s$  = the length on the meridian from minute to minute or degree to degree as desired.

$T = N \cot L$  = the tangent at the central point of the map,  $L$  being the latitude and  $N$  the normal at that point.

$(Rp) = N' \cos l$  = the radius of the parallel at any point of latitude (above or below the central point) of which the ordinate is required.

$(n')p$  = the number of minutes of the parallel of the new point of which the ordinate is required.

3. *In maps of large portions of the Earth's surface* deviations from real magnitudes may be lessened by making the developing cone cut two parallels equidistant from the middle parallel; say through one-third of the length of the middle meridian of the map.

It will then be necessary to substitute for  $T$  in the preceding equation, the distance from the vertex of the cone to either intersection of the Earth's surface

$$= \frac{Rp}{\sin S}, \quad S \text{ being the angle at the vertex between the}$$

elements of the cone and its axis; equal, in a spheroid, to one-half the sum of the geocentric latitudes of the two points of intersection.

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 22° 0' |            | Lat. 22° 30' |            | Lat. 23° 0' |            |
|-------------------------|-------------|------------|--------------|------------|-------------|------------|
|                         | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ |
| 1'                      | 1882.0      | 0.1        | 1875.3       | 0.1        | 1868.5      | 0.1        |
| 2                       | 3763.9      | 0.4        | 3750.6       | 0.4        | 3737.0      | 0.4        |
| 3                       | 5645.9      | 0.9        | 5625.9       | 1.0        | 5605.4      | 1.0        |
| 4                       | 7527.8      | 1.6        | 7501.2       | 1.7        | 7473.9      | 1.7        |
| 5                       | 9409.9      | 2.6        | 9376.4       | 2.6        | 9342.4      | 2.7        |
| 6                       | 11291.8     | 3.7        | 11251.7      | 3.7        | 11210.9     | 3.8        |
| 7                       | 13173.7     | 5.0        | 13127.0      | 5.1        | 13079.4     | 5.2        |
| 8                       | 15055.7     | 6.6        | 15002.3      | 6.7        | 14947.8     | 6.8        |
| 9                       | 16937.6     | 8.3        | 16877.6      | 8.5        | 16816.3     | 8.6        |
| 10                      | 18819.6     | 10.3       | 18752.9      | 10.5       | 18684.8     | 10.6       |
| 11                      | 20701.6     | 12.4       | 20628.2      | 12.6       | 20553.3     | 12.8       |
| 12                      | 22583.5     | 14.8       | 22503.5      | 15.0       | 22421.8     | 15.3       |
| 13                      | 24465.5     | 17.3       | 24378.8      | 17.6       | 24290.2     | 17.9       |
| 14                      | 26347.4     | 20.1       | 26254.1      | 20.5       | 26158.7     | 20.8       |
| 15                      | 28229.4     | 23.1       | 28129.3      | 23.5       | 28027.2     | 23.9       |
| 16                      | 30111.4     | 26.2       | 30004.6      | 26.7       | 29895.7     | 27.2       |
| 17                      | 31993.3     | 29.6       | 31879.9      | 30.2       | 31764.2     | 30.7       |
| 18                      | 33875.3     | 33.2       | 33755.2      | 33.3       | 33632.6     | 34.4       |
| 19                      | 35757.2     | 37.0       | 35630.5      | 37.7       | 35501.1     | 38.3       |
| 20                      | 37639.2     | 41.0       | 37505.8      | 41.7       | 37369.6     | 42.5       |
| 25                      | 47049.0     | 64.1       | 46675.8      | 65.2       | 46712.0     | 66.4       |
| 30                      | 56458.7     | 92.3       | 56258.7      | 93.9       | 56054.3     | 95.6       |
| 40                      | 75278.2     | 164.1      | 75011.5      | 167.0      | 74733.0     | 169.9      |
| 50                      | 94097.7     | 256.3      | 93764.2      | 260.9      | 93423.7     | 265.5      |
| 1° 00                   | 112917.0    | 369.1      | 112516.9     | 375.8      | 112108.2    | 382.3      |
| 1 20                    | 150555.4    | 656.2      | 150021.9     | 668.0      | 149476.9    | 679.6      |
| 1 30                    | 169374.4    | 830.5      | 168774.2     | 845.4      | 168161.1    | 860.1      |
| 1 40                    | 188193.3    | 1025.3     | 187526.3     | 1043.8     | 186845.1    | 1061.8     |
| 2 00                    | 225830.5    | 1476.5     | 225030.0     | 1503.0     | 224212.5    | 1529.1     |
| 2 30                    | 282284.7    | 2307.1     | 281284.0     | 2348.5     | 280261.9    | 2389.2     |
| 3 00                    | 338736.6    | 3322.2     | 337535.6     | 3381.8     | 336309.0    | 3440.4     |
| 3 30                    | 395186.0    | 4521.9     | 393784.5     | 4603.0     | 392353.1    | 4682.8     |
| 4 00                    | 451632.0    | 5906.2     | 450029.9     | 6012.1     | 448393.7    | 6116.2     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 23° 30' |            | Lat. 24° 0' |            | Lat. 24° 30' |            |
|-------------------------|--------------|------------|-------------|------------|--------------|------------|
|                         | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ |
| 1'                      | 1861.5       | 0.1        | 1854.4      | 0.1        | 1847.2       | 0.1        |
| 2                       | 3723.1       | 0.4        | 3708.9      | 0.4        | 3694.4       | 0.4        |
| 3                       | 5584.6       | 1.0        | 5563.3      | 1.0        | 5541.6       | 1.0        |
| 4                       | 7446.1       | 1.8        | 7417.7      | 1.8        | 7388.8       | 1.8        |
| 5                       | 9307.6       | 2.7        | 9272.2      | 2.7        | 9236.0       | 2.8        |
| 6                       | 11169.2      | 3.9        | 11126.6     | 3.9        | 11083.2      | 4.0        |
| 7                       | 13030.7      | 5.3        | 12981.0     | 5.4        | 12930.4      | 5.4        |
| 8                       | 14892.2      | 6.9        | 14835.5     | 7.0        | 14777.6      | 7.1        |
| 9                       | 16753.7      | 8.7        | 16689.9     | 8.9        | 16624.8      | 9.0        |
| 10                      | 18615.3      | 10.8       | 18544.3     | 11.0       | 18472.0      | 11.1       |
| 11                      | 20476.8      | 13.1       | 20398.8     | 13.3       | 20319.2      | 13.5       |
| 12                      | 22338.3      | 15.6       | 22253.2     | 15.8       | 22166.4      | 16.0       |
| 13                      | 24199.9      | 18.2       | 24107.6     | 18.5       | 24013.6      | 18.8       |
| 14                      | 26061.4      | 21.2       | 25962.1     | 21.5       | 25860.8      | 21.8       |
| 15                      | 27922.9      | 24.3       | 27816.5     | 24.7       | 27708.0      | 25.1       |
| 16                      | 29784.4      | 27.7       | 29670.9     | 28.1       | 29555.2      | 28.5       |
| 17                      | 31646.0      | 31.2       | 31525.4     | 31.7       | 31402.4      | 32.2       |
| 18                      | 33507.5      | 35.0       | 33379.8     | 35.5       | 33249.6      | 36.0       |
| 19                      | 35369.0      | 39.0       | 35234.2     | 39.6       | 35096.8      | 40.2       |
| 20                      | 37230.5      | 43.2       | 37088.7     | 43.9       | 36944.0      | 44.6       |
| 25                      | 46538.1      | 67.5       | 46360.8     | 68.6       | 46179.9      | 69.6       |
| 30                      | 55845.8      | 97.2       | 55632.9     | 98.7       | 55415.9      | 100.3      |
| 40                      | 74460.9      | 172.7      | 74177.1     | 175.5      | 73887.7      | 178.3      |
| 50                      | 93076.0      | 269.9      | 92721.3     | 274.3      | 92359.5      | 278.5      |
| 1° 00                   | 111691.0     | 388.7      | 111365.3    | 394.9      | 110831.4     | 401.1      |
| 1 20                    | 148920.6     | 690.9      | 148353.0    | 702.1      | 147774.1     | 713.0      |
| 1 30                    | 167535.2     | 874.5      | 166896.6    | 888.6      | 166245.4     | 902.4      |
| 1 40                    | 186149.7     | 1079.6     | 185440.1    | 1097.0     | 184716.5     | 1114.1     |
| 2 00                    | 223377.9     | 1554.6     | 222526.4    | 1579.7     | 221658.0     | 1604.3     |
| 2 30                    | 279218.6     | 2429.1     | 278154.1    | 2468.3     | 277068.4     | 2506.8     |
| 3 00                    | 335056.8     | 3497.9     | 333779.1    | 3554.4     | 332476.1     | 3609.8     |
| 3 30                    | 390892.0     | 4761.1     | 389401.1    | 4837.9     | 387880.6     | 4913.3     |
| 4 00                    | 446723.4     | 6218.5     | 445019.2    | 6318.9     | 443281.1     | 6417.4     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of $Z$ . | Lat. $25^{\circ} 0'$ |            | Lat. $25^{\circ} 30'$ |            | Lat. $26^{\circ} 0'$ |            |
|----------------------------|----------------------|------------|-----------------------|------------|----------------------|------------|
|                            | $\delta m$           | $\delta p$ | $\delta m$            | $\delta p$ | $\delta m$           | $\delta p$ |
| 1'                         | 1839.8               | 0.1        | 1832.3                | 0.1        | 1824.7               | 0.1        |
| 2                          | 3679.6               | 0.5        | 3664.6                | 0.5        | 3649.3               | 0.5        |
| 3                          | 5519.5               | 1.0        | 5496.9                | 1.0        | 5474.0               | 1.0        |
| 4                          | 7359.3               | 1.8        | 7329.2                | 1.8        | 7298.6               | 1.9        |
| 5                          | 9199.1               | 2.8        | 9161.5                | 2.9        | 9123.3               | 2.9        |
| 6                          | 11038.9              | 4.1        | 10993.8               | 4.1        | 10947.9              | 4.2        |
| 7                          | 12878.8              | 5.5        | 12826.1               | 5.6        | 12772.6              | 5.7        |
| 8                          | 14718.6              | 7.2        | 14658.5               | 7.3        | 14597.2              | 7.4        |
| 9                          | 16558.4              | 9.2        | 16490.8               | 9.3        | 16421.9              | 9.4        |
| 10                         | 18398.2              | 11.3       | 18323.1               | 11.5       | 18246.5              | 11.6       |
| 11                         | 20238.0              | 13.7       | 20155.4               | 13.9       | 20071.2              | 14.1       |
| 12                         | 22077.9              | 16.3       | 21987.7               | 16.5       | 21895.8              | 16.8       |
| 13                         | 23917.7              | 19.1       | 23820.0               | 19.4       | 23740.5              | 19.7       |
| 14                         | 25757.5              | 22.2       | 25652.3               | 22.5       | 25545.1              | 22.8       |
| 15                         | 27597.3              | 25.4       | 27484.6               | 25.8       | 27369.8              | 26.2       |
| 16                         | 29437.1              | 29.0       | 29316.9               | 29.4       | 29194.4              | 29.8       |
| 17                         | 31277.0              | 32.7       | 31149.2               | 33.2       | 31019.1              | 33.6       |
| 18                         | 33116.8              | 36.6       | 32981.5               | 37.2       | 32843.7              | 37.7       |
| 19                         | 34956.6              | 40.8       | 34813.8               | 41.4       | 34668.4              | 42.0       |
| 20                         | 36796.4              | 45.2       | 36646.1               | 45.9       | 36493.0              | 46.5       |
| 25                         | 45995.5              | 70.7       | 45807.6               | 71.7       | 45616.2              | 72.7       |
| 30                         | 55194.6              | 101.8      | 54969.1               | 103.2      | 54739.5              | 104.7      |
| 40                         | 73592.7              | 180.9      | 73292.0               | 183.6      | 72985.8              | 186.1      |
| 50                         | 91990.7              | 282.7      | 91614.9               | 286.8      | 91232.1              | 290.8      |
| 1° 00                      | 110388.6             | 407.1      | 109827.6              | 413.0      | 109478.3             | 418.8      |
| 1 20                       | 147184.0             | 723.8      | 146582.7              | 734.3      | 145970.3             | 744.6      |
| 1 30                       | 165581.5             | 916.0      | 164905.0              | 929.3      | 164216.0             | 942.3      |
| 1 40                       | 183978.8             | 1130.9     | 183227.1              | 1147.3     | 182461.5             | 1163.4     |
| 2 00                       | 220772.7             | 1628.5     | 219870.6              | 1652.1     | 218951.9             | 1675.2     |
| 2 30                       | 275961.6             | 2544.5     | 274823.9              | 2581.4     | 273685.3             | 2617.6     |
| 3 00                       | 331147.8             | 3664.1     | 329794.3              | 3717.3     | 328415.8             | 3769.3     |
| 3 30                       | 386330.6             | 4987.2     | 384761.3              | 5059.6     | 383142.7             | 5130.5     |
| 4 00                       | 441509.4             | 6512.9     | 439704.0              | 6608.5     | 437865.3             | 6701.0     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 26° 30' |            | Lat. 27° 0' |            | Lat. 27° 30' |            |
|-------------------------|--------------|------------|-------------|------------|--------------|------------|
|                         | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ |
| 1'                      | 1816.9       | 0.1        | 1808.9      | 0.1        | 1800.9       | 0.1        |
| 2                       | 3633.7       | 0.5        | 3617.9      | 0.5        | 3601.7       | 0.5        |
| 3                       | 5450.6       | 1.1        | 5426.8      | 1.1        | 5402.6       | 1.1        |
| 4                       | 7267.4       | 1.9        | 7235.7      | 1.9        | 7203.4       | 1.9        |
| 5                       | 9084.3       | 2.9        | 9044.6      | 3.0        | 9004.3       | 3.0        |
| 6                       | 10901.2      | 4.2        | 10853.6     | 4.3        | 10805.1      | 4.4        |
| 7                       | 12718.0      | 5.8        | 12662.5     | 5.9        | 12606.0      | 5.9        |
| 8                       | 14534.9      | 7.5        | 14471.4     | 7.6        | 14406.9      | 7.7        |
| 9                       | 16351.7      | 9.5        | 16280.3     | 9.7        | 16207.7      | 9.8        |
| 10                      | 18168.6      | 11.8       | 18089.3     | 11.9       | 18008.6      | 12.1       |
| 11                      | 19985.5      | 14.3       | 19898.2     | 14.5       | 19809.4      | 14.6       |
| 12                      | 21802.3      | 17.0       | 21707.1     | 17.2       | 21610.3      | 17.4       |
| 13                      | 23619.2      | 19.9       | 23516.0     | 20.2       | 23411.1      | 20.4       |
| 14                      | 25436.0      | 23.1       | 25325.0     | 23.4       | 25212.0      | 23.7       |
| 15                      | 27252.9      | 26.5       | 27133.9     | 26.9       | 27012.8      | 27.2       |
| 16                      | 29069.8      | 30.2       | 28942.8     | 30.6       | 28813.7      | 30.9       |
| 17                      | 30886.6      | 34.1       | 30751.7     | 34.5       | 30614.6      | 34.9       |
| 18                      | 32703.5      | 38.2       | 32560.7     | 38.7       | 32415.4      | 39.2       |
| 19                      | 34520.3      | 42.6       | 34369.6     | 43.1       | 34216.3      | 43.6       |
| 20                      | 36337.2      | 47.2       | 36178.5     | 47.8       | 36017.1      | 48.4       |
| 25                      | 45421.4      | 73.7       | 45223.1     | 74.7       | 45021.4      | 75.6       |
| 30                      | 54505.6      | 106.1      | 54267.7     | 107.5      | 54025.6      | 108.8      |
| 40                      | 72674.1      | 188.6      | 72356.8     | 191.1      | 72034.0      | 193.5      |
| 50                      | 90842.4      | 294.8      | 90445.8     | 298.6      | 90042.4      | 302.4      |
| 1° 00                   | 109010.7     | 424.5      | 108534.8    | 430.0      | 108050.6     | 435.4      |
| 1 20                    | 145346.7     | 754.6      | 144712.1    | 764.4      | 144066.5     | 774.0      |
| 1 30                    | 163514.5     | 955.1      | 162800.5    | 967.5      | 162074.2     | 979.6      |
| 1 40                    | 181682.0     | 1179.1     | 180888.7    | 1194.4     | 180081.7     | 1209.4     |
| 2 00                    | 218016.4     | 1697.9     | 217064.4    | 1720.0     | 216095.9     | 1741.6     |
| 2 30                    | 272515.9     | 2652.9     | 271325.7    | 2687.5     | 270114.9     | 2721.2     |
| 3 00                    | 327012.2     | 3820.2     | 325583.8    | 3870.0     | 324130.7     | 3918.6     |
| 3 30                    | 381505.0     | 5199.8     | 379838.2    | 5267.5     | 378142.5     | 5333.6     |
| 4 00                    | 435993.2     | 6791.5     | 434088.0    | 6880.0     | 432149.7     | 6966.3     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 28° 0' |            | Lat. 28° 30' |            | Lat. 29°.  |            |
|-------------------------|-------------|------------|--------------|------------|------------|------------|
|                         | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ | $\delta m$ | $\delta p$ |
| 1'                      | 1792.7      | 0.1        | 1784.3       | 0.1        | 1775.8     | 0.1        |
| 2                       | 3585.3      | 0.5        | 3568.6       | 0.5        | 3551.7     | 0.5        |
| 3                       | 5378.0      | 1.1        | 5352.9       | 1.1        | 5327.5     | 1.1        |
| 4                       | 7170.6      | 2.0        | 7137.2       | 2.0        | 7103.3     | 2.0        |
| 5                       | 8963.3      | 3.1        | 8921.5       | 3.1        | 8879.1     | 3.1        |
| 6                       | 10755.9     | 4.4        | 10705.8      | 4.5        | 10655.0    | 4.5        |
| 7                       | 12548.6     | 6.0        | 12490.2      | 6.1        | 12430.8    | 6.1        |
| 8                       | 14341.2     | 7.8        | 14274.5      | 7.9        | 14206.6    | 8.0        |
| 9                       | 16133.9     | 9.9        | 16058.8      | 10.0       | 15982.5    | 10.1       |
| 10                      | 17926.5     | 12.2       | 17843.1      | 12.4       | 17758.3    | 12.5       |
| 11                      | 19719.2     | 14.8       | 19627.4      | 15.0       | 19534.1    | 15.2       |
| 12                      | 21511.8     | 17.6       | 21411.7      | 17.8       | 21309.9    | 18.0       |
| 13                      | 23304.5     | 20.7       | 23196.0      | 20.9       | 23085.8    | 21.2       |
| 14                      | 25097.1     | 24.0       | 24980.3      | 24.3       | 24861.6    | 24.5       |
| 15                      | 26889.8     | 27.5       | 26764.6      | 27.9       | 26637.4    | 28.2       |
| 16                      | 28682.4     | 31.3       | 28548.9      | 31.7       | 28413.2    | 32.1       |
| 17                      | 30475.1     | 35.4       | 30333.2      | 35.8       | 30189.1    | 36.2       |
| 18                      | 32267.7     | 39.7       | 32117.2      | 40.1       | 31964.9    | 40.6       |
| 19                      | 34060.3     | 44.2       | 33901.8      | 44.7       | 33740.7    | 45.2       |
| 20                      | 35853.0     | 49.0       | 35686.1      | 49.5       | 35516.6    | 50.1       |
| 25                      | 44816.2     | 76.5       | 44607.6      | 78.4       | 44395.7    | 78.3       |
| 30                      | 53779.4     | 110.1      | 53529.1      | 111.4      | 53274.8    | 112.7      |
| 40                      | 71705.8     | 195.8      | 71372.1      | 198.1      | 71032.9    | 200.3      |
| 50                      | 89632.0     | 306.0      | 89214.9      | 309.6      | 88790.9    | 313.0      |
| 1° 00                   | 107558.2    | 440.7      | 107057.6     | 445.8      | 106548.8   | 450.8      |
| 1 20                    | 143410.0    | 783.4      | 142742.5     | 792.5      | 142064.1   | 801.4      |
| 1 30                    | 161335.6    | 991.5      | 160584.6     | 1003.0     | 159821.5   | 1014.3     |
| 1 40                    | 179260.9    | 1224.2     | 178426.5     | 1238.3     | 177578.6   | 1252.2     |
| 2 00                    | 215110.9    | 1762.6     | 214109.6     | 1783.2     | 213092.0   | 1803.1     |
| 2 30                    | 268883.6    | 2754.1     | 267631.8     | 2786.2     | 266359.6   | 2817.4     |
| 3 00                    | 322652.8    | 3965.9     | 321150.5     | 4012.1     | 319623.7   | 4057.1     |
| 3 30                    | 376418.1    | 5398.1     | 374665.0     | 5460.9     | 372883.4   | 5522.1     |
| 4 00                    | 430178.5    | 7050.6     | 428174.6     | 7132.7     | 426138.2   | 7212.6     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 29° 30' |            | Lat. 30° 0' |            | Lat. 30° 30' |            |
|-------------------------|--------------|------------|-------------|------------|--------------|------------|
|                         | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ |
| 1'                      | 1767.2       | 0.1        | 1758.5      | 0.1        | 1749.6       | 0.1        |
| 2                       | 3534.4       | 0.5        | 3516.9      | 0.5        | 3499.2       | 0.5        |
| 3                       | 5301.6       | 1.1        | 5275.4      | 1.2        | 5248.8       | 1.2        |
| 4                       | 7068.9       | 2.0        | 7032.9      | 2.0        | 6998.3       | 2.1        |
| 5                       | 8836.1       | 3.2        | 8792.3      | 3.2        | 8747.9       | 3.2        |
| 6                       | 10603.3      | 4.6        | 10550.8     | 4.6        | 10497.5      | 4.6        |
| 7                       | 12370.5      | 6.2        | 12309.3     | 6.3        | 12247.1      | 6.3        |
| 8                       | 14137.7      | 8.1        | 14067.8     | 8.2        | 13996.7      | 8.2        |
| 9                       | 15904.9      | 10.3       | 15826.2     | 10.4       | 15746.3      | 10.5       |
| 10                      | 17672.7      | 12.7       | 17584.7     | 12.8       | 17495.9      | 12.9       |
| 11                      | 19439.4      | 15.3       | 19343.1     | 15.5       | 19245.4      | 15.6       |
| 12                      | 21206.6      | 18.2       | 21101.6     | 18.4       | 20995.0      | 18.6       |
| 13                      | 22973.8      | 21.4       | 22860.1     | 21.6       | 22744.6      | 21.8       |
| 14                      | 24741.0      | 24.8       | 24618.5     | 25.1       | 23494.2      | 25.3       |
| 15                      | 26508.2      | 28.5       | 26377.0     | 28.8       | 25243.8      | 29.1       |
| 16                      | 28275.4      | 32.4       | 28135.5     | 32.7       | 26993.3      | 33.1       |
| 17                      | 30042.6      | 36.6       | 29893.9     | 37.0       | 28742.9      | 37.4       |
| 18                      | 31809.9      | 41.0       | 31652.4     | 41.4       | 30492.5      | 41.8       |
| 19                      | 33577.1      | 45.7       | 33410.9     | 46.2       | 32242.1      | 46.6       |
| 20                      | 35344.3      | 51.6       | 35169.3     | 51.2       | 33991.7      | 51.7       |
| 25                      | 44180.3      | 79.1       | 43961.6     | 79.9       | 43239.6      | 80.7       |
| 30                      | 53016.4      | 113.9      | 52753.9     | 115.1      | 52487.4      | 116.3      |
| 40                      | 70688.4      | 202.5      | 70338.4     | 204.6      | 69983.1      | 206.6      |
| 50                      | 88360.2      | 316.4      | 87922.8     | 319.7      | 87478.7      | 322.9      |
| 1° 00                   | 106032.0     | 455.6      | 105507.1    | 460.4      | 104974.1     | 464.9      |
| 1 20                    | 141375.0     | 810.0      | 140675.1    | 818.4      | 139964.4     | 826.6      |
| 1 30                    | 159046.2     | 1025.2     | 158258.7    | 1035.8     | 157459.2     | 1046.1     |
| 1 40                    | 176717.1     | 1265.7     | 175842.2    | 1278.8     | 174953.8     | 1291.5     |
| 2 00                    | 212058.1     | 1822.6     | 211008.1    | 1841.5     | 209942.1     | 1859.8     |
| 2 30                    | 265067.1     | 2847.8     | 263754.5    | 2877.3     | 262421.8     | 2905.9     |
| 3 00                    | 318072.5     | 4100.8     | 316497.1    | 4143.3     | 314897.6     | 4184.5     |
| 3 30                    | 371073.4     | 5581.7     | 369235.2    | 5639.5     | 367368.9     | 5695.6     |
| 4 00                    | 424069.3     | 7290.3     | 421968.0    | 7365.9     | 419834.7     | 7439.1     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. $31^{\circ} 0'$ . |            | Lat. $31^{\circ} 30'$ |            | Lat. $32^{\circ} 0'$ |            |
|-------------------------|------------------------|------------|-----------------------|------------|----------------------|------------|
|                         | $\delta m$             | $\delta p$ | $\delta m$            | $\delta p$ | $\delta m$           | $\delta p$ |
| 1'                      | 1740.6                 | 0.1        | 1731.4                | 0.1        | 1722.1               | 0.1        |
| 2                       | 3481.1                 | 0.5        | 3462.8                | 0.5        | 3444.3               | 0.5        |
| 3                       | 5221.7                 | 1.2        | 5194.3                | 1.2        | 5166.4               | 1.2        |
| 4                       | 6962.3                 | 2.1        | 6925.7                | 2.1        | 6888.6               | 2.1        |
| 5                       | 8702.9                 | 3.3        | 8657.1                | 3.3        | 8610.7               | 3.3        |
| 6                       | 10443.4                | 4.7        | 10388.5               | 4.7        | 10332.8              | 4.8        |
| 7                       | 12184.0                | 6.4        | 12119.9               | 6.4        | 12055.0              | 6.5        |
| 8                       | 13924.6                | 8.3        | 13851.4               | 8.4        | 13777.1              | 8.5        |
| 9                       | 15665.1                | 10.6       | 15582.8               | 10.7       | 15499.3              | 10.8       |
| 10                      | 17405.7                | 13.0       | 17314.2               | 13.2       | 17221.4              | 13.3       |
| 11                      | 19146.3                | 15.8       | 19045.6               | 15.9       | 18943.6              | 16.1       |
| 12                      | 20886.8                | 18.8       | 20777.1               | 18.9       | 20665.7              | 19.1       |
| 13                      | 22627.4                | 22.0       | 22508.5               | 22.2       | 22387.8              | 22.4       |
| 14                      | 24368.0                | 25.6       | 24239.9               | 25.8       | 24110.0              | 26.0       |
| 15                      | 26108.5                | 29.3       | 25971.3               | 29.6       | 25832.1              | 29.9       |
| 16                      | 27849.1                | 33.4       | 27702.7               | 33.7       | 27554.3              | 34.0       |
| 17                      | 29589.7                | 37.7       | 29434.2               | 38.0       | 29276.4              | 38.4       |
| 18                      | 31330.3                | 42.2       | 31165.6               | 42.6       | 30998.5              | 43.0       |
| 19                      | 33070.8                | 47.1       | 32897.0               | 47.5       | 32720.7              | 47.9       |
| 20                      | 34811.4                | 52.2       | 34628.4               | 52.6       | 34442.8              | 53.1       |
| 25                      | 43514.2                | 81.5       | 43286.0               | 82.3       | 43053.5              | 83.0       |
| 30                      | 52217.0                | 117.3      | 51942.5               | 118.4      | 51664.1              | 119.5      |
| 40                      | 69622.5                | 208.6      | 69256.6               | 210.5      | 68885.4              | 212.4      |
| 50                      | 87027.9                | 326.0      | 86570.5               | 328.9      | 86106.5              | 331.8      |
| 1° 00                   | 104433.2               | 469.4      | 103884.3              | 473.7      | 103327.4             | 477.8      |
| 1 20                    | 139243.1               | 834.5      | 138511.2              | 842.1      | 137768.8             | 849.5      |
| 1 30                    | 156647.8               | 1056.1     | 155824.4              | 1065.8     | 154989.1             | 1075.1     |
| 1 40                    | 174052.2               | 1303.8     | 173137.2              | 1315.8     | 172209.1             | 1327.3     |
| 2 00                    | 208860.0               | 1877.5     | 207762.0              | 1894.7     | 206648.2             | 1911.3     |
| 2 30                    | 261069.1               | 2933.7     | 259696.5              | 2960.5     | 258304.1             | 2986.5     |
| 3 00                    | 313274.2               | 4224.5     | 311626.9              | 4263.1     | 309955.8             | 4300.5     |
| 3 30                    | 365474.6               | 5750.0     | 363552.4              | 5802.6     | 361602.5             | 5853.5     |
| 4 00                    | 417669.4               | 7510.2     | 415472.3              | 7578.9     | 413243.4             | 7645.3     |



*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. $32^{\circ} 30'$ |            | Lat. $33^{\circ} 0'$ |            | Lat. $33^{\circ} 30'$ |        |
|-------------------------|-----------------------|------------|----------------------|------------|-----------------------|--------|
|                         | $\delta m$            | $\delta p$ | $\delta m$           | $\delta p$ | $\delta m$            | $p$    |
| 1'                      | 1712.7                | 0.1        | 1703.2               | 0.1        | 1693.5                | 0.1    |
| 2                       | 3425.5                | 0.5        | 3406.4               | 0.5        | 3387.0                | 0.5    |
| 3                       | 5138.2                | 1.2        | 5109.6               | 1.2        | 5080.6                | 1.2    |
| 4                       | 6850.9                | 2.1        | 6812.8               | 2.2        | 6774.1                | 2.2    |
| 5                       | 8563.7                | 3.3        | 8515.9               | 3.4        | 8467.6                | 3.4    |
| 6                       | 10276.4               | 4.8        | 10219.1              | 4.9        | 10161.1               | 4.9    |
| 7                       | 11989.1               | 6.6        | 11922.3              | 6.6        | 11815.6               | 6.7    |
| 8                       | 13701.8               | 8.6        | 13625.5              | 8.6        | 13548.1               | 8.7    |
| 9                       | 15414.6               | 10.8       | 15328.7              | 10.9       | 15241.7               | 11.0   |
| 10                      | 17127.3               | 13.4       | 17031.9              | 13.5       | 16935.2               | 13.6   |
| 11                      | 18840.0               | 16.2       | 18735.1              | 16.3       | 18628.7               | 16.4   |
| 12                      | 20552.8               | 19.3       | 20438.3              | 19.4       | 20322.2               | 19.6   |
| 13                      | 22265.5               | 22.6       | 22141.4              | 22.8       | 22015.7               | 23.0   |
| 14                      | 23978.2               | 26.2       | 23844.6              | 26.4       | 23709.2               | 26.6   |
| 15                      | 25690.9               | 30.1       | 25547.8              | 30.4       | 25402.7               | 30.6   |
| 16                      | 27403.7               | 34.3       | 27251.0              | 34.5       | 27096.3               | 34.9   |
| 17                      | 29116.4               | 38.7       | 28954.2              | 39.0       | 28789.8               | 39.3   |
| 18                      | 30829.1               | 43.4       | 30657.4              | 43.7       | 30483.3               | 44.0   |
| 19                      | 32541.9               | 48.5       | 32360.6              | 49.0       | 32176.8               | 49.1   |
| 20                      | 34254.6               | 53.5       | 34063.8              | 54.0       | 33870.3               | 54.4   |
| 25                      | 42818.2               | 83.6       | 42579.6              | 84.3       | 42337.9               | 85.0   |
| 30                      | 51381.8               | 120.5      | 51095.5              | 121.4      | 50805.4               | 122.3  |
| 40                      | 68508.9               | 214.1      | 68127.2              | 215.9      | 67740.4               | 217.5  |
| 50                      | 85635.9               | 334.6      | 85158.8              | 337.3      | 84675.2               | 339.9  |
| 1° 00                   | 102762.7              | 481.8      | 102190.2             | 485.7      | 101609.9              | 489.4  |
| 1 20                    | 137015.8              | 856.6      | 136252.4             | 863.5      | 135478.6              | 870.1  |
| 1 30                    | 154142.0              | 1084.1     | 153283.1             | 1092.8     | 152412.6              | 1101.2 |
| 1 40                    | 171267.0              | 1338.4     | 170313.6             | 1349.2     | 169346.3              | 1359.5 |
| 2 00                    | 205518.7              | 1927.4     | 204373.5             | 1942.8     | 203212.7              | 1957.7 |
| 2 30                    | 256892.0              | 3011.5     | 255460.4             | 3035.6     | 254009.2              | 3058.8 |
| 3 00                    | 308261.1              | 4336.6     | 306542.9             | 4371.3     | 304801.4              | 4404.7 |
| 3 30                    | 359625.1              | 5902.6     | 357620.3             | 5949.9     | 355588.2              | 5995.3 |
| 4 00                    | 410983.2              | 7709.5     | 408691.6             | 7771.2     | 406368.8              | 7830.6 |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 34° 0' |            | Lat. 34° 30' |            | Lat. 35° 0' |            |
|-------------------------|-------------|------------|--------------|------------|-------------|------------|
|                         | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ |
| 1'                      | 1683.7      | 0.1        | 1673.8       | 0.1        | 1663.7      | 0.1        |
| 2                       | 3367.4      | 0.5        | 3347.6       | 0.6        | 3327.5      | 0.6        |
| 3                       | 5051.1      | 1.2        | 5021.4       | 1.2        | 4991.2      | 1.2        |
| 4                       | 6734.9      | 2.2        | 6695.1       | 2.2        | 6654.9      | 2.2        |
| 5                       | 8418.6      | 3.4        | 8368.9       | 3.4        | 8318.7      | 3.5        |
| 6                       | 10102.3     | 4.9        | 10042.7      | 5.0        | 9982.4      | 5.0        |
| 7                       | 11786.0     | 6.7        | 11716.5      | 6.8        | 11646.1     | 6.8        |
| 8                       | 13469.7     | 8.8        | 13390.3      | 8.8        | 13309.8     | 8.9        |
| 9                       | 15153.4     | 11.1       | 15064.1      | 11.2       | 14973.6     | 11.2       |
| 10                      | 16837.2     | 13.7       | 16737.9      | 13.8       | 16637.3     | 13.9       |
| 11                      | 18520.9     | 16.6       | 18411.6      | 16.7       | 18301.0     | 16.8       |
| 12                      | 20204.6     | 19.7       | 20085.4      | 19.9       | 19964.8     | 20.0       |
| 13                      | 21888.3     | 23.1       | 21759.2      | 23.3       | 21628.5     | 23.5       |
| 14                      | 23572.0     | 26.8       | 23433.0      | 27.0       | 23292.2     | 27.2       |
| 15                      | 25255.7     | 30.8       | 25106.8      | 31.0       | 24955.9     | 31.2       |
| 16                      | 26939.4     | 35.1       | 26780.6      | 35.3       | 26619.7     | 35.5       |
| 17                      | 28623.1     | 39.6       | 28454.4      | 39.8       | 28283.4     | 40.1       |
| 18                      | 30306.9     | 44.4       | 30128.1      | 44.7       | 29947.1     | 45.0       |
| 19                      | 31990.6     | 49.4       | 31801.9      | 49.8       | 31610.9     | 50.1       |
| 20                      | 33674.3     | 54.8       | 33475.7      | 55.2       | 33274.6     | 55.5       |
| 25                      | 42092.8     | 85.6       | 41844.6      | 86.2       | 41593.2     | 86.7       |
| 30                      | 50511.4     | 123.2      | 50213.5      | 125.1      | 49911.8     | 124.9      |
| 40                      | 67348.3     | 219.1      | 66951.1      | 220.6      | 65548.9     | 222.1      |
| 50                      | 84185.1     | 342.3      | 83688.7      | 344.7      | 83185.8     | 347.0      |
| 1° 00                   | 101021.8    | 493.0      | 100426.0     | 496.4      | 99822.6     | 499.7      |
| 1 20                    | 134694.5    | 876.4      | 133900.1     | 882.5      | 133095.5    | 883.3      |
| 1 30                    | 151530.5    | 1109.2     | 150636.8     | 1116.9     | 149731.5    | 1124.2     |
| 1 40                    | 168366.1    | 1369.4     | 167373.1     | 1378.9     | 166367.3    | 1387.9     |
| 2 00                    | 202036.4    | 1971.9     | 200844.7     | 1985.6     | 199637.8    | 1998.6     |
| 2 30                    | 252538.7    | 3081.1     | 251049.0     | 3102.5     | 249540.1    | 3122.8     |
| 3 00                    | 303036.6    | 4436.8     | 301248.7     | 4467.5     | 299437.8    | 4496.9     |
| 3 30                    | 353529.0    | 6039.0     | 351442.8     | 6080.8     | 349329.8    | 6120.8     |
| 4 00                    | 404015.1    | 7887.7     | 401630.5     | 7942.3     | 399215.4    | 7994.5     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 35° 30' |            | Lat. 36° 0' |            | Lat. 36° 30' |            |
|-------------------------|--------------|------------|-------------|------------|--------------|------------|
|                         | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ |
| 1'                      | 1653.5       | 0.1        | 1643.2      | 0.1        | 1632.8       | 0.1        |
| 2                       | 3307.1       | 0.6        | 3286.5      | 0.6        | 3265.6       | 0.6        |
| 3                       | 4960.6       | 1.3        | 4929.7      | 1.3        | 4898.4       | 1.3        |
| 4                       | 6614.2       | 2.2        | 6572.9      | 2.2        | 6531.2       | 2.3        |
| 5                       | 8267.7       | 3.5        | 8216.2      | 3.5        | 8164.0       | 3.5        |
| 6                       | 9921.3       | 5.0        | 9859.4      | 5.1        | 9796.8       | 5.1        |
| 7                       | 11574.8      | 6.8        | 11502.7     | 6.9        | 11429.6      | 6.9        |
| 8                       | 13228.4      | 8.9        | 13145.9     | 9.0        | 13062.4      | 9.0        |
| 9                       | 14881.9      | 11.3       | 14789.1     | 11.4       | 14695.2      | 11.4       |
| 10                      | 16535.5      | 14.0       | 16432.4     | 14.0       | 16328.0      | 14.1       |
| 11                      | 18189.0      | 16.9       | 18075.6     | 17.0       | 17960.8      | 17.0       |
| 12                      | 19842.5      | 20.1       | 19718.8     | 20.2       | 19593.6      | 20.3       |
| 13                      | 21496.1      | 23.6       | 21362.0     | 23.7       | 21226.4      | 23.9       |
| 14                      | 23149.6      | 27.4       | 23005.3     | 27.5       | 22859.2      | 27.7       |
| 15                      | 24803.2      | 31.4       | 24648.5     | 31.6       | 24492.0      | 31.8       |
| 16                      | 26456.7      | 35.7       | 26291.8     | 36.0       | 26124.8      | 36.2       |
| 17                      | 28110.3      | 40.4       | 27935.0     | 40.6       | 27757.6      | 40.8       |
| 18                      | 29763.8      | 45.2       | 29578.2     | 45.5       | 29390.4      | 45.8       |
| 19                      | 31417.3      | 50.4       | 31221.2     | 50.7       | 31023.2      | 51.0       |
| 20                      | 33070.9      | 55.9       | 32864.7     | 56.2       | 32656.0      | 56.5       |
| 25                      | 41338.6      | 87.2       | 41080.8     | 87.8       | 40819.9      | 88.3       |
| 30                      | 49606.2      | 125.7      | 49296.9     | 126.4      | 48983.9      | 127.1      |
| 40                      | 66141.5      | 223.4      | 65729.1     | 224.8      | 65311.7      | 226.0      |
| 50                      | 82676.6      | 349.1      | 82161.1     | 351.2      | 81639.3      | 353.1      |
| 1° 00                   | 99211.5      | 502.7      | 98592.9     | 507.7      | 97966.7      | 508.5      |
| 1 20                    | 132280.7     | 893.8      | 131435.9    | 899.1      | 130621.0     | 904.1      |
| 1 30                    | 148814.9     | 1131.2     | 147886.9    | 1137.9     | 146947.7     | 1144.2     |
| 1 40                    | 165348.8     | 1396.6     | 164317.7    | 1404.8     | 163274.0     | 1412.6     |
| 2 00                    | 198415.4     | 2011.1     | 197178.0    | 2022.9     | 195925.6     | 2034.1     |
| 2 30                    | 248012.1     | 3142.3     | 246465.3    | 3160.8     | 244899.6     | 3178.3     |
| 3 00                    | 297604.0     | 4524.9     | 295747.6    | 4551.6     | 293868.6     | 4576.8     |
| 3 30                    | 347190.2     | 6158.9     | 345024.1    | 6195.2     | 342831.7     | 6229.5     |
| 4 00                    | 396769.7     | 8044.3     | 394293.8    | 8091.6     | 391787.8     | 8136.5     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 37° 0' |            | Lat. 37° 30' |            | Lat. 38° 0' |            |
|-------------------------|-------------|------------|--------------|------------|-------------|------------|
|                         | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ |
| 1'                      | 1622.2      | 0.1        | 1611.6       | 0.1        | 1600.7      | 0.1        |
| 2                       | 3244.5      | 0.6        | 3223.1       | 0.6        | 3201.5      | 0.6        |
| 3                       | 4866.7      | 1.3        | 4834.7       | 1.3        | 4802.2      | 1.3        |
| 4                       | 6489.0      | 2.3        | 6446.2       | 2.3        | 6403.0      | 2.3        |
| 5                       | 8111.2      | 3.5        | 8057.8       | 3.6        | 8003.7      | 3.6        |
| 6                       | 9733.4      | 5.1        | 9669.3       | 5.1        | 9604.5      | 5.2        |
| 7                       | 11355.7     | 7.0        | 11280.9      | 7.0        | 11205.2     | 7.0        |
| 8                       | 12977.9     | 9.1        | 12892.4      | 9.1        | 12806.0     | 9.2        |
| 9                       | 14600.2     | 11.5       | 14504.0      | 11.6       | 14406.7     | 11.6       |
| 10                      | 16222.4     | 14.2       | 16115.6      | 14.3       | 16007.5     | 14.3       |
| 11                      | 17844.6     | 17.2       | 17727.1      | 17.3       | 17608.2     | 17.3       |
| 12                      | 19466.9     | 20.4       | 19338.6      | 20.5       | 19209.0     | 20.6       |
| 13                      | 21089.1     | 24.0       | 20950.2      | 24.1       | 20809.7     | 24.2       |
| 14                      | 22711.4     | 27.8       | 22561.8      | 28.0       | 22410.5     | 28.1       |
| 15                      | 24333.6     | 31.9       | 24173.3      | 32.1       | 24011.2     | 32.3       |
| 16                      | 25955.8     | 36.4       | 25784.9      | 36.5       | 25612.0     | 36.7       |
| 17                      | 27578.1     | 41.0       | 27396.4      | 41.2       | 27212.7     | 41.4       |
| 18                      | 29200.3     | 46.0       | 29008.0      | 46.2       | 28813.4     | 46.4       |
| 19                      | 30822.6     | 51.3       | 30619.5      | 51.5       | 30414.2     | 51.7       |
| 20                      | 32444.8     | 56.8       | 32231.1      | 57.1       | 32015.0     | 57.3       |
| 25                      | 40555.9     | 88.7       | 40288.8      | 89.1       | 40018.6     | 89.6       |
| 30                      | 48667.1     | 127.8      | 48346.5      | 128.4      | 48022.3     | 129.0      |
| 40                      | 64889.2     | 227.2      | 64461.9      | 228.3      | 64029.6     | 229.3      |
| 50                      | 81111.3     | 355.0      | 80577.1      | 356.7      | 80036.7     | 358.3      |
| 1° 00                   | 97333.1     | 511.2      | 96692.0      | 513.7      | 96043.6     | 516.0      |
| 1 20                    | 129776.1    | 908.8      | 128921.3     | 913.2      | 128056.7    | 917.4      |
| 1 30                    | 145997.2    | 1150.2     | 145035.5     | 1155.8     | 144062.6    | 1161.0     |
| 1 40                    | 162217.9    | 1419.9     | 161149.4     | 1426.9     | 160068.5    | 1433.4     |
| 2 00                    | 194658.2    | 2044.7     | 193375.9     | 2054.7     | 192078.9    | 2064.1     |
| 2 30                    | 243315.2    | 3194.9     | 241712.2     | 3210.5     | 240090.8    | 3225.1     |
| 3 00                    | 291967.1    | 4600.7     | 290043.4     | 4623.1     | 288097.5    | 4644.1     |
| 3 30                    | 340613.1    | 6262.0     | 338368.4     | 6292.6     | 336098.0    | 6321.2     |
| 4 00                    | 389251.9    | 8178.9     | 386686.3     | 8218.8     | 384091.9    | 8256.3     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 35° 30' |            | Lat. 39° 0' |            | Lat. 39° 30' |            |
|-------------------------|--------------|------------|-------------|------------|--------------|------------|
|                         | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ |
| 1'                      | 1589.8       | 0.1        | 1578.8      | 0.1        | 1567.6       | 0.1        |
| 2                       | 3179.6       | 0.6        | 3157.5      | 0.6        | 3135.2       | 0.6        |
| 3                       | 4769.5       | 1.3        | 4736.3      | 1.3        | 4702.8       | 1.3        |
| 4                       | 6359.3       | 2.3        | 6315.1      | 2.3        | 6270.4       | 2.3        |
| 5                       | 7949.1       | 3.6        | 7893.8      | 3.6        | 7838.0       | 3.6        |
| 6                       | 9538.9       | 5.2        | 9472.6      | 5.2        | 9405.6       | 5.2        |
| 7                       | 11128.7      | 7.1        | 11051.4     | 7.1        | 10973.2      | 7.1        |
| 8                       | 12718.6      | 9.2        | 12630.1     | 9.2        | 12540.8      | 9.3        |
| 9                       | 14308.4      | 11.7       | 14208.9     | 11.7       | 14108.4      | 11.7       |
| 10                      | 15898.2      | 14.4       | 15787.7     | 14.5       | 15676.0      | 14.5       |
| 11                      | 17488.0      | 17.4       | 17366.4     | 17.5       | 17243.6      | 17.5       |
| 12                      | 19077.8      | 20.7       | 18945.2     | 20.8       | 18811.1      | 20.9       |
| 13                      | 20667.6      | 24.3       | 20524.0     | 24.4       | 20378.7      | 24.5       |
| 14                      | 22257.4      | 28.2       | 22102.7     | 28.3       | 21946.3      | 28.4       |
| 15                      | 23847.3      | 32.4       | 23681.5     | 32.5       | 23513.9      | 32.6       |
| 16                      | 25437.1      | 36.8       | 25260.3     | 37.0       | 25081.5      | 37.1       |
| 17                      | 27026.9      | 41.6       | 26839.0     | 41.8       | 26649.1      | 41.9       |
| 18                      | 28616.7      | 46.6       | 28417.8     | 46.8       | 28216.7      | 47.0       |
| 19                      | 30206.5      | 52.0       | 29996.6     | 52.2       | 29784.3      | 52.3       |
| 20                      | 31796.3      | 57.6       | 31575.3     | 57.8       | 31351.9      | 58.0       |
| 25                      | 39745.4      | 90.0       | 39469.1     | 90.3       | 39189.8      | 90.6       |
| 30                      | 47694.4      | 129.5      | 47362.9     | 130.1      | 47027.7      | 130.5      |
| 40                      | 63592.4      | 230.3      | 63150.3     | 231.2      | 62703.4      | 232.0      |
| 50                      | 79490.2      | 359.9      | 78937.6     | 361.3      | 78379.0      | 362.6      |
| 1° 00                   | 95387.8      | 518.2      | 94724.7     | 520.2      | 94054.4      | 522.1      |
| 1 20                    | 127182.3     | 921.2      | 126298.1    | 924.8      | 125404.3     | 928.2      |
| 1 30                    | 143079.0     | 1165.9     | 142084.4    | 1170.5     | 141078.8     | 1174.7     |
| 1 40                    | 158975.5     | 1439.4     | 157870.3    | 1445.1     | 156753.0     | 1450.2     |
| 2 00                    | 190767.1     | 2072.8     | 189440.8    | 2080.9     | 188100.1     | 2088.3     |
| 2 30                    | 238451.0     | 3238.7     | 236793.0    | 3251.4     | 235116.9     | 3263.0     |
| 3 00                    | 286129.6     | 4663.8     | 284139.8    | 4682.0     | 282128.3     | 4698.8     |
| 3 30                    | 333801.8     | 6347.9     | 331480.2    | 6372.7     | 329133.2     | 6395.6     |
| 4 00                    | 381466.7     | 8291.2     | 378813.1    | 8323.6     | 376130.5     | 8353.4     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 40° 0' |            | Lat. 40° 30' |            | Lat. 41° 0' |            |
|-------------------------|-------------|------------|--------------|------------|-------------|------------|
|                         | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ |
| 1'                      | 1556.3      | 0.1        | 1544.9       | 0.1        | 1533.4      | 0.1        |
| 2                       | 3112.6      | 0.6        | 3089.8       | 0.6        | 3066.7      | 0.6        |
| 3                       | 4668.9      | 1.3        | 4634.7       | 1.3        | 4600.1      | 1.3        |
| 4                       | 6225.2      | 2.3        | 6179.6       | 2.3        | 6133.5      | 2.3        |
| 5                       | 7781.5      | 3.6        | 7724.5       | 3.6        | 7666.8      | 3.7        |
| 6                       | 9337.8      | 5.2        | 9269.4       | 5.3        | 9200.2      | 5.3        |
| 7                       | 10894.1     | 7.1        | 10814.3      | 7.2        | 10733.6     | 7.2        |
| 8                       | 12450.4     | 9.3        | 12359.2      | 9.3        | 12266.9     | 9.4        |
| 9                       | 14006.7     | 11.8       | 13904.0      | 11.8       | 13800.3     | 11.9       |
| 10                      | 15563.0     | 14.6       | 15448.9      | 14.6       | 15333.7     | 14.6       |
| 11                      | 17119.3     | 17.6       | 16993.8      | 17.7       | 16867.0     | 17.7       |
| 12                      | 18675.6     | 21.0       | 18538.7      | 21.0       | 18400.4     | 21.4       |
| 13                      | 20231.9     | 24.6       | 20083.6      | 24.7       | 19933.7     | 24.7       |
| 14                      | 21788.2     | 28.5       | 21628.5      | 28.6       | 21467.1     | 28.7       |
| 15                      | 23344.5     | 32.7       | 23173.4      | 32.8       | 23000.4     | 32.9       |
| 16                      | 24900.8     | 37.2       | 24718.3      | 37.4       | 24533.8     | 37.5       |
| 17                      | 26457.1     | 42.0       | 26263.2      | 42.2       | 26067.2     | 42.3       |
| 18                      | 28013.4     | 47.1       | 27808.1      | 47.3       | 27600.5     | 47.4       |
| 19                      | 29569.8     | 52.5       | 29352.9      | 52.7       | 29133.9     | 52.8       |
| 20                      | 31126.1     | 58.2       | 30897.8      | 58.4       | 30667.3     | 58.5       |
| 25                      | 38907.5     | 90.9       | 38632.2      | 91.2       | 38334.0     | 91.4       |
| 30                      | 46689.0     | 130.9      | 46346.7      | 131.3      | 46000.3     | 131.7      |
| 40                      | 62251.8     | 232.8      | 61795.3      | 233.5      | 61334.2     | 234.1      |
| 50                      | 77814.4     | 363.7      | 77243.9      | 364.8      | 76667.4     | 365.8      |
| 1° 00                   | 93376.9     | 523.8      | 92692.2      | 525.3      | 92000.4     | 526.7      |
| 1 20                    | 124500.9    | 931.2      | 123588.0     | 933.9      | 122665.7    | 936.4      |
| 1 30                    | 140062.5    | 1178.5     | 139035.5     | 1182.0     | 137997.8    | 1185.1     |
| 1 40                    | 155623.7    | 1455.0     | 154482.6     | 1459.3     | 153329.6    | 1463.1     |
| 2 00                    | 186744.9    | 2095.2     | 185375.4     | 2101.4     | 183991.8    | 2106.9     |
| 2 30                    | 233422.9    | 3273.7     | 231710.9     | 3283.4     | 229998.3    | 3292.0     |
| 3 00                    | 280095.3    | 4714.1     | 278040.9     | 4728.1     | 275965.1    | 4740.6     |
| 3 30                    | 326761.1    | 6416.5     | 324364.1     | 6435.4     | 321942.2    | 6452.4     |
| 4 00                    | 373419.3    | 8380.7     | 370679.4     | 8405.5     | 367911.3    | 8427.7     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. $41^{\circ} 30'$ |            | Lat. $42^{\circ} 0'$ |            | Lat. $42^{\circ} 30'$ |            |
|-------------------------|-----------------------|------------|----------------------|------------|-----------------------|------------|
|                         | $\delta m$            | $\delta p$ | $\delta m$           | $\delta p$ | $\delta m$            | $\delta p$ |
| 1                       | 1521.7                | 0.1        | 1510.0               | 0.1        | 1498.1                | 0.1        |
| 2                       | 3043.4                | 0.6        | 3019.9               | 0.6        | 2996.2                | 0.6        |
| 3                       | 4565.2                | 1.3        | 4529.9               | 1.3        | 4494.2                | 1.3        |
| 4                       | 6086.9                | 2.3        | 6039.8               | 2.4        | 5992.3                | 2.4        |
| 5                       | 7608.6                | 3.7        | 7549.8               | 3.7        | 7490.4                | 3.7        |
| 6                       | 9130.3                | 5.3        | 9059.7               | 5.3        | 8988.6                | 5.3        |
| 7                       | 10652.0               | 7.2        | 10569.7              | 7.2        | 10486.5               | 7.2        |
| 8                       | 12173.8               | 9.4        | 12079.6              | 9.4        | 11984.6               | 9.4        |
| 9                       | 13695.5               | 11.9       | 13589.6              | 11.9       | 13482.7               | 11.9       |
| 10                      | 15217.2               | 14.7       | 15099.6              | 14.7       | 14980.8               | 14.7       |
| 11                      | 16738.9               | 17.7       | 16609.5              | 17.8       | 16478.8               | 17.8       |
| 12                      | 18260.6               | 21.1       | 18119.5              | 21.2       | 17976.9               | 21.2       |
| 13                      | 19782.3               | 24.8       | 19629.4              | 24.8       | 19475.0               | 24.9       |
| 14                      | 21304.0               | 28.7       | 21139.4              | 28.8       | 20973.1               | 28.8       |
| 15                      | 22825.8               | 33.0       | 22649.3              | 33.1       | 22471.1               | 33.1       |
| 16                      | 24347.5               | 37.5       | 24159.3              | 37.6       | 23969.2               | 37.6       |
| 17                      | 25869.2               | 42.4       | 25669.2              | 42.5       | 25467.3               | 42.5       |
| 18                      | 27390.9               | 47.5       | 27179.2              | 47.6       | 26965.4               | 47.7       |
| 19                      | 28912.6               | 52.9       | 28689.1              | 53.0       | 28463.4               | 53.1       |
| 20                      | 30434.3               | 58.6       | 30199.1              | 58.8       | 29961.5               | 58.9       |
| 25                      | 38042.9               | 91.6       | 37748.8              | 91.8       | 37451.3               | 92.0       |
| 30                      | 45651.4               | 132.0      | 45298.5              | 132.3      | 44942.2               | 132.5      |
| 40                      | 60868.3               | 234.6      | 60397.8              | 235.1      | 59922.7               | 235.5      |
| 50                      | 76085.1               | 366.6      | 75496.9              | 367.4      | 74903.0               | 368.0      |
| 1° 00                   | 91301.6               | 527.9      | 90595.9              | 529.0      | 89883.2               | 529.9      |
| 1 20                    | 121733.9              | 938.6      | 120792.9             | 940.5      | 119842.6              | 942.1      |
| 1 30                    | 136949.6              | 1187.9     | 135890.9             | 1190.3     | 134821.8              | 1192.3     |
| 1 40                    | 152164.9              | 1466.5     | 150988.5             | 1469.5     | 149800.6              | 1472.0     |
| 2 00                    | 182594.1              | 2111.8     | 181182.5             | 2116.1     | 179756.9              | 2119.7     |
| 2 30                    | 228234.1              | 3299.7     | 226469.4             | 3306.4     | 224687.4              | 3312.0     |
| 3 00                    | 273868.3              | 4751.6     | 271750.5             | 4761.2     | 269612.0              | 4769.3     |
| 3 30                    | 319495.6              | 6467.5     | 317024.7             | 6480.5     | 314529.5              | 6491.6     |
| 4 00                    | 365115.0              | 8447.3     | 362290.8             | 8464.4     | 359438.9              | 8478.8     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 43° 0' |            | Lat. 43° 30' |            | Lat. 44° 0' |            |
|-------------------------|-------------|------------|--------------|------------|-------------|------------|
|                         | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ |
| 1'                      | 1486.1      | 0.1        | 1474.0       | 0.1        | 1461.8      | 0.1        |
| 2                       | 2972.2      | 0.6        | 2948.0       | 0.6        | 2923.5      | 0.6        |
| 3                       | 4458.3      | 1.3        | 4421.9       | 1.3        | 4385.3      | 1.3        |
| 4                       | 5944.3      | 2.4        | 5895.9       | 2.4        | 5847.0      | 2.4        |
| 5                       | 7430.4      | 3.7        | 7369.9       | 3.7        | 7308.8      | 3.7        |
| 6                       | 8916.5      | 5.3        | 8843.9       | 5.3        | 8770.5      | 5.3        |
| 7                       | 10402.6     | 7.2        | 10317.8      | 7.2        | 10232.3     | 7.2        |
| 8                       | 11888.7     | 9.4        | 11791.8      | 9.5        | 11694.1     | 9.5        |
| 9                       | 13374.8     | 11.9       | 13265.8      | 12.0       | 13155.8     | 12.0       |
| 10                      | 14860.8     | 14.7       | 14739.8      | 14.8       | 14617.6     | 14.8       |
| 11                      | 16346.9     | 17.8       | 16213.7      | 17.8       | 16079.3     | 17.9       |
| 12                      | 17833.0     | 21.2       | 17687.7      | 21.2       | 17541.1     | 21.3       |
| 13                      | 19319.1     | 24.9       | 19161.7      | 24.9       | 19002.8     | 25.0       |
| 14                      | 20805.2     | 28.9       | 20635.7      | 28.9       | 20464.6     | 28.9       |
| 15                      | 22291.2     | 33.2       | 22109.6      | 33.2       | 21926.3     | 33.2       |
| 16                      | 23777.3     | 37.7       | 23583.6      | 37.8       | 23386.1     | 37.8       |
| 17                      | 25263.4     | 42.6       | 25057.6      | 42.6       | 24849.9     | 42.7       |
| 18                      | 26749.5     | 47.8       | 26531.6      | 47.8       | 26311.6     | 47.9       |
| 19                      | 28235.6     | 53.2       | 28005.5      | 53.3       | 27773.4     | 53.3       |
| 20                      | 29721.7     | 59.0       | 29479.5      | 59.0       | 29235.1     | 59.1       |
| 25                      | 37102.0     | 92.1       | 36849.3      | 92.2       | 36543.8     | 92.3       |
| 30                      | 44582.4     | 132.7      | 44219.2      | 132.8      | 43852.6     | 132.9      |
| 40                      | 59443.0     | 235.8      | 58958.7      | 236.1      | 58469.9     | 236.3      |
| 50                      | 74303.4     | 368.5      | 73698.0      | 368.9      | 73087.0     | 369.2      |
| 1° 00                   | 89163.6     | 530.7      | 88437.1      | 531.2      | 87703.9     | 531.7      |
| 1 20                    | 118883.1    | 943.4      | 117914.5     | 944.4      | 116936.9    | 945.2      |
| 1 30                    | 133742.4    | 1194.0     | 132652.7     | 1195.3     | 131552.9    | 1196.3     |
| 1 40                    | 148601.2    | 1474.1     | 147390.5     | 1475.7     | 146168.4    | 1476.9     |
| 2 00                    | 178317.6    | 2123.7     | 176864.7     | 2125.0     | 175398.2    | 2126.7     |
| 2 30                    | 222888.2    | 3316.7     | 221071.9     | 3320.3     | 219238.7    | 3323.0     |
| 3 00                    | 267452.8    | 4776.0     | 265273.1     | 4781.3     | 263073.1    | 4785.1     |
| 3 30                    | 312010.3    | 6500.7     | 309467.1     | 6507.9     | 306900.3    | 6513.0     |
| 4 00                    | 356559.5    | 8490.7     | 353652.8     | 8500.1     | 350719.0    | 8506.8     |



*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 44° 30' |            | Lat. 45° 0' |            | Lat. 45° 30' |            |
|-------------------------|--------------|------------|-------------|------------|--------------|------------|
|                         | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ |
| 1'                      | 1449.4       | 0.1        | 1437.0      | 0.1        | 1424.4       | 0.1        |
| 2                       | 2898.9       | 0.6        | 2874.0      | 0.6        | 2848.9       | 0.6        |
| 3                       | 4348.3       | 1.3        | 4311.0      | 1.3        | 4273.3       | 1.3        |
| 4                       | 5797.7       | 2.4        | 5747.9      | 2.4        | 5697.7       | 2.4        |
| 5                       | 7247.1       | 3.7        | 7184.9      | 3.7        | 7122.2       | 3.7        |
| 6                       | 8696.6       | 5.3        | 8621.9      | 5.3        | 8546.6       | 5.3        |
| 7                       | 10146.0      | 7.2        | 10058.9     | 7.2        | 9971.0       | 7.2        |
| 8                       | 11595.4      | 9.5        | 11495.9     | 9.5        | 11395.4      | 9.5        |
| 9                       | 13044.8      | 12.0       | 12932.9     | 12.0       | 12819.9      | 12.0       |
| 10                      | 14494.3      | 14.8       | 14369.8     | 14.8       | 14244.3      | 14.8       |
| 11                      | 15943.7      | 17.9       | 15806.8     | 17.9       | 15668.7      | 17.9       |
| 12                      | 17393.1      | 21.3       | 17243.8     | 21.3       | 17093.1      | 21.3       |
| 13                      | 18842.5      | 25.0       | 18680.8     | 25.0       | 18517.6      | 25.0       |
| 14                      | 20292.0      | 29.0       | 20117.7     | 29.0       | 19942.0      | 29.0       |
| 15                      | 21741.4      | 33.2       | 21554.7     | 33.3       | 21366.4      | 33.2       |
| 16                      | 23190.8      | 37.8       | 22991.7     | 37.8       | 22790.8      | 37.8       |
| 17                      | 24640.2      | 42.7       | 24428.7     | 42.7       | 24215.3      | 42.7       |
| 18                      | 26089.7      | 47.9       | 25865.7     | 47.9       | 25639.7      | 47.9       |
| 19                      | 27539.1      | 53.3       | 27302.7     | 53.4       | 27064.1      | 53.3       |
| 20                      | 28988.5      | 59.1       | 28739.6     | 59.1       | 28488.6      | 59.1       |
| 25                      | 36235.6      | 92.3       | 35924.5     | 92.4       | 35610.6      | 92.3       |
| 30                      | 43482.6      | 133.0      | 43109.3     | 133.0      | 42732.7      | 133.0      |
| 40                      | 57976.6      | 236.4      | 57478.9     | 236.5      | 56976.8      | 236.4      |
| 50                      | 72470.4      | 369.4      | 71848.3     | 369.5      | 71220.6      | 369.4      |
| 1° 00                   | 86964.0      | 531.9      | 86217.4     | 532.0      | 85464.2      | 532.0      |
| 1 20                    | 115950.3     | 945.7      | 114954.9    | 945.8      | 113950.6     | 945.7      |
| 1 30                    | 130442.9     | 1196.8     | 129323.0    | 1197.1     | 128193.2     | 1196.9     |
| 1 40                    | 144935.2     | 1477.6     | 143690.8    | 1477.9     | 142435.5     | 1477.7     |
| 2 00                    | 173918.3     | 2127.7     | 172425.0    | 2128.1     | 170918.5     | 2127.8     |
| 2 30                    | 217388.7     | 3324.6     | 215522.0    | 3325.2     | 213638.8     | 3324.8     |
| 3 00                    | 260853.0     | 4787.4     | 258612.9    | 4788.3     | 256352.9     | 4787.7     |
| 3 30                    | 304310.0     | 6516.2     | 301896.3    | 6517.3     | 299059.6     | 6516.5     |
| 4 00                    | 347758.4     | 8510.9     | 344771.2    | 8512.5     | 341757.6     | 8511.4     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 46° 0' |            | Lat. 46° 30' |            | Lat. 47° 0' |            |
|-------------------------|-------------|------------|--------------|------------|-------------|------------|
|                         | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ |
| 1'                      | 1411.8      | 0.1        | 1399.0       | 0.1        | 1386.1      | 0.1        |
| 2                       | 2823.5      | 0.6        | 2798.0       | 0.6        | 2772.2      | 0.6        |
| 3                       | 4235.3      | 1.3        | 4197.0       | 1.3        | 4158.4      | 1.3        |
| 4                       | 5647.1      | 2.4        | 5596.0       | 2.4        | 5544.5      | 2.4        |
| 5                       | 7058.8      | 3.7        | 6995.0       | 3.7        | 6930.6      | 3.7        |
| 6                       | 8470.6      | 5.3        | 8394.0       | 5.3        | 8316.7      | 5.3        |
| 7                       | 9882.4      | 7.2        | 9793.0       | 7.2        | 9702.8      | 7.2        |
| 8                       | 11294.1     | 9.5        | 11192.0      | 9.4        | 11089.0     | 9.4        |
| 9                       | 12705.9     | 12.0       | 12591.0      | 12.0       | 12475.1     | 11.9       |
| 10                      | 14117.7     | 14.8       | 13990.0      | 14.8       | 13861.2     | 14.7       |
| 11                      | 15529.4     | 17.9       | 15389.0      | 17.9       | 15247.3     | 17.8       |
| 12                      | 16941.2     | 21.3       | 16788.0      | 21.3       | 16633.4     | 21.2       |
| 13                      | 18353.0     | 25.0       | 18186.9      | 24.9       | 18019.5     | 24.9       |
| 14                      | 19764.7     | 28.9       | 19585.9      | 28.9       | 19405.7     | 28.9       |
| 15                      | 21176.5     | 33.2       | 20984.9      | 33.2       | 20791.8     | 33.2       |
| 16                      | 22588.3     | 37.8       | 22383.9      | 37.8       | 22177.9     | 37.7       |
| 17                      | 24000.0     | 42.7       | 23782.9      | 42.7       | 23564.0     | 42.6       |
| 18                      | 25411.8     | 47.9       | 25181.9      | 47.8       | 24950.1     | 47.8       |
| 19                      | 26823.6     | 53.3       | 26580.9      | 53.3       | 26336.2     | 53.2       |
| 20                      | 28235.3     | 59.1       | 27979.9      | 59.0       | 27722.4     | 59.0       |
| 25                      | 35294.1     | 92.3       | 24974.8      | 92.2       | 34652.9     | 92.2       |
| 30                      | 42352.9     | 132.9      | 41969.8      | 132.8      | 41583.4     | 132.7      |
| 40                      | 56470.3     | 236.3      | 55959.5      | 236.2      | 55444.3     | 235.9      |
| 50                      | 70587.5     | 369.3      | 69949.0      | 369.0      | 69305.1     | 368.6      |
| 1° 00                   | 84704.5     | 531.7      | 83938.2      | 531.3      | 83165.6     | 530.8      |
| 1 20                    | 112937.6    | 945.3      | 111915.9     | 944.6      | 110885.7    | 943.6      |
| 1 30                    | 127053.6    | 1196.4     | 125904.2     | 1195.5     | 124747.2    | 1194.3     |
| 1 40                    | 141169.2    | 1477.0     | 139892.1     | 1476.0     | 138604.3    | 1474.4     |
| 2 00                    | 169399.0    | 2126.9     | 167866.4     | 2125.4     | 166321.0    | 2123.2     |
| 2 30                    | 211739.3    | 3323.3     | 209823.5     | 3320.9     | 207891.7    | 3317.5     |
| 3 00                    | 254073.4    | 4785.6     | 251774.4     | 4782.1     | 249456.0    | 4777.2     |
| 3 30                    | 296400.0    | 6513.8     | 293717.6     | 6509.0     | 291012.8    | 6502.2     |
| 4 00                    | 338717.8    | 8507.8     | 335652.1     | 8501.5     | 332560.6    | 8492.7     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards,*

| Long.<br>value<br>of Z. | Lat. 47° 30' |            | Lat. 48° 0' |            | Lat. 48° 30' |            |
|-------------------------|--------------|------------|-------------|------------|--------------|------------|
|                         | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ |
| 1'                      | 1373.1       | 0.1        | 1360.0      | 0.1        | 1346.9       | 0.1        |
| 2                       | 2746.3       | 0.6        | 2720.1      | 0.6        | 2693.7       | 0.6        |
| 3                       | 4119.4       | 1.3        | 4080.1      | 1.3        | 4040.6       | 1.3        |
| 4                       | 5492.5       | 2.4        | 5440.2      | 2.4        | 5387.4       | 2.4        |
| 5                       | 6865.7       | 3.7        | 6800.2      | 3.7        | 6734.3       | 3.7        |
| 6                       | 8238.8       | 5.3        | 8160.3      | 5.3        | 8081.1       | 5.3        |
| 7                       | 9612.0       | 7.2        | 9520.3      | 7.2        | 9428.0       | 7.2        |
| 8                       | 10985.1      | 9.4        | 10880.4     | 9.4        | 10774.8      | 9.4        |
| 9                       | 12358.2      | 11.9       | 12240.4     | 11.9       | 12121.7      | 11.9       |
| 10                      | 13731.4      | 14.7       | 13600.5     | 14.7       | 13468.5      | 14.7       |
| 11                      | 15104.5      | 17.8       | 14960.5     | 17.8       | 14815.4      | 17.8       |
| 12                      | 16477.6      | 21.2       | 16320.5     | 21.2       | 16162.2      | 21.1       |
| 13                      | 17850.8      | 24.9       | 17680.6     | 24.8       | 17509.1      | 24.8       |
| 14                      | 19223.9      | 28.9       | 19040.6     | 28.8       | 18855.9      | 28.8       |
| 15                      | 20597.0      | 33.1       | 20400.7     | 33.1       | 20202.8      | 33.0       |
| 16                      | 21970.1      | 37.7       | 21760.7     | 37.6       | 21549.6      | 37.6       |
| 17                      | 23343.3      | 42.6       | 23120.7     | 42.5       | 22896.5      | 42.4       |
| 18                      | 24716.4      | 47.7       | 24480.8     | 47.6       | 24243.3      | 47.5       |
| 19                      | 26089.5      | 53.1       | 25840.8     | 53.1       | 25590.2      | 53.0       |
| 20                      | 27462.7      | 58.9       | 27200.9     | 58.8       | 26937.0      | 58.7       |
| 25                      | 34328.3      | 92.0       | 34001.0     | 91.9       | 33671.2      | 91.7       |
| 30                      | 41193.9      | 132.5      | 40801.2     | 132.3      | 40405.4      | 132.0      |
| 40                      | 54925.0      | 235.6      | 54401.4     | 235.2      | 53873.6      | 234.7      |
| 50                      | 68655.8      | 368.1      | 68001.4     | 367.5      | 67341.7      | 366.8      |
| 1° 00                   | 82386.5      | 530.1      | 81601.1     | 529.2      | 80809.5      | 528.2      |
| 1 20                    | 109846.9     | 942.4      | 108799.7    | 940.8      | 107744.2     | 939.0      |
| 1 30                    | 123576.6     | 1192.7     | 122398.5    | 1190.7     | 121211.0     | 1188.4     |
| 1 40                    | 137305.6     | 1472.4     | 135996.8    | 1470.0     | 134677.3     | 1467.1     |
| 2 00                    | 164762.8     | 2120.3     | 163191.9    | 2116.8     | 161608.6     | 2112.7     |
| 2 30                    | 205943.9     | 3313.0     | 203980.3    | 3307.5     | 202001.0     | 3301.1     |
| 3 00                    | 247118.6     | 4770.7     | 244762.2    | 4762.9     | 242387.0     | 4753.5     |
| 3 30                    | 288285.6     | 6493.5     | 285536.3    | 6482.8     | 282765.2     | 6470.1     |
| 4 00                    | 329443.7     | 8481.3     | 326301.5    | 8467.3     | 323134.3     | 8450.7     |

*Co-ordinates,  $\delta m$ ,  $\delta p$ , in Yards.*

| Long.<br>value<br>of Z. | Lat. 49° 0' |            | Lat. 49° 30' |            | Lat. 50° 0' |            |
|-------------------------|-------------|------------|--------------|------------|-------------|------------|
|                         | $\delta m$  | $\delta p$ | $\delta m$   | $\delta p$ | $\delta m$  | $\delta p$ |
| 1'                      | 1333.6      | 0.1        | 1320.2       | 0.1        | 1306.7      | 0.1        |
| 2                       | 2667.1      | 0.6        | 2640.3       | 0.6        | 2213.3      | 0.6        |
| 3                       | 4000.7      | 1.3        | 2960.5       | 1.3        | 3920.0      | 1.3        |
| 4                       | 5334.2      | 2.3        | 5280.6       | 2.3        | 5226.6      | 2.3        |
| 5                       | 6667.8      | 3.7        | 6600.8       | 3.7        | 6533.3      | 3.6        |
| 6                       | 8001.3      | 5.3        | 7920.9       | 5.3        | 7839.9      | 5.2        |
| 7                       | 9334.9      | 7.2        | 9241.1       | 7.2        | 9146.6      | 7.1        |
| 8                       | 10668.4     | 9.4        | 10561.2      | 9.3        | 10453.2     | 9.3        |
| 9                       | 12002.0     | 11.9       | 11881.4      | 11.8       | 11759.9     | 11.8       |
| 10                      | 13335.5     | 14.6       | 13201.6      | 14.6       | 13066.5     | 14.6       |
| 11                      | 14669.1     | 17.7       | 14521.7      | 17.7       | 14373.2     | 17.6       |
| 12                      | 16002.7     | 21.1       | 15841.8      | 21.0       | 15679.8     | 21.0       |
| 13                      | 17336.2     | 24.7       | 17162.0      | 24.7       | 16986.5     | 24.6       |
| 14                      | 18669.7     | 28.7       | 18482.1      | 28.6       | 18293.1     | 28.5       |
| 15                      | 20003.3     | 32.9       | 19802.3      | 32.8       | 19599.8     | 32.8       |
| 16                      | 21336.8     | 37.5       | 21122.4      | 37.4       | 20906.4     | 37.3       |
| 17                      | 22670.4     | 42.3       | 22442.6      | 42.2       | 22213.1     | 42.1       |
| 18                      | 24004.0     | 47.4       | 23762.8      | 47.3       | 23519.7     | 47.2       |
| 19                      | 25337.5     | 52.8       | 25082.9      | 52.7       | 24826.4     | 52.6       |
| 20                      | 26671.1     | 58.6       | 26403.1      | 58.4       | 26133.0     | 58.2       |
| 25                      | 33338.8     | 91.5       | 33003.8      | 91.2       | 32666.2     | 91.0       |
| 30                      | 40006.5     | 131.7      | 39604.5      | 131.4      | 39199.4     | 131.0      |
| 40                      | 53341.7     | 234.2      | 52805.7      | 233.6      | 52265.7     | 232.9      |
| 50                      | 66676.8     | 365.9      | 66006.8      | 365.0      | 65331.7     | 364.0      |
| 1° 00                   | 80011.6     | 527.0      | 79207.6      | 525.6      | 78397.5     | 524.1      |
| 1 20                    | 106680.4    | 936.8      | 105608.3     | 934.4      | 104528.2    | 931.7      |
| 1 30                    | 120014.2    | 1185.7     | 118808.2     | 1182.6     | 117593.0    | 1179.2     |
| 1 40                    | 133347.5    | 1463.8     | 132007.5     | 1460.0     | 130657.4    | 1455.8     |
| 2 00                    | 160012.8    | 2107.9     | 158404.8     | 2102.5     | 156784.7    | 2096.4     |
| 2 30                    | 200006.3    | 3293.6     | 197996.2     | 3285.1     | 195970.8    | 3275.6     |
| 3 00                    | 239993.2    | 4742.8     | 237551.0     | 4730.5     | 235150.6    | 4716.9     |
| 3 30                    | 279972.3    | 6455.4     | 277158.0     | 6438.8     | 274322.4    | 6420.2     |
| 4 00                    | 319942.3    | 8316.6     | 316725.8     | 8409.9     | 313485.0    | 8385.6     |

*Arcs of the Parallel—Values of D p, in Yards.*

|    |    | L. 20° 30' | L. 21° 0' | L. 21° 30' | L. 22° 0' | L. 22° 30' | L. 23° 0' |
|----|----|------------|-----------|------------|-----------|------------|-----------|
| '  | "  |            |           |            |           |            |           |
|    | 7  | 221.8      | 221.1     | 220.3      | 219.6     | 218.8      | 218.0     |
|    | 8  | 253.5      | 252.6     | 251.8      | 250.9     | 250.0      | 249.1     |
|    | 9  | 285.2      | 284.2     | 283.3      | 282.3     | 281.3      | 280.3     |
|    | 10 | 316.9      | 315.8     | 314.7      | 313.7     | 312.5      | 311.4     |
|    | 20 | 633.7      | 631.6     | 629.5      | 627.3     | 625.1      | 622.8     |
|    | 30 | 950.6      | 947.4     | 944.2      | 941.0     | 937.6      | 934.2     |
|    | 40 | 1267.4     | 1263.2    | 1259.0     | 1254.6    | 1250.2     | 1245.7    |
|    | 50 | 1584.3     | 1579.1    | 1573.7     | 1568.3    | 1562.7     | 1557.1    |
|    | 60 | 1901.1     | 1894.9    | 1888.5     | 1881.9    | 1875.3     | 1868.5    |
| 7  | -  | 13307.8    | 13264.1   | 13219.4    | 13173.7   | 13127.0    | 13079.4   |
| 8  | -  | 15208.9    | 15159.0   | 15107.9    | 15055.7   | 15002.3    | 14947.9   |
| 9  | -  | 17110.0    | 17053.8   | 16996.4    | 16937.6   | 16877.6    | 16816.3   |
| 10 | -  | 19011.1    | 18948.7   | 18884.9    | 18819.6   | 18752.9    | 18684.8   |
| 20 | -  | 38022.1    | 37897.4   | 37769.7    | 37639.2   | 37505.8    | 37369.6   |
| 30 | -  | 57033.2    | 56846.1   | 56654.6    | 56458.8   | 56258.8    | 56054.4   |
| 40 | -  | 76044.3    | 75794.8   | 75539.5    | 75278.4   | 75011.7    | 74739.3   |
| 50 | -  | 95055.4    | 94743.4   | 94424.3    | 94098.0   | 93764.6    | 93424.1   |
| 60 | -  | 114066.4   | 113692.1  | 113309.2   | 112917.7  | 112517.6   | 112108.9  |

*Meridional Arcs—Values of D m, in Yards.*

|    |    | L. 21° 0' | L. 22° 0' | L. 23° 0' |
|----|----|-----------|-----------|-----------|
| '  | "  |           |           |           |
|    | 7  | 235.4     | 235.4     | 235.5     |
|    | 8  | 269.0     | 269.1     | 269.1     |
|    | 9  | 302.7     | 302.7     | 302.8     |
|    | 10 | 336.3     | 336.4     | 336.4     |
|    | 20 | 672.6     | 672.7     | 672.8     |
|    | 30 | 1008.9    | 1009.1    | 1009.2    |
|    | 40 | 1345.2    | 1345.4    | 1345.6    |
|    | 50 | 1681.6    | 1681.8    | 1682.0    |
|    | 60 | 2017.9    | 2018.1    | 2018.4    |
| 7  | -  | 14125.0   | 14126.7   | 14128.5   |
| 8  | -  | 16142.9   | 16144.8   | 16146.8   |
| 9  | -  | 18160.8   | 18162.9   | 18165.2   |
| 10 | -  | 20178.6   | 20181.0   | 20183.5   |
| 20 | -  | 40357.2   | 40362.1   | 40367.1   |
| 30 | -  | 60535.9   | 60543.1   | 60550.6   |
| 40 | -  | 80714.5   | 80724.1   | 80734.1   |
| 50 | -  | 100893.1  | 100905.2  | 100917.6  |
| 60 | -  | 121071.7  | 121086.2  | 121101.2  |

Intermediate minutes and seconds will be found by moving the decimal point.

*Arcs of the Parallel—Values of D p, in Yards.*

|    |    | L. 23° 30' | L. 24° 0' | L. 24° 30' | L. 25° 0' | L. 25° 30' | L. 26° 0' |
|----|----|------------|-----------|------------|-----------|------------|-----------|
| '  | "  |            |           |            |           |            |           |
|    | 7  | 217.2      | 216.4     | 215.4      | 214.6     | 213.8      | 212.9     |
|    | 8  | 248.2      | 247.3     | 246.3      | 245.3     | 244.3      | 243.3     |
|    | 9  | 279.2      | 278.2     | 277.1      | 276.0     | 274.8      | 273.7     |
|    | 10 | 310.3      | 309.1     | 307.9      | 306.6     | 305.4      | 304.1     |
|    | 20 | 620.5      | 618.1     | 615.7      | 613.3     | 610.8      | 608.2     |
|    | 30 | 930.8      | 927.6     | 923.6      | 919.9     | 916.2      | 912.3     |
|    | 40 | 1241.0     | 1236.3    | 1231.5     | 1226.5    | 1221.5     | 1216.4    |
|    | 50 | 1551.3     | 1545.4    | 1539.3     | 1533.2    | 1526.9     | 1520.5    |
|    | 60 | 1861.5     | 1854.4    | 1847.2     | 1839.8    | 1832.3     | 1824.7    |
| 7  | -  | 13030.7    | 12981.0   | 12930.4    | 12878.8   | 12826.1    | 12772.6   |
| 8  | -  | 14892.2    | 14835.5   | 14777.6    | 14718.6   | 14658.5    | 14597.2   |
| 9  | -  | 16753.8    | 16689.9   | 16624.8    | 16558.4   | 16490.8    | 16421.9   |
| 10 | -  | 18615.3    | 18544.3   | 18472.0    | 18398.2   | 18323.1    | 18246.5   |
| 20 | -  | 37230.6    | 37088.7   | 36944.0    | 36796.5   | 36646.1    | 36493.0   |
| 30 | -  | 55845.8    | 55633.0   | 55416.0    | 55194.7   | 54969.2    | 54739.6   |
| 40 | -  | 74461.1    | 74177.4   | 73887.9    | 73592.9   | 73292.3    | 72986.1   |
| 50 | -  | 93076.4    | 92721.7   | 92359.9    | 91991.1   | 91615.3    | 91232.6   |
| 60 | -  | 111691.7   | 111266.0  | 110831.9   | 110389.4  | 109938.4   | 109479.1  |

*Meridional Arcs—Values of D m, in Yards.*

|    |    | L. 24° 0' | L. 25° 0' | L. 26° 0' |
|----|----|-----------|-----------|-----------|
| '  | "  |           |           |           |
|    | 7  | 235.5     | 235.5     | 235.6     |
|    | 8  | 269.1     | 269.2     | 269.2     |
|    | 9  | 302.8     | 302.8     | 302.9     |
|    | 10 | 336.4     | 336.5     | 336.5     |
|    | 20 | 672.9     | 673.0     | 673.1     |
|    | 30 | 1009.3    | 1009.4    | 1009.6    |
|    | 40 | 1345.7    | 1345.9    | 1346.1    |
|    | 50 | 1682.2    | 1682.4    | 1682.6    |
|    | 60 | 2018.6    | 2018.9    | 2019.2    |
| 7  | -  | 14130.3   | 14132.1   | 14134.1   |
| 8  | -  | 16148.9   | 16151.0   | 16153.2   |
| 9  | -  | 18167.5   | 18169.3   | 18172.4   |
| 10 | -  | 20186.1   | 20188.8   | 20191.5   |
| 20 | -  | 40372.2   | 40377.5   | 40382.0   |
| 30 | -  | 60558.3   | 60566.3   | 60574.6   |
| 40 | -  | 80744.4   | 80755.1   | 80766.1   |
| 50 | -  | 100930.5  | 100943.9  | 100957.6  |
| 60 | -  | 121116.6  | 121132.6  | 121149.1  |

Intermediate minutes and seconds will be found by moving the decimal point.

*Arcs of the Parallel—Values of D p, in Yards.*

|    |    | L. 26° 30' | L. 27° 0' | L. 27° 30' | L. 28° 0' | L. 28° 30' | L. 29° 0' |
|----|----|------------|-----------|------------|-----------|------------|-----------|
| '  | "  |            |           |            |           |            |           |
|    | 7  | 212.0      | 211.0     | 210.1      | 209.1     | 208.2      | 207.2     |
|    | 8  | 242.2      | 241.2     | 240.1      | 239.0     | 237.9      | 236.8     |
|    | 9  | 272.5      | 271.3     | 270.1      | 268.9     | 267.6      | 266.4     |
|    | 10 | 302.8      | 301.5     | 300.1      | 298.8     | 297.4      | 296.0     |
|    | 20 | 605.6      | 603.0     | 600.3      | 597.6     | 594.8      | 591.9     |
|    | 30 | 908.4      | 904.5     | 900.4      | 896.3     | 892.2      | 887.9     |
|    | 40 | 1211.2     | 1206.0    | 1200.6     | 1195.1    | 1189.5     | 1183.9    |
|    | 50 | 1514.0     | 1507.4    | 1500.7     | 1493.9    | 1486.9     | 1479.9    |
|    | 60 | 1816.9     | 1808.9    | 1800.9     | 1792.7    | 1784.3     | 1775.8    |
| 7  | -  | 12718.0    | 12663.5   | 12606.0    | 12548.6   | 12490.1    | 12430.8   |
| 8  | -  | 14534.9    | 14471.4   | 14406.9    | 14341.2   | 14274.5    | 14206.6   |
| 9  | -  | 16351.7    | 16280.3   | 16207.7    | 16133.9   | 16058.8    | 15982.5   |
| 10 | -  | 18168.6    | 18089.3   | 18008.6    | 17926.5   | 17843.1    | 17758.3   |
| 20 | -  | 36337.2    | 36178.5   | 36017.1    | 35853.0   | 35686.2    | 35516.6   |
| 30 | -  | 54505.8    | 54267.8   | 54025.7    | 53779.5   | 53529.3    | 53274.9   |
| 40 | -  | 72674.4    | 72357.1   | 72034.3    | 71706.1   | 71372.4    | 71033.2   |
| 50 | -  | 90843.0    | 90446.3   | 90042.9    | 89632.6   | 89215.4    | 88791.5   |
| 60 | -  | 109011.5   | 108535.6  | 108051.4   | 107559.1  | 107058.5   | 106549.8  |

*Meridional Arcs—Values of D m, in Yards.*

|    |    | L. 27° 0' | L. 28° 0' | L. 29° 0' |
|----|----|-----------|-----------|-----------|
| '  | "  |           |           |           |
|    | 7  | 235.6     | 235.6     | 235.7     |
|    | 8  | 269.3     | 269.3     | 269.3     |
|    | 9  | 302.9     | 303.0     | 303.0     |
|    | 10 | 336.6     | 336.6     | 336.7     |
|    | 20 | 673.1     | 673.2     | 673.3     |
|    | 30 | 1009.7    | 1009.9    | 1010.0    |
|    | 40 | 1346.3    | 1346.5    | 1346.7    |
|    | 50 | 1682.9    | 1683.1    | 1683.3    |
|    | 60 | 2019.4    | 2019.7    | 2020.0    |
| 7  | -  | 14136.0   | 14138.1   | 14140.1   |
| 8  | -  | 16155.5   | 16157.8   | 16160.2   |
| 9  | -  | 18174.9   | 18177.5   | 18180.2   |
| 10 | -  | 20194.3   | 20197.2   | 20200.2   |
| 20 | -  | 40388.7   | 40394.5   | 40400.4   |
| 30 | -  | 60583.0   | 60591.7   | 60600.6   |
| 40 | -  | 80777.4   | 80788.9   | 80800.8   |
| 50 | -  | 100971.7  | 100986.2  | 101001.0  |
| 60 | -  | 121166.0  | 121183.4  | 121201.2  |

Intermediate minutes and seconds will be found by moving the decimal point.

*Arcs of the Parallel—Values of D p, in Yards.*

|    | L. 29° 30' | L. 30° 0' | L. 30° 30' | L. 31° 0' | L. 31° 30' | L. 32° 0' |
|----|------------|-----------|------------|-----------|------------|-----------|
| '  |            |           |            |           |            |           |
| "  |            |           |            |           |            |           |
| 7  | 206.2      | 205.2     | 204.1      | 203.1     | 202.0      | 200.9     |
| 8  | 235.6      | 234.5     | 233.3      | 232.1     | 230.9      | 229.6     |
| 9  | 265.1      | 263.8     | 262.4      | 261.1     | 259.7      | 258.3     |
| 10 | 294.5      | 293.1     | 291.6      | 290.1     | 288.6      | 287.0     |
| 20 | 589.1      | 586.2     | 583.2      | 580.2     | 577.1      | 574.0     |
| 30 | 833.6      | 829.2     | 824.8      | 820.3     | 815.7      | 811.1     |
| 40 | 1178.1     | 1172.3    | 1166.4     | 1160.4    | 1154.3     | 1148.1    |
| 50 | 1472.7     | 1465.4    | 1458.0     | 1450.5    | 1442.9     | 1435.1    |
| 60 | 1767.2     | 1758.5    | 1749.6     | 1740.6    | 1731.4     | 1722.1    |
| 7  | - 12370.5  | 12309.3   | 12247.1    | 12184.0   | 12120.0    | 12055.0   |
| 8  | - 14137.7  | 14067.7   | 13996.7    | 13924.6   | 13851.4    | 13777.1   |
| 9  | - 15904.9  | 15826.2   | 15746.3    | 15665.1   | 15582.8    | 15499.3   |
| 10 | - 17672.2  | 17584.7   | 17495.9    | 17405.7   | 17314.2    | 17221.4   |
| 20 | - 35344.3  | 35169.4   | 34991.7    | 34811.4   | 34628.4    | 34442.9   |
| 30 | - 53016.5  | 52754.0   | 52487.6    | 52217.1   | 51942.7    | 51664.3   |
| 40 | - 70688.7  | 70398.7   | 69983.4    | 69622.8   | 69256.9    | 68885.7   |
| 50 | - 88360.8  | 87923.4   | 87479.3    | 87028.5   | 86571.1    | 86107.1   |
| 60 | - 106033.0 | 105508.1  | 104975.2   | 104434.2  | 103885.3   | 103328.6  |

*Meridional Arcs—Values of D m, in Yards.*

|    |   | L. 30° 0' |  | L. 31° 0' |  | L. 32° 0' |
|----|---|-----------|--|-----------|--|-----------|
| '  |   |           |  |           |  |           |
| "  |   |           |  |           |  |           |
| 7  |   | 235.7     |  | 235.7     |  | 235.8     |
| 8  |   | 269.4     |  | 269.4     |  | 269.5     |
| 9  |   | 303.0     |  | 303.1     |  | 303.1     |
| 10 |   | 336.7     |  | 336.8     |  | 336.8     |
| 20 |   | 673.4     |  | 673.5     |  | 673.6     |
| 30 |   | 1010.2    |  | 1010.3    |  | 1010.5    |
| 40 |   | 1346.9    |  | 1347.1    |  | 1347.3    |
| 50 |   | 1683.6    |  | 1683.9    |  | 1684.1    |
| 60 |   | 2020.3    |  | 2020.6    |  | 2020.9    |
| 7  | - | 14142.3   |  | 14144.4   |  | 14146.6   |
| 8  | - | 16162.6   |  | 16165.1   |  | 16167.6   |
| 9  | - | 18182.9   |  | 18185.7   |  | 18188.5   |
| 10 | - | 20203.2   |  | 20206.3   |  | 20209.5   |
| 20 | - | 40406.5   |  | 40412.6   |  | 40418.9   |
| 30 | - | 60609.7   |  | 60619.0   |  | 60628.4   |
| 40 | - | 80812.9   |  | 80825.3   |  | 80837.9   |
| 50 | - | 101016.1  |  | 101031.6  |  | 101047.4  |
| 60 | - | 121219.4  |  | 121237.9  |  | 121256.8  |

Intermediate minutes and seconds will be found by moving the decimal point.



*Arcs of the parallel—Values of D p, in Yards.*

|    |    | L. 32° 30' | L. 33° 0' | L. 33° 30' | L. 34° 0' | L. 34° 30' | L. 35° 0' |
|----|----|------------|-----------|------------|-----------|------------|-----------|
| '  | "  |            |           |            |           |            |           |
|    | 7  | 199.8      | 198.7     | 197.6      | 196.4     | 195.3      | 194.1     |
|    | 8  | 228.4      | 227.1     | 225.8      | 224.5     | 223.2      | 221.8     |
|    | 9  | 256.9      | 254.5     | 254.0      | 252.6     | 251.1      | 249.6     |
|    | 10 | 285.5      | 283.9     | 282.3      | 280.6     | 279.0      | 277.3     |
|    | 20 | 570.9      | 567.7     | 564.5      | 561.2     | 557.9      | 554.6     |
|    | 30 | 856.4      | 851.6     | 846.8      | 841.9     | 836.9      | 831.9     |
|    | 40 | 1141.8     | 1135.5    | 1129.0     | 1122.5    | 1115.9     | 1109.2    |
|    | 50 | 1427.3     | 1419.3    | 1411.3     | 1403.1    | 1394.8     | 1386.4    |
|    | 60 | 1712.7     | 1703.2    | 1693.5     | 1683.7    | 1673.8     | 1663.7    |
| 7  | -  | 11989.1    | 11922.3   | 11854.6    | 11786.0   | 11716.5    | 11646.1   |
| 8  | -  | 13701.9    | 13625.5   | 13548.1    | 13469.7   | 13390.3    | 13309.8   |
| 9  | -  | 15414.6    | 15328.7   | 15241.7    | 15153.5   | 15064.1    | 14973.6   |
| 10 | -  | 17127.3    | 17031.9   | 16935.2    | 16837.2   | 16737.9    | 16637.3   |
| 20 | -  | 34254.6    | 34063.8   | 33870.4    | 33674.3   | 33475.8    | 33274.6   |
| 30 | -  | 51381.9    | 51095.7   | 50805.5    | 50511.5   | 50213.6    | 49911.9   |
| 40 | -  | 68509.3    | 68127.6   | 67740.7    | 67348.7   | 66951.5    | 66549.2   |
| 50 | -  | 85636.6    | 85159.5   | 84675.9    | 84185.8   | 83689.4    | 83186.5   |
| 60 | -  | 102763.9   | 102191.4  | 101611.1   | 101023.0  | 100427.3   | 99823.8   |

*Meridional Arcs—Values of D m, in Yards.*

|    |    | L. 33° 0' |  | L. 34° 0' |  | L. 35° 0' |
|----|----|-----------|--|-----------|--|-----------|
|    | "  |           |  |           |  |           |
|    | 7  | 235.8     |  | 235.9     |  | 235.9     |
|    | 8  | 269.5     |  | 269.5     |  | 269.6     |
|    | 9  | 303.2     |  | 303.2     |  | 303.3     |
|    | 10 | 336.9     |  | 336.9     |  | 337.0     |
|    | 20 | 673.8     |  | 673.9     |  | 674.0     |
|    | 30 | 1010.6    |  | 1010.8    |  | 1011.0    |
|    | 40 | 1347.5    |  | 1347.7    |  | 1347.9    |
|    | 50 | 1684.4    |  | 1684.7    |  | 1684.9    |
|    | 60 | 2021.3    |  | 2021.6    |  | 2021.9    |
| 7  | -  | 14148.9   |  | 14151.2   |  | 14153.5   |
| 8  | -  | 16170.1   |  | 16172.7   |  | 16175.4   |
| 9  | -  | 18191.4   |  | 18194.3   |  | 18197.3   |
| 10 | -  | 20212.7   |  | 20215.9   |  | 20219.2   |
| 20 | -  | 40425.4   |  | 40431.9   |  | 40438.5   |
| 30 | -  | 60638.0   |  | 60647.8   |  | 60657.7   |
| 40 | -  | 80850.7   |  | 80863.7   |  | 80877.0   |
| 50 | -  | 101063.4  |  | 101079.7  |  | 101096.2  |
| 60 | -  | 121276.1  |  | 121295.6  |  | 121315.4  |

Intermediate minutes and seconds will be found by moving the decimal point.

*Arcs of the Parallel—Values of D p, in Yards.*

|    |   | L. 35° 30' | L. 36° 0' | L. 36° 30' | L. 37° 0' | L. 37° 30' | L. 38° 0' |
|----|---|------------|-----------|------------|-----------|------------|-----------|
| 7  | " | 192.9      | 191.7     | 190.5      | 189.3     | 188.0      | 186.8     |
| 8  | " | 220.5      | 219.1     | 217.7      | 216.3     | 214.9      | 213.4     |
| 9  | " | 248.0      | 246.5     | 244.9      | 243.3     | 241.7      | 240.1     |
| 10 | " | 275.6      | 273.9     | 272.1      | 270.4     | 268.6      | 266.8     |
| 20 | " | 551.2      | 547.7     | 544.3      | 540.7     | 537.2      | 533.6     |
| 30 | " | 826.8      | 821.6     | 816.4      | 811.1     | 805.8      | 800.4     |
| 40 | " | 1102.4     | 1095.5    | 1088.5     | 1081.5    | 1074.4     | 1067.2    |
| 50 | " | 1378.0     | 1369.4    | 1360.7     | 1351.9    | 1343.0     | 1334.0    |
| 60 | " | 1653.5     | 1643.2    | 1632.9     | 1622.2    | 1611.6     | 1600.7    |
| 7  | - | 11574.8    | 11502.7   | 11429.6    | 11355.7   | 11280.9    | 11205.2   |
| 8  | - | 13228.4    | 13145.9   | 13062.4    | 12977.9   | 12892.5    | 12806.0   |
| 9  | - | 14881.9    | 14789.1   | 14695.2    | 14600.2   | 14504.0    | 14406.7   |
| 10 | - | 16535.5    | 16432.4   | 16328.0    | 16222.4   | 16115.6    | 16007.5   |
| 20 | - | 33070.9    | 32864.7   | 32656.0    | 32444.8   | 32231.1    | 32015.0   |
| 30 | - | 49606.4    | 49297.1   | 48984.0    | 48667.2   | 48346.7    | 48022.5   |
| 40 | - | 66141.9    | 65729.5   | 65312.1    | 64889.6   | 64462.3    | 64030.0   |
| 50 | - | 82677.3    | 82161.8   | 81640.1    | 81112.0   | 80577.8    | 80037.5   |
| 60 | - | 99212.8    | 98594.2   | 97968.1    | 97334.4   | 96693.4    | 96045.0   |

*Meridional Arcs—Values of D m, in Yards.*

|    |   | Log 36° 0' |  | L. 37° 0' |  | L. 38° 0' |
|----|---|------------|--|-----------|--|-----------|
| 7  | " | 235.9      |  | 236.0     |  | 236.0     |
| 8  | " | 269.6      |  | 269.7     |  | 269.7     |
| 9  | " | 303.3      |  | 303.4     |  | 303.4     |
| 10 | " | 337.0      |  | 337.1     |  | 337.2     |
| 20 | " | 674.1      |  | 674.2     |  | 674.3     |
| 30 | " | 1011.1     |  | 1011.3    |  | 1011.5    |
| 40 | " | 1348.2     |  | 1348.4    |  | 1348.6    |
| 50 | " | 1685.2     |  | 1685.5    |  | 1685.8    |
| 60 | " | 2022.3     |  | 2022.6    |  | 2022.9    |
| 7  | - | 14155.8    |  | 14158.2   |  | 14160.6   |
| 8  | - | 16178.1    |  | 16180.8   |  | 16183.5   |
| 9  | - | 18200.3    |  | 18203.4   |  | 18206.5   |
| 10 | - | 20222.6    |  | 20226.0   |  | 20229.4   |
| 20 | - | 40445.2    |  | 40451.9   |  | 40458.8   |
| 30 | - | 60667.5    |  | 60677.9   |  | 60688.2   |
| 40 | - | 80890.3    |  | 80903.9   |  | 80917.6   |
| 50 | - | 101112.9   |  | 101129.9  |  | 101147.0  |
| 60 | - | 121335.5   |  | 121355.8  |  | 121376.4  |

Intermediate minutes and seconds will be found by moving the decimal point.

*Arcs of the Parallel—Values of D p, in Yards.*

|    |    | L. 38° 30' | L. 39° 0' | L. 39° 30' | L. 40° 0' | L. 40° 30' | L. 41° 0' |
|----|----|------------|-----------|------------|-----------|------------|-----------|
|    | 7  | 185.5      | 184.2     | 182.9      | 181.6     | 180.2      | 178.9     |
|    | 8  | 212.0      | 210.5     | 209.0      | 207.5     | 206.0      | 204.4     |
|    | 9  | 238.5      | 236.8     | 235.1      | 233.4     | 231.7      | 230.0     |
|    | 10 | 265.0      | 263.1     | 261.3      | 259.4     | 257.5      | 255.6     |
|    | 20 | 529.9      | 526.3     | 522.5      | 518.8     | 515.0      | 511.1     |
|    | 30 | 794.9      | 789.4     | 783.8      | 778.2     | 772.4      | 766.7     |
|    | 40 | 1059.9     | 1052.5    | 1045.1     | 1037.5    | 1029.9     | 1022.2    |
|    | 50 | 1324.9     | 1315.6    | 1306.3     | 1296.9    | 1287.4     | 1277.8    |
|    | 60 | 1589.8     | 1578.8    | 1567.6     | 1556.3    | 1544.9     | 1533.4    |
| 7  | -  | 11128.7    | 11051.4   | 10973.2    | 10894.1   | 10814.3    | 10733.6   |
| 8  | -  | 12718.6    | 12630.2   | 12540.8    | 12450.4   | 12359.2    | 12266.9   |
| 9  | -  | 14308.4    | 14208.9   | 14108.4    | 14006.8   | 13904.1    | 13800.3   |
| 10 | -  | 15898.2    | 15787.7   | 15676.0    | 15563.1   | 15448.9    | 15333.4   |
| 20 | -  | 31796.4    | 31575.4   | 31351.9    | 31126.1   | 30897.9    | 30667.3   |
| 30 | -  | 47694.6    | 47363.1   | 47027.9    | 46689.2   | 46346.8    | 46001.0   |
| 40 | -  | 63592.6    | 63150.8   | 62703.9    | 62252.2   | 61795.8    | 61334.6   |
| 50 | -  | 79491.0    | 78938.4   | 78379.9    | 77815.3   | 77244.7    | 76668.3   |
| 60 | -  | 95389.2    | 94726.1   | 94055.8    | 93378.3   | 92693.7    | 92001.9   |

*Meridional Arcs—Values of D m, in Yards.*

|    |    | L. 39° 0' | L. 40° 0' | L. 40° 0' |
|----|----|-----------|-----------|-----------|
|    | 7  | 236.0     | 236.1     | 236.1     |
|    | 8  | 269.8     | 269.8     | 269.9     |
|    | 9  | 303.5     | 303.5     | 303.6     |
|    | 10 | 337.2     | 337.3     | 337.3     |
|    | 20 | 674.4     | 674.5     | 674.7     |
|    | 30 | 1011.6    | 1011.8    | 1012.0    |
|    | 40 | 1348.9    | 1349.1    | 1349.3    |
|    | 50 | 1686.1    | 1686.4    | 1686.7    |
|    | 60 | 2023.3    | 2023.6    | 2024.0    |
| 7  | -  | 14163.0   | 14165.4   | 14167.9   |
| 8  | -  | 16186.3   | 16189.1   | 16191.9   |
| 9  | -  | 18209.6   | 18212.7   | 18215.8   |
| 10 | -  | 20232.8   | 20236.3   | 20239.8   |
| 20 | -  | 40465.7   | 40472.7   | 40479.7   |
| 30 | -  | 60698.5   | 60709.0   | 60719.5   |
| 40 | -  | 80931.4   | 80945.3   | 80959.3   |
| 50 | -  | 101164.2  | 101181.6  | 101199.2  |
| 60 | -  | 121397.1  | 121418.0  | 121439.0  |

Intermediate minutes and seconds will be found by moving the decimal point.

*Arcs of the Parallel—Values of D p, in Yards.*

|    |    | L. 41° 30' | L. 42° 0' | L. 42° 30' | L. 43° 0' | L. 43° 30' | L. 44° 0' |
|----|----|------------|-----------|------------|-----------|------------|-----------|
| '  | "  |            |           |            |           |            |           |
|    | 7  | 177.5      | 176.2     | 174.8      | 173.4     | 172.0      | 170.5     |
|    | 8  | 202.9      | 201.3     | 199.7      | 198.1     | 196.5      | 194.9     |
|    | 9  | 228.3      | 226.5     | 224.7      | 222.9     | 221.1      | 219.3     |
|    | 10 | 253.6      | 251.7     | 249.7      | 247.7     | 245.7      | 243.6     |
|    | 20 | 507.2      | 503.3     | 449.4      | 495.4     | 491.3      | 487.3     |
|    | 30 | 760.9      | 755.0     | 749.0      | 743.0     | 737.0      | 730.9     |
|    | 40 | 1014.5     | 1006.6    | 998.7      | 990.7     | 982.7      | 974.5     |
|    | 50 | 1268.1     | 1258.3    | 1248.4     | 1238.4    | 1228.3     | 1218.1    |
|    | 60 | 1521.7     | 1510.0    | 1498.1     | 1486.1    | 1474.0     | 1461.8    |
| 7  | -  | 10652.0    | 10569.7   | 10486.6    | 10402.6   | 10317.9    | 10232.3   |
| 8  | -  | 12173.8    | 12079.7   | 11984.6    | 11888.7   | 11791.8    | 11694.1   |
| 9  | -  | 13695.5    | 13589.6   | 13482.7    | 13374.8   | 13265.8    | 13155.8   |
| 10 | -  | 15217.2    | 15099.6   | 14980.8    | 14860.9   | 14739.8    | 14617.6   |
| 20 | -  | 30434.4    | 30199.1   | 29961.6    | 29721.7   | 29479.6    | 29235.2   |
| 30 | -  | 45651.6    | 45298.7   | 44942.4    | 44582.6   | 44219.4    | 43852.8   |
| 40 | -  | 60868.8    | 60398.3   | 59923.2    | 59443.4   | 58959.2    | 58470.4   |
| 50 | -  | 76086.0    | 75497.9   | 74903.9    | 74304.3   | 73698.9    | 73088.0   |
| 60 | -  | 91303.2    | 90597.4   | 89884.7    | 89165.1   | 88438.7    | 87705.6   |

*Meridional Arcs—Values of D m, in Yards.*

|    |    | L. 42° 0' | L. 43° 0' | L. 44° 0' |
|----|----|-----------|-----------|-----------|
| '  | "  |           |           |           |
|    | 7  | 236.2     | 236.2     | 236.3     |
|    | 8  | 269.9     | 270.0     | 270.0     |
|    | 9  | 303.7     | 303.7     | 303.8     |
|    | 10 | 337.4     | 337.4     | 337.5     |
|    | 20 | 674.8     | 674.9     | 675.0     |
|    | 30 | 1012.2    | 1012.3    | 1012.5    |
|    | 40 | 1349.6    | 1349.8    | 1350.0    |
|    | 50 | 1686.9    | 1687.2    | 1687.5    |
|    | 60 | 2024.3    | 2024.7    | 2025.0    |
| 7  | -  | 14170.3   | 14172.8   | 14175.3   |
| 8  | -  | 16194.7   | 16197.5   | 16200.3   |
| 9  | -  | 18219.0   | 18222.2   | 18225.4   |
| 10 | -  | 20243.4   | 20246.9   | 20250.4   |
| 20 | -  | 40486.7   | 40493.8   | 40500.9   |
| 30 | -  | 60730.1   | 60740.7   | 60751.3   |
| 40 | -  | 80973.4   | 80987.5   | 81001.7   |
| 50 | -  | 101216.8  | 101234.4  | 101252.2  |
| 60 | -  | 121460.1  | 121481.3  | 121502.6  |

Intermediate minutes and seconds will be found by moving the decimal point.

*Arcs of the Parallel—Values of D p, in Yards.*

|    |    | L. 44° 30' | L. 45° 0' | L. 45° 30' | L. 46° 0' | L. 46° 30' | L. 47° 0' |
|----|----|------------|-----------|------------|-----------|------------|-----------|
| '  | "  |            |           |            |           |            |           |
|    | 7  | 169.1      | 167.6     | 166.2      | 164.7     | 163.2      | 161.7     |
|    | 8  | 193.3      | 191.6     | 189.9      | 188.2     | 186.5      | 184.8     |
|    | 9  | 217.4      | 215.5     | 213.7      | 211.8     | 209.8      | 207.9     |
|    | 10 | 241.6      | 239.5     | 237.4      | 235.3     | 233.2      | 331.0     |
|    | 20 | 483.1      | 479.0     | 474.8      | 470.6     | 466.3      | 462.0     |
|    | 30 | 724.7      | 718.5     | 712.2      | 705.9     | 699.5      | 693.1     |
|    | 40 | 966.3      | 958.0     | 949.6      | 941.2     | 932.7      | 924.1     |
|    | 50 | 1207.9     | 1197.5    | 1187.0     | 1176.5    | 1165.8     | 1155.1    |
|    | 60 | 1449.4     | 1437.0    | 1424.4     | 1411.8    | 1399.0     | 1386.1    |
| 7  | -  | 10146.0    | 10058.9   | 9971.0     | 9882.4    | 9793.0     | 9702.8    |
| 8  | -  | 11595.4    | 11495.9   | 11395.5    | 11294.2   | 11192.0    | 11069.0   |
| 9  | -  | 13044.8    | 12932.9   | 12819.9    | 12705.9   | 12591.0    | 12475.1   |
| 10 | -  | 14494.3    | 14369.8   | 14244.3    | 14117.7   | 13990.0    | 13861.2   |
| 20 | -  | 28988.6    | 28739.7   | 28488.6    | 28235.4   | 27980.0    | 27722.4   |
| 30 | -  | 43482.8    | 43109.5   | 42733.0    | 42353.1   | 41970.0    | 41583.6   |
| 40 | -  | 57977.1    | 57479.4   | 56977.3    | 56470.8   | 55960.0    | 55444.8   |
| 50 | -  | 72471.4    | 71849.2   | 71221.6    | 70588.5   | 69950.0    | 69306.0   |
| 60 | -  | 86965.7    | 86219.1   | 85465.9    | 84706.2   | 83940.0    | 83167.3   |

*Meridional Arcs—Values of D m, in Yards.*

|    |    | L. 45° 0' |  | L. 46° 0' |  | L. 47° 0' |
|----|----|-----------|--|-----------|--|-----------|
| '  | "  |           |  |           |  |           |
|    | 7  | 236.3     |  | 236.3     |  | 236.4     |
|    | 8  | 270.1     |  | 270.1     |  | 270.1     |
|    | 9  | 303.8     |  | 303.9     |  | 303.9     |
|    | 10 | 337.6     |  | 337.6     |  | 337.7     |
|    | 20 | 675.1     |  | 675.3     |  | 675.4     |
|    | 30 | 1012.7    |  | 1012.9    |  | 1013.1    |
|    | 40 | 1350.3    |  | 1350.5    |  | 1350.7    |
|    | 50 | 1687.8    |  | 1688.1    |  | 1688.4    |
|    | 60 | 2025.4    |  | 2025.8    |  | 2026.1    |
| 7  | -  | 14177.8   |  | 14180.3   |  | 14182.8   |
| 8  | -  | 16203.2   |  | 16206.0   |  | 16208.9   |
| 9  | -  | 18228.6   |  | 18231.8   |  | 18235.0   |
| 10 | -  | 20254.0   |  | 20257.5   |  | 20261.1   |
| 20 | -  | 40508.0   |  | 40515.1   |  | 40522.2   |
| 30 | -  | 60761.9   |  | 60772.6   |  | 60783.2   |
| 40 | -  | 81015.9   |  | 81030.1   |  | 81044.3   |
| 50 | -  | 101269.9  |  | 101287.7  |  | 101305.4  |
| 60 | -  | 121523.9  |  | 121545.2  |  | 121566.5  |

Intermediate minutes and seconds will be found by moving the decimal point.

*Arcs of the Parallel—Values of D p, in Yards.*

|    |    | L. 47° 30' | L. 48° 0' | L. 48° 30' | L. 49° 0' | L. 49° 30' | L. 50° 0' |
|----|----|------------|-----------|------------|-----------|------------|-----------|
| '  | "  |            |           |            |           |            |           |
|    | 7  | 160.2      | 158.7     | 157.1      | 155.6     | 154.0      | 152.4     |
|    | 8  | 183.1      | 181.3     | 179.6      | 177.8     | 176.0      | 174.2     |
|    | 9  | 206.0      | 204.0     | 202.0      | 200.0     | 198.0      | 196.0     |
|    | 10 | 228.9      | 226.7     | 224.5      | 222.3     | 220.0      | 217.8     |
|    | 20 | 457.7      | 453.3     | 449.0      | 444.5     | 440.1      | 435.6     |
|    | 30 | 686.6      | 680.0     | 673.4      | 666.8     | 660.1      | 653.3     |
|    | 40 | 915.4      | 906.7     | 897.9      | 889.0     | 880.1      | 871.1     |
|    | 50 | 1144.3     | 1133.4    | 1122.4     | 1111.3    | 1100.1     | 1088.9    |
|    | 60 | 1373.1     | 1360.0    | 1346.9     | 1333.6    | 1320.2     | 1306.7    |
| 7  | -  | 9612.0     | 9520.3    | 9428.0     | 9334.9    | 9241.1     | 9146.6    |
| 8  | -  | 10985.1    | 10880.4   | 10774.8    | 10668.5   | 10561.2    | 10453.2   |
| 9  | -  | 12358.2    | 12240.4   | 12121.7    | 12002.0   | 11881.4    | 11759.9   |
| 10 | -  | 13731.4    | 13600.5   | 13468.5    | 13335.6   | 13201.6    | 13066.5   |
| 20 | -  | 27462.7    | 27200.9   | 26937.1    | 26671.1   | 26403.1    | 26133.1   |
| 30 | -  | 41194.1    | 40801.4   | 40405.6    | 40006.7   | 39604.7    | 39199.6   |
| 40 | -  | 54925.5    | 54401.9   | 53874.1    | 53342.3   | 52806.2    | 52266.2   |
| 50 | -  | 68656.8    | 68002.4   | 67342.7    | 66677.8   | 66007.8    | 65332.7   |
| 60 | -  | 82388.2    | 81602.8   | 80811.2    | 80013.4   | 79209.4    | 78399.3   |

*Meridional Arcs—Values of D m, in Yards.*

|    |    | L. 48° 0' | L. 49° 0' | L. 50° 0' |
|----|----|-----------|-----------|-----------|
| '  | "  |           |           |           |
|    | 7  | 236.4     | 236.5     | 236.5     |
|    | 8  | 270.2     | 270.2     | 270.3     |
|    | 9  | 304.0     | 304.0     | 304.1     |
|    | 10 | 337.7     | 337.8     | 337.9     |
|    | 20 | 675.5     | 675.6     | 675.7     |
|    | 30 | 1013.2    | 1013.4    | 1013.6    |
|    | 40 | 1351.0    | 1351.2    | 1351.4    |
|    | 50 | 1688.7    | 1689.0    | 1689.3    |
|    | 60 | 2026.5    | 2026.8    | 2027.2    |
| 7  | -  | 14185.2   | 14187.7   | 14190.2   |
| 8  | -  | 16211.7   | 16214.5   | 16217.3   |
| 9  | -  | 18238.2   | 18241.3   | 18244.5   |
| 10 | -  | 20264.6   | 20268.1   | 20271.7   |
| 20 | -  | 40529.2   | 40536.3   | 40543.3   |
| 30 | -  | 60793.9   | 60804.4   | 60815.0   |
| 40 | -  | 81058.5   | 81072.6   | 81086.6   |
| 50 | -  | 101323.1  | 101340.7  | 101358.9  |
| 60 | -  | 121587.7  | 121608.9  | 121629.9  |

Intermediate minutes and seconds will be found by moving the decimal point.

*Lengths in Nautical miles and Statute miles of degrees of  
Latitude and Longitude in different Latitudes.*

| DEGREE OF THE PARALLEL.  |                    |                   | DEGREE OF THE MERIDIAN.      |                    |                   |
|--------------------------|--------------------|-------------------|------------------------------|--------------------|-------------------|
| Latitude of<br>Parallel. | Nautical<br>miles. | Statute<br>miles. | Latitude of<br>middle point. | Nautical<br>miles. | Statute<br>miles. |
| 20°                      | 56.404             | 65.018            | 20°                          | 59.664             | 68.777            |
| 21                       | 56.039             | 64.598            |                              |                    |                   |
| 22                       | 55.657             | 64.158            |                              |                    |                   |
| 23                       | 55.258             | 63.698            |                              |                    |                   |
| 24                       | 54.843             | 63.219            |                              |                    |                   |
| 25                       | 54.411             | 62.721            | 25                           | 59.706             | 68.825            |
| 26                       | 53.962             | 62.204            |                              |                    |                   |
| 27                       | 53.497             | 61.668            |                              |                    |                   |
| 28                       | 53.016             | 61.113            |                              |                    |                   |
| 29                       | 52.518             | 60.540            |                              |                    |                   |
| 30                       | 52.005             | 59.948            | 30                           | 59.749             | 68.875            |
| 31                       | 51.476             | 59.338            |                              |                    |                   |
| 32                       | 50.931             | 58.709            |                              |                    |                   |
| 33                       | 50.370             | 58.063            |                              |                    |                   |
| 34                       | 49.794             | 57.399            |                              |                    |                   |
| 35                       | 49.203             | 56.718            | 35                           | 59.796             | 68.929            |
| 36                       | 48.597             | 56.019            |                              |                    |                   |
| 37                       | 47.976             | 55.304            |                              |                    |                   |
| 38                       | 47.341             | 54.571            |                              |                    |                   |
| 39                       | 46.960             | 53.822            |                              |                    |                   |
| 40                       | 46.026             | 53.056            | 40                           | 59.847             | 68.987            |
| 41                       | 45.348             | 52.274            |                              |                    |                   |
| 42                       | 44.654             | 51.476            |                              |                    |                   |
| 43                       | 43.949             | 50.662            |                              |                    |                   |
| 44                       | 43.230             | 49.833            |                              |                    |                   |
| 45                       | 42.497             | 48.988            | 45                           | 59.899             | 69.048            |
| 46                       | 41.752             | 48.128            |                              |                    |                   |
| 47                       | 40.993             | 47.254            |                              |                    |                   |
| 48                       | 40.222             | 46.365            |                              |                    |                   |
| 49                       | 39.439             | 45.462            |                              |                    |                   |
| 50                       | 38.643             | 44.545            | 50                           | 59.951             | 69.108            |

A degree of longitude at the equator = 69.163 statute miles.

A second of time at the equator = 1521.6 feet.

## APPENDIX.

### MAGNETIC OBSERVATIONS.

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*On the use of the Portable Declinometer in the determination of the magnetic Declination (variation) and Horizontal Intensity.*

#### ABSOLUTE DECLINATION.

The adjustment of the Declinometer consists in bringing the line of detorsion (or the direction in which the force of torsion of the thread acts,) first approximately, then accurately, into the magnetic meridian; in determining the zero division of the scale corresponding to the magnetic axis of the collimator magnet, and in bringing the line of collimation of the Theodolite telescope into the magnetic meridian, its vertical wire coinciding with this division.

Having determined the readings of the verniers of the Azimuth circle of the Theodolite corresponding to the magnetic axis of the collimator magnet, turn the telescope into the direction of some object whose azimuth from true north is known, or can be determined, and read off again. The difference of these readings added to or subtracted from the true azimuth of the object referred to, will give the absolute declination.

As the direction of the magnetic meridian is continually changing, the instrument should be left in adjustment, and observed half-hourly, or hourly, for as long a period as possible, in order that the mean declination may be obtained,



instead of the declination at one period only. By this means, also, variations of declination will be obtained.

The angular value of the magnet's scale is determined by measuring with the theodolite the horizontal angle subtended by a certain number of its divisions, the magnet being temporarily fixed. As the interval of the lens and scale is adjusted by the maker, so that the divisions shall be most clearly seen at infini-distant focus, if the adjustment is very accurately made the angular value of the scale will be the same at whatever distance the telescope of the Theodolite may be placed. This, however, should always be tested.

If  $\alpha$ , denote the angular value of one division of the scale, and  $\frac{H}{F}$  the ratio of the torsion and magnetic forces, the true declination changes are deduced from the observed readings, by multiplying their differences by the constant co-efficient  $\alpha \times \left(1 + \frac{H}{F}\right)$ .

The value of  $\frac{H}{F}$  is determined by turning the torsion circle through two or more large angles (for example  $90^\circ$ ) and noting the corresponding differences of reading; if  $w$  equals the mean of the former, and  $u$  that of the latter, reduced to angular value,  $\frac{H}{F} = \frac{w}{w - u}$ .

The value of the co-efficient  $\alpha \left(1 + \frac{H}{F}\right)$  must be given with every abstract of observations; and also a statement of whether increasing numbers denote an easterly or westerly movement of the north end of the magnet.

## ABSOLUTE HORIZONTAL INTENSITY.

The determination of the horizontal intensity requires two distinct series of observations or experiments; those of deflection and those of vibration.

Experiments of Deflection give the ratio of the magnetic moment of the deflecting magnet to the Horizontal Intensity.

Experiments of Vibration, the product of the same quantities. The absolute value of either is obtained by comparing the two.

*The experiments of deflection* consist in observing the angles through which a freely suspended magnet is deflected, by the action of a second magnet, placed at different distances from it in the direction of a line passing through its centre, perpendicular either to the axis of the suspended magnet, or to the magnetic meridian.

The experiments of deflection with the portable declinometer should be made, if possible, at three distances at each side of the suspended magnet, reversing the deflecting magnet each time, and repeating the reversals so as to obtain four readings at each distance on each side. The first distance should be as near as the length of the collimator scale will allow. The second distance, if possible, one-third greater than the first, and the third intermediate to the two first.

When the deflecting magnet is shifted from the east to the west side of the suspended magnet, reverse the order of distances, so that the mean results may correspond nearly to the same time of observation. The corrections for changes of temperature and intensity (during the time employed in the observations) will, in the absence of pro-

per instruments for observing them, in most cases, be compensated by this system of observation.

*Calculation.*—The ratio of the magnetic moment of the deflecting magnet to the horizontal intensity is to be calculated in any case from the observations at each distance taken separately ; if

$m$  = the magnetic moment of the deflecting magnet,

$X$  = the horizontal intensity,

$r$  = the distance between the centres of the deflecting and suspended magnets expressed in feet and decimals of a foot,

$u$  = the corresponding angle of deflection, obtained by multiplying half the mean of each partial result (at each distance) by the angular value of one scale division corrected for torsion,

then: 
$$\frac{m}{X} = \frac{1}{2} r^2 \tan u.$$

*The experiments of vibration* consist in suspending the magnet, used as a deflecting bar, in a wooden box of suitable dimensions, and noting the times at which some central division of the scale passes across the vertical wire of the telescope (of the Theodolite) during at least 300 vibrations ; the magnet having been first made to vibrate steadily, and the arc of vibration reduced to as small a size as the observations will allow.

As the time of vibration depends on the form and weight of the suspended mass, as well as on the product of the magnetic moment of the magnet into the horizontal intensity, its moment of inertia must be experiment-

ally determined before the required value of this product can be obtained. The experiment consists in observing a second series of vibrations with two cylindrical weights of equal dimensions, whose moment of inertia is known, suspended at opposite ends of the magnet ; if,

$K$  = the moment of the suspended magnet and stirrup, (the value required,)

$K'$  = the moment of inertia of the weights,

$T'$  and  $T$  = the times of vibration with and without the weights,

$$K = K' \left( \frac{T'}{T^2 - T'^2} \right)$$

the moment of inertia of the weights is calculated by the formula,

$$K' = \left( \frac{1}{2} l^2 + r^2 \right) p$$

where :

$l$  = interval of the points of suspension, or length of the magnet diminished by the depth of the grooves in which the threads rest,  $r$  = the radius of the cylinders, and  $2p$  their mass, expressed respectively in feet and grains.

The value of  $K$  must be ascertained with very great accuracy from the mean of several series of observations with and without the weights ; once satisfactorily determined, it may be employed as a constant quantity, and the observations with weights need not be repeated in after determinations of the intensity. A small correction must be applied for the changes in the dimensions or form of the suspended mass, produced by changes of temperature ; the correction consists in multiplying the

value of  $K$  by  $1 + 2e(t' - t)$ , where  $t'$  denotes the actual temperature of the magnet,  $t$  the temperature corresponding to the time of the original observations, and  $e$  the coefficient of dilatation of steel for  $1^\circ$  Fahrenheit = 0.000069.

*Calculation.*—The product of the horizontal intensity into the magnetic moment of the suspended magnet is obtained by the formula :

$$\pi X = \frac{\pi^2 K}{T^2}$$

where  $\pi$  = circumference of circle to diameter 1.

$K$  = the moment of inertia of suspended magnet and stirrup.

$T$  = the time of vibration, corrected.

The observed times of vibration must be corrected for the force of torsion of the suspension thread, the rate of chronometer, the arc of vibration, the change of horizontal force between the observations of deflection and vibration, and the differences in the magnetic moment of the deflecting magnet, produced by an increase or decrease of temperature, and by the earth's inducing action. The corrections are to be applied according to the formula :

$$T^2 = \left\{ T' \left( 1 - \frac{r}{86400} \right) \cdot \left( 1 - \frac{a a'}{16} \right) \right\}^2 \cdot \left( 1 + \frac{H}{F} \right) \cdot \left( 1 + \frac{\Delta X}{X} \right) \cdot \left( 1 - (t' - t) g \right) \cdot \left( 1 + \frac{\Delta m}{m} \right).$$

$\frac{\Delta X}{X}$  the change of horizontal force between the experiments of deflection and vibration, and  $\frac{\Delta m}{m}$  the difference

in the magnetic moment of the deflecting magnet, produced by the earth's inducing action, are determined from experiments with the Bifilar magnetometer—when this instrument is not used, as is the case in our observations and upon magnetic surveys generally, the formula becomes:

$$T^3 = \left\{ T' \left( 1 - \frac{r}{86400} - \frac{a a'}{16} \right) \right\}^3 \times \left( 1 + \frac{H}{F} \right) \\ \times \left( 1 - (t' - t) q \right)$$

where:

$T$  and  $T'$  = the true and observed times of vibration,

$r$  = the rate of the chronometer  $\left\{ \begin{array}{l} - \text{when losing,} \\ + \text{when gaining} \end{array} \right.$

$a$  and  $a'$  = the initial and terminal semi-arcs of vibration in parts of radius,

$\frac{H}{F}$  = the ratio of the torsion and magnetic forces,

$t$  = the temperature of the deflecting magnet during the experiments of deflection,

$t'$  = the temperature of the deflecting magnet during the experiments of vibration,

$q$  = the change of magnetic moment of the deflecting magnet for  $1^\circ$  of temperature.

The value of  $\frac{a a'}{16}$  is found by the formula:

$$\frac{a a'}{16} = a^2 d d' \times 0.00007272^2$$

where  $d, d'$  denote the semi-arcs of vibration in divisions of scale, and  $a$ , the angular value of 1 division.\*

$$q = \frac{1}{t - t_0} a \cdot n \cdot \cot u.$$

where  $a$  = the arc value of 1 division of scale in terms of radius,

$h$  = the difference of scale readings corrected for changes of declination,

$t - t_0$  = the corresponding difference of temperature,

$u$  = the angle of deflection at the lowest mean temperature.

*Final calculation of the results.*

By the observations of deflection, we have  $\frac{m}{X} = A$

By those of vibration, . . .  $m X = B$

$$\text{whence, } X = \sqrt{\frac{B}{A}}$$

$$\text{and } m = \sqrt{A B}.$$

\*The correction for arc, in an extreme case when the initial semi-arc was 36 scale divisions ( $1^\circ 40' 30''$ ), amounted to only 0.000037.

The correction for rate, when the chronometer loses 3 seconds per day, is 0.000084.

From examples in Riddell's Instructions, the value of the horizontal intensity is not carried beyond four decimal figures, and as these two corrections only change the fifth decimal, it will be, in most instances, needless to compute them, and the final formula would then be further reduced to

$$T^2 = T'^2 \times \left(1 + \frac{H}{F}\right) (1 - (t' - t) q).$$

The horizontal intensity being thus determined, the *Total Intensity* will be found by dividing the horizontal intensity by the cosine of the *Dip*, deduced from observations with the dipping needle.

#### OBSERVATIONS FOR THE DIP, OR ABSOLUTE INCLINATION.

In addition to the usual method of conducting observations of the Dip Circle, it is desirable that a few series should be made in different azimuths, for the purpose of testing the axles of the needles and the limb of the instrument (which is often magnetic;) if  $\eta$  denote the observed inclination of the needle,  $\theta$  the inclination sought,  $\alpha$  the azimuth of the vertical circle.

$$\tan \theta = \tan \eta \operatorname{co-sec} \alpha$$

The true inclination may be inferred also from the observed inclinations of the needle in any two planes at right angles to one another, without the knowledge of the angle  $\alpha$ , according to the formula

$$\cot^2 \theta = \cot^2 \eta + \cot^2 \eta'$$

The difference between the mean of the results obtained by observations in different azimuths, and the result obtained by observations in the magnetic meridian, should be applied as a constant correction for the errors of axle and limb to all preceding or subsequent observations made in the meridian.



*To compute, theoretically, the variations in the magnetic declination, due to changes in the Latitude and Longitude.*

In a system of rectangular co-ordinates of which  $z_0$  is the origin, let—

$z$  = declination at P.

$M$  = increase of declination in the direction,  $x$ .

$N$  = increase of declination in the direction,  $y$ .

$x$  = difference of longitude.

$y$  = difference of latitude.

At the origin,

$$\sum x = 0;$$

$$\sum y = 0;$$

$$n L = \sum z; \quad L = \frac{\sum z}{n}$$

$$M \sum x^2 + N \sum x y = \sum x z.$$

$$M \sum x y + N \sum y^2 = \sum y z.$$

Let  $z - L = K$ ; then,

Equation of the line passing through all the points of equal declination is,  $M x + N y = K$ , and the angle which it makes with the meridian.

$$= \arcsin \left( \tan \theta = - \frac{N}{M} \right)$$

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**TABLES AND FORMULÆ.**

**PART III.**

**ASTRONOMY.**

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## ASTRONOMY.

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### I. *Of Sidereal and Solar Time.*

*True or apparent Solar time* is that deduced from observations of the Sun, or is the same as that shown by a well adjusted sun-dial.

*Mean Solar Time* is derived from the time employed by the Earth in revolving on its axis, as compared with the Sun, supposed to move at a mean rate in its orbit, and to make 365.242218 revolutions in a mean Gregorian year. It cannot be immediately obtained from observation, but is always deduced from apparent time by the aid of the equation of time, which is the angular distance, in time, between the mean and true sun; or mean solar time = apparent solar time  $\pm$  equation of time.

*Sidereal Time* is the portion of a sidereal day which has elapsed since the transit of the first point of Aries. Its point of origin cannot be determined by observation, but it is known at any moment by the right ascension of whatever object may be then in the meridian, or

Sidereal time of a star's culmination = AR of \*

Sidereal time at mean moon = AR mean ☾ at mean moon; and, generally,

Sidereal time = sidereal time at mean moon  $\pm$  solar time from mean moon (expressed in sidereal intervals.)

Solar time = sidereal time — sidereal time at mean moon, (the difference being reduced to a solar interval.)

*Example—*

To find the mean solar time of the passage of Altair over the meridian of Washington, on the 10th July, 1849.

|                                                                                          |                                                         |
|------------------------------------------------------------------------------------------|---------------------------------------------------------|
| AR: Altair, July 10th, 1849 . . . . .                                                    | <sup>h</sup> <sup>m</sup> <sup>s</sup><br>= 19 43 27 39 |
| Sidereal time at mean moon at Washington . . . . .                                       | = 7 14 00.96                                            |
| Sidereal interval past Washington mean moon . . . . .                                    | = 12 29 26.43                                           |
| Retardation of mean on sidereal time . . . . .                                           | = — 2 02.27                                             |
| Corresponding mean time interval past mean moon or<br>mean time of culmination . . . . . | = 12 27 23.66                                           |

The nautical almanacs give the sidereal time at mean moon for each day of the year for a certain meridian.

If the sidereal day be taken equal to 24 sidereal hours, the mean solar day will be equal to  $24^h 03^m 56^s.55$  of those sidereal hours; or the daily acceleration of sidereal on mean solar time (which is the mean motion of the earth in a mean solar day,) is  $3^m 56^s.5554$  of sidereal time; hence the sidereal time at mean moon under any meridian other than that of the nautical almanac used, will be found by allowing the proportion of this quantity due to the difference of longitude of the two places.

If the mean solar day be taken equal to 24 mean solar hours, the sidereal day will be equal to  $23^h 56^m 04^s.09$  of those solar hours, or the daily retardation of mean solar on sidereal time is  $3^m 55^s.9093$  of solar time.

The astronomical day begins at noon. In the civil or common method of reckoning, the day is supposed to commence at the *preceding* midnight. The civil reckoning is therefore 12 hours in advance of the astronomical reckoning, and in the above example, July 10th,  $12^h 27^m 23^s.66$  astronomical time, corresponds to July 11th,  $0^h 27^m 23^s.66$  A. M. civil time.

## II. To find the time by an altitude of the Sun or a star.

Sidereal time = AR \*  $\pm$  \*'s hour angle,

Solar time = 24<sup>hr</sup>  $\pm$  ☉'s hour angle,

$$2 m = L + \Delta + A,$$

$$\sin^2 \frac{1}{2} p = \frac{\cos m \cdot \sin (m - A)}{\cos L \cdot \sin \Delta}, \text{ where}$$

$L$  = the latitude of the place of observation.

$\Delta$  = the north polar distance of the sun or the star.

$A$  = the corrected altitude of the sun or star.

= obs. alt. - (refrac'n - paral'x)  $\pm$  semi-diam.

$p$  = the hour angle of the sun or star.

The formula gives the arc in degrees, which must be converted into time, as in one of the following four cases:

1. When we have the *corrected* altitude of the sun's *centre*, the hour angle,  $p$ , in time, is the *apparent* time when the sun is in the west, or the complement of 24 hours when in the east. To reduce it to *mean* time apply the equation of time.

2. But should the *sidereal* time be required, transform the mean time thus obtained to sidereal time, as previously explained.

3. When the altitude is that of a star, the sidereal time is at once deduced from the hour angle  $p$ .

4. And if, in this last instance, solar time should be required, convert this sidereal time into solar time by means of the equation,

$$\text{Solar time} = \text{AR } * - \text{AR } \odot \pm p.$$

In which the sign  $+$  is used if the star is observed in the west, and the sign  $-$  if in the east; or,

Mean solar time = the mean solar equivalent of (sid. time of obs'n - sid'l time of preced'g mean moon at place.)

*For converting intervals of SIDEREAL into corresponding intervals of MEAN SOLAR time.*

| HOURS. |          | MINUTES. |       |    |       | SECONDS. |       |    |       |
|--------|----------|----------|-------|----|-------|----------|-------|----|-------|
| h.     | m. s.    | m.       | s.    | m. | s.    | s.       | s.    | s. | s.    |
| 1      | 0 9.830  | 1        | 0.164 | 31 | 5.079 | 1        | 0.003 | 31 | 0.085 |
| 2      | 0 19.659 | 2        | 0.328 | 32 | 5.242 | 2        | 0.005 | 32 | 0.087 |
| 3      | 0 29.489 | 3        | 0.491 | 33 | 5.406 | 3        | 0.008 | 33 | 0.090 |
| 4      | 0 39.318 | 4        | 0.655 | 34 | 5.570 | 4        | 0.011 | 34 | 0.093 |
| 5      | 0 49.148 | 5        | 0.819 | 35 | 5.734 | 5        | 0.014 | 35 | 0.096 |
| 6      | 0 58.977 | 6        | 0.983 | 36 | 5.898 | 6        | 0.016 | 36 | 0.098 |
| 7      | 1 8.807  | 7        | 1.147 | 37 | 6.062 | 7        | 0.019 | 37 | 0.101 |
| 8      | 1 18.636 | 8        | 1.311 | 38 | 6.225 | 8        | 0.022 | 38 | 0.104 |
| 9      | 1 28.466 | 9        | 1.474 | 39 | 6.389 | 9        | 0.025 | 39 | 0.106 |
| 10     | 1 38.296 | 10       | 1.638 | 40 | 6.553 | 10       | 0.027 | 40 | 0.109 |
| 11     | 1 48.125 | 11       | 1.802 | 41 | 6.717 | 11       | 0.030 | 41 | 0.112 |
| 12     | 1 57.955 | 12       | 1.966 | 42 | 6.881 | 12       | 0.033 | 42 | 0.115 |
| 13     | 2 7.784  | 13       | 2.130 | 43 | 7.044 | 13       | 0.036 | 43 | 0.118 |
| 14     | 2 17.614 | 14       | 2.294 | 44 | 7.208 | 14       | 0.038 | 44 | 0.120 |
| 15     | 2 27.443 | 15       | 2.457 | 45 | 7.372 | 15       | 0.041 | 45 | 0.123 |
| 16     | 2 37.273 | 16       | 2.621 | 46 | 7.536 | 16       | 0.044 | 46 | 0.126 |
| 17     | 2 47.103 | 17       | 2.785 | 47 | 7.700 | 17       | 0.047 | 47 | 0.128 |
| 18     | 2 56.932 | 18       | 2.949 | 48 | 7.864 | 18       | 0.049 | 48 | 0.131 |
| 19     | 3 6.762  | 19       | 3.113 | 49 | 8.027 | 19       | 0.052 | 49 | 0.134 |
| 20     | 3 16.591 | 20       | 3.277 | 50 | 8.191 | 20       | 0.055 | 50 | 0.137 |
| 21     | 3 26.421 | 21       | 3.440 | 51 | 8.355 | 21       | 0.057 | 51 | 0.140 |
| 22     | 3 36.250 | 22       | 3.604 | 52 | 8.519 | 22       | 0.060 | 52 | 0.142 |
| 23     | 3 46.080 | 23       | 3.768 | 53 | 8.683 | 23       | 0.063 | 53 | 0.145 |
| 24     | 3 55.909 | 24       | 3.932 | 54 | 8.847 | 24       | 0.066 | 54 | 0.148 |
|        |          | 25       | 4.096 | 55 | 9.010 | 25       | 0.068 | 55 | 0.150 |
|        |          | 26       | 4.259 | 56 | 9.174 | 26       | 0.071 | 56 | 0.153 |
|        |          | 27       | 4.423 | 57 | 9.338 | 27       | 0.074 | 57 | 0.156 |
|        |          | 28       | 4.587 | 58 | 9.502 | 28       | 0.076 | 58 | 0.159 |
|        |          | 29       | 4.751 | 59 | 9.666 | 29       | 0.079 | 59 | 0.161 |
|        |          | 30       | 4.915 | 60 | 9.830 | 30       | 0.082 | 60 | 0.164 |

The quantities taken from this table must be *subtracted* from a sidereal interval, to obtain the corresponding interval in mean solar time.

*For converting intervals of MEAN SOLAR Time into corresponding intervals of SIDEREAL Time.*

| HOURS. |          | MINUTES. |       |    |       | SECONDS. |       |    |       |
|--------|----------|----------|-------|----|-------|----------|-------|----|-------|
| h.     | m. s.    | m.       | s.    | m. | s.    | s.       | s.    | s. | s.    |
| 1      | 0 9.856  | 1        | 0.164 | 31 | 5.092 | 1        | 0.003 | 31 | 0.085 |
| 2      | 0 19.713 | 2        | 0.329 | 32 | 5.257 | 2        | 0.005 | 32 | 0.088 |
| 3      | 0 29.569 | 3        | 0.493 | 33 | 5.421 | 3        | 0.008 | 33 | 0.090 |
| 4      | 0 39.426 | 4        | 0.657 | 34 | 5.585 | 4        | 0.011 | 34 | 0.093 |
| 5      | 0 49.282 | 5        | 0.821 | 35 | 5.750 | 5        | 0.014 | 35 | 0.096 |
| 6      | 0 59.139 | 6        | 0.986 | 36 | 5.914 | 6        | 0.016 | 36 | 0.098 |
| 7      | 1 8.995  | 7        | 1.150 | 37 | 6.078 | 7        | 0.019 | 37 | 0.101 |
| 8      | 1 18.852 | 8        | 1.314 | 38 | 6.242 | 8        | 0.022 | 38 | 0.104 |
| 9      | 1 28.708 | 9        | 1.478 | 39 | 6.407 | 9        | 0.025 | 39 | 0.106 |
| 10     | 1 38.565 | 10       | 1.643 | 40 | 6.571 | 10       | 0.027 | 40 | 0.109 |
| 11     | 1 48.421 | 11       | 1.807 | 41 | 6.735 | 11       | 0.030 | 41 | 0.112 |
| 12     | 1 58.278 | 12       | 1.971 | 42 | 6.900 | 12       | 0.033 | 42 | 0.115 |
| 13     | 2 8.134  | 13       | 2.136 | 43 | 7.064 | 13       | 0.036 | 43 | 0.118 |
| 14     | 2 17.991 | 14       | 2.300 | 44 | 7.228 | 14       | 0.038 | 44 | 0.120 |
| 15     | 2 27.847 | 15       | 2.464 | 45 | 7.392 | 15       | 0.041 | 45 | 0.123 |
| 16     | 2 37.704 | 16       | 2.628 | 46 | 7.557 | 16       | 0.044 | 46 | 0.126 |
| 17     | 2 47.560 | 17       | 2.793 | 47 | 7.721 | 17       | 0.047 | 47 | 0.128 |
| 18     | 2 57.416 | 18       | 2.957 | 48 | 7.885 | 18       | 0.049 | 48 | 0.131 |
| 19     | 3 7.273  | 19       | 3.121 | 49 | 8.050 | 19       | 0.052 | 49 | 0.134 |
| 20     | 3 17.129 | 20       | 3.285 | 50 | 8.214 | 20       | 0.055 | 50 | 0.137 |
| 21     | 3 26.986 | 21       | 3.450 | 51 | 8.378 | 21       | 0.057 | 51 | 0.140 |
| 22     | 3 36.842 | 22       | 3.614 | 52 | 8.542 | 22       | 0.060 | 52 | 0.142 |
| 23     | 3 46.699 | 23       | 3.778 | 53 | 8.707 | 23       | 0.063 | 53 | 0.145 |
| 24     | 4 56.555 | 24       | 3.943 | 54 | 8.871 | 24       | 0.066 | 54 | 0.148 |
|        |          | 25       | 4.107 | 55 | 9.035 | 25       | 0.068 | 55 | 0.151 |
|        |          | 26       | 4.271 | 56 | 9.199 | 26       | 0.071 | 56 | 0.153 |
|        |          | 27       | 4.436 | 57 | 9.364 | 27       | 0.074 | 57 | 0.156 |
|        |          | 28       | 4.600 | 58 | 9.528 | 28       | 0.077 | 58 | 0.159 |
|        |          | 29       | 4.764 | 59 | 9.692 | 29       | 0.079 | 59 | 0.161 |
|        |          | 30       | 4.928 | 60 | 9.856 | 30       | 0.082 | 60 | 0.164 |

The quantities taken from this table must be *added* to a mean interval, to obtain the corresponding interval in sidereal time.



*To convert parts of the Equator in Arc into Sidereal Time,  
or to convert Terrestrial Longitude in Arc into Time.*

## DEGREES.

| Arc. | Time. | Arc. | Time. | Arc. | Time. | Arc. | Time. |
|------|-------|------|-------|------|-------|------|-------|
| °    | h m   | °    | h m   | °    | h m   | °    | h m   |
| 1    | 0 4   | 31   | 2 4   | 61   | 4 4   | 91   | 6 4   |
| 2    | 0 8   | 32   | 2 8   | 62   | 4 8   | 92   | 6 8   |
| 3    | 0 12  | 33   | 2 12  | 63   | 4 12  | 93   | 6 12  |
| 4    | 0 16  | 34   | 2 16  | 64   | 4 16  | 94   | 6 16  |
| 5    | 0 20  | 35   | 2 20  | 65   | 4 20  | 95   | 6 20  |
| 6    | 0 24  | 36   | 2 24  | 66   | 4 24  | 96   | 6 24  |
| 7    | 0 28  | 37   | 2 28  | 67   | 4 28  | 97   | 6 28  |
| 8    | 0 32  | 38   | 2 32  | 68   | 4 32  | 98   | 6 32  |
| 9    | 0 36  | 39   | 2 36  | 69   | 4 36  | 99   | 6 36  |
| 10   | 0 40  | 40   | 2 40  | 70   | 4 40  | 100  | 6 40  |
| 11   | 0 44  | 41   | 2 44  | 71   | 4 44  | 101  | 6 44  |
| 12   | 0 48  | 42   | 2 48  | 72   | 4 48  | 102  | 6 48  |
| 13   | 0 52  | 43   | 2 52  | 73   | 4 52  | 103  | 6 52  |
| 14   | 0 56  | 44   | 2 56  | 74   | 4 56  | 104  | 6 56  |
| 15   | 1 0   | 45   | 3 0   | 75   | 5 0   | 105  | 7 0   |
| 16   | 1 4   | 46   | 3 4   | 76   | 5 4   | 106  | 7 4   |
| 17   | 1 8   | 47   | 3 8   | 77   | 5 8   | 107  | 7 8   |
| 18   | 1 12  | 48   | 3 12  | 78   | 5 12  | 108  | 7 12  |
| 19   | 1 16  | 49   | 3 16  | 79   | 5 16  | 109  | 7 16  |
| 20   | 1 20  | 50   | 3 20  | 80   | 5 20  | 110  | 7 20  |
| 21   | 1 24  | 51   | 3 24  | 81   | 5 24  | 111  | 7 24  |
| 22   | 1 28  | 52   | 3 28  | 82   | 5 28  | 112  | 7 28  |
| 23   | 1 32  | 53   | 3 32  | 83   | 5 32  | 113  | 7 32  |
| 24   | 1 36  | 54   | 3 36  | 84   | 5 36  | 114  | 7 36  |
| 25   | 1 40  | 55   | 3 40  | 85   | 5 40  | 115  | 7 40  |
| 26   | 1 44  | 56   | 3 44  | 86   | 5 44  | 116  | 7 44  |
| 27   | 1 48  | 57   | 3 48  | 87   | 5 48  | 117  | 7 48  |
| 28   | 1 52  | 58   | 3 52  | 88   | 5 52  | 118  | 7 52  |
| 29   | 1 56  | 59   | 3 56  | 89   | 5 56  | 119  | 7 56  |
| 30   | 2 0   | 60   | 4 0   | 90   | 6 0   | 120  | 8 0   |

*To convert parts of the Equator in Arc into Sidereal Time,  
or to convert Terrestrial Longitude in Arc into Time.*

## DEGREES.

| Arc. | Time. | Arc. | Time. | Arc. | Time. | Arc. | Time. |
|------|-------|------|-------|------|-------|------|-------|
| °    | h m   | °    | h m   | °    | h m   | °    | h m   |
| 121  | 8 4   | 151  | 10 4  | 181  | 12 4  | 211  | 14 4  |
| 122  | 8 8   | 152  | 10 8  | 182  | 12 8  | 212  | 14 8  |
| 123  | 8 12  | 153  | 10 12 | 183  | 12 12 | 213  | 14 12 |
| 124  | 8 16  | 154  | 10 16 | 184  | 12 16 | 214  | 14 16 |
| 125  | 8 20  | 155  | 10 20 | 185  | 12 20 | 215  | 14 20 |
| 126  | 8 24  | 156  | 10 24 | 186  | 12 24 | 216  | 14 24 |
| 127  | 8 28  | 157  | 10 28 | 187  | 12 28 | 217  | 14 28 |
| 128  | 8 32  | 158  | 10 32 | 188  | 12 32 | 218  | 14 32 |
| 129  | 8 36  | 159  | 10 36 | 189  | 12 36 | 219  | 14 36 |
| 130  | 8 40  | 160  | 10 40 | 190  | 12 40 | 220  | 14 40 |
| 131  | 8 44  | 161  | 10 44 | 191  | 12 44 | 221  | 14 44 |
| 132  | 8 48  | 162  | 10 48 | 192  | 12 48 | 222  | 14 48 |
| 133  | 8 52  | 163  | 10 52 | 193  | 12 52 | 223  | 14 52 |
| 134  | 8 56  | 164  | 10 56 | 194  | 12 56 | 224  | 14 56 |
| 135  | 9 0   | 165  | 11 0  | 195  | 13 0  | 225  | 15 0  |
| 136  | 9 4   | 166  | 11 4  | 196  | 13 4  | 226  | 15 4  |
| 137  | 9 8   | 167  | 11 8  | 197  | 13 8  | 227  | 15 8  |
| 138  | 9 12  | 168  | 11 12 | 198  | 13 12 | 228  | 15 12 |
| 139  | 9 16  | 169  | 11 16 | 199  | 13 16 | 229  | 15 16 |
| 140  | 9 20  | 170  | 11 20 | 200  | 13 20 | 230  | 15 20 |
| 141  | 9 24  | 171  | 11 24 | 201  | 13 24 | 231  | 15 24 |
| 142  | 9 28  | 172  | 11 28 | 202  | 13 28 | 232  | 15 28 |
| 143  | 9 32  | 173  | 11 32 | 203  | 13 32 | 233  | 15 32 |
| 144  | 9 36  | 174  | 11 36 | 204  | 13 36 | 234  | 15 36 |
| 145  | 9 40  | 175  | 11 40 | 205  | 13 40 | 235  | 15 40 |
| 146  | 9 44  | 176  | 11 44 | 206  | 13 44 | 236  | 15 44 |
| 147  | 9 48  | 177  | 11 48 | 207  | 13 48 | 237  | 15 48 |
| 148  | 9 52  | 178  | 11 52 | 208  | 13 52 | 238  | 15 52 |
| 149  | 9 56  | 179  | 11 56 | 209  | 13 56 | 239  | 15 56 |
| 150  | 10 0  | 180  | 12 0  | 210  | 14 0  | 240  | 16 0  |

*To convert parts of the Equator in Arc into Sidereal Time,  
or to convert Terrestrial Longitude in Arc into Time.*

## DEGREES.

| Arc. | Time. | Arc. | Time. | Arc. | Time. | Arc. | Time. |
|------|-------|------|-------|------|-------|------|-------|
| °    | h m   | °    | h m   | °    | h m   | °    | h m   |
| 241  | 16 4  | 271  | 18 4  | 301  | 20 4  | 331  | 22 4  |
| 242  | 16 8  | 272  | 18 8  | 302  | 20 8  | 332  | 22 8  |
| 243  | 16 12 | 273  | 18 12 | 303  | 20 12 | 333  | 22 12 |
| 244  | 16 16 | 274  | 18 16 | 304  | 20 16 | 334  | 22 16 |
| 245  | 16 20 | 275  | 18 20 | 305  | 20 20 | 335  | 22 20 |
| 246  | 16 24 | 276  | 18 24 | 306  | 20 24 | 336  | 22 24 |
| 247  | 16 28 | 277  | 18 28 | 307  | 20 28 | 337  | 22 28 |
| 248  | 16 32 | 278  | 18 32 | 308  | 20 32 | 338  | 22 32 |
| 249  | 16 36 | 279  | 18 36 | 309  | 20 36 | 339  | 22 36 |
| 250  | 16 40 | 280  | 18 40 | 310  | 20 40 | 340  | 22 40 |
| 251  | 16 44 | 281  | 18 44 | 311  | 20 44 | 341  | 22 44 |
| 252  | 16 48 | 282  | 18 48 | 312  | 20 48 | 342  | 22 48 |
| 253  | 16 52 | 283  | 18 52 | 313  | 20 52 | 343  | 22 52 |
| 254  | 16 56 | 284  | 18 56 | 314  | 20 56 | 344  | 22 56 |
| 255  | 17 0  | 285  | 19 0  | 315  | 21 0  | 345  | 23 0  |
| 256  | 17 4  | 286  | 19 4  | 316  | 21 4  | 346  | 23 4  |
| 257  | 17 8  | 287  | 19 8  | 317  | 21 8  | 347  | 23 8  |
| 258  | 17 12 | 288  | 19 12 | 318  | 21 12 | 348  | 23 12 |
| 259  | 17 16 | 289  | 19 16 | 319  | 21 16 | 349  | 23 16 |
| 260  | 17 20 | 290  | 19 20 | 320  | 21 20 | 350  | 23 20 |
| 261  | 17 24 | 291  | 19 24 | 321  | 21 24 | 351  | 23 24 |
| 262  | 17 28 | 292  | 19 28 | 322  | 21 28 | 352  | 23 28 |
| 263  | 17 32 | 293  | 19 32 | 323  | 21 32 | 353  | 23 32 |
| 264  | 17 36 | 294  | 19 36 | 324  | 21 36 | 354  | 23 36 |
| 265  | 17 40 | 295  | 19 40 | 325  | 21 40 | 355  | 23 40 |
| 266  | 17 44 | 296  | 19 44 | 326  | 21 44 | 356  | 23 44 |
| 267  | 17 48 | 297  | 19 48 | 327  | 21 48 | 357  | 23 48 |
| 268  | 17 52 | 298  | 19 52 | 328  | 21 52 | 358  | 23 52 |
| 269  | 17 56 | 299  | 19 56 | 329  | 21 56 | 359  | 23 56 |
| 270  | 18 0  | 300  | 20 0  | 330  | 22 0  | 360  | 24 0  |

*To convert parts of the Equator in Arc into Sidereal Time  
or to convert Terrestrial Longitude in Arc into Time.*

| MINUTES. |       |      |       | SECONDS. |       |      |       |
|----------|-------|------|-------|----------|-------|------|-------|
| Arc.     | Time. | Arc. | Time. | Arc.     | Time. | Arc. | Time. |
| '        | m s   | '    | m s   | "        | s     | "    | s     |
| 1        | 0 4   | 31   | 2 4   | 1        | 0.067 | 31   | 2.067 |
| 2        | 0 8   | 32   | 2 8   | 2        | 0.133 | 32   | 2.133 |
| 3        | 0 12  | 33   | 2 12  | 3        | 0.200 | 33   | 2.200 |
| 4        | 0 16  | 34   | 2 16  | 4        | 0.267 | 34   | 2.267 |
| 5        | 0 20  | 35   | 2 20  | 5        | 0.333 | 35   | 2.333 |
| 6        | 0 24  | 36   | 2 24  | 6        | 0.400 | 36   | 2.400 |
| 7        | 0 28  | 37   | 2 28  | 7        | 0.467 | 37   | 2.467 |
| 8        | 0 32  | 38   | 2 32  | 8        | 0.533 | 38   | 2.533 |
| 9        | 0 36  | 39   | 2 36  | 9        | 0.600 | 39   | 2.600 |
| 10       | 0 40  | 40   | 2 40  | 10       | 0.667 | 40   | 2.667 |
| 11       | 0 44  | 41   | 2 44  | 11       | 0.733 | 41   | 2.733 |
| 12       | 0 48  | 42   | 2 48  | 12       | 0.800 | 42   | 2.800 |
| 13       | 0 52  | 43   | 2 52  | 13       | 0.867 | 43   | 2.867 |
| 14       | 0 56  | 44   | 2 56  | 14       | 0.933 | 44   | 2.933 |
| 15       | 1 0   | 45   | 3 0   | 15       | 1.000 | 45   | 3.000 |
| 16       | 1 4   | 46   | 3 4   | 16       | 1.067 | 46   | 3.067 |
| 17       | 1 8   | 47   | 3 8   | 17       | 1.133 | 47   | 3.133 |
| 18       | 1 12  | 48   | 3 12  | 18       | 1.200 | 48   | 3.200 |
| 19       | 1 16  | 49   | 3 16  | 19       | 1.267 | 49   | 3.267 |
| 20       | 1 20  | 50   | 3 20  | 20       | 1.333 | 50   | 3.333 |
| 21       | 1 24  | 51   | 3 24  | 21       | 1.400 | 51   | 3.400 |
| 22       | 1 28  | 52   | 3 28  | 22       | 1.467 | 52   | 3.467 |
| 23       | 1 32  | 53   | 3 32  | 23       | 1.533 | 53   | 3.533 |
| 24       | 1 36  | 54   | 3 36  | 24       | 1.600 | 54   | 3.600 |
| 25       | 1 40  | 55   | 3 40  | 25       | 1.667 | 55   | 3.667 |
| 26       | 1 44  | 56   | 3 44  | 26       | 1.733 | 56   | 3.733 |
| 27       | 1 48  | 57   | 3 48  | 27       | 1.800 | 57   | 3.800 |
| 28       | 1 52  | 58   | 3 52  | 28       | 1.867 | 58   | 3.867 |
| 29       | 1 56  | 59   | 3 56  | 29       | 1.933 | 59   | 3.933 |
| 30       | 2 0   | 60   | 4 0   | 30       | 2.000 | 60   | 4.000 |

*To convert Sidereal Time into parts of the Equator in Arc,  
or to convert Time into Terrestrial Longitude in Arc.*

| HOURS. |      | MINUTES. |      |      |       | SECONDS. |      |      |       |
|--------|------|----------|------|------|-------|----------|------|------|-------|
| Time   | Arc. | Time     | Arc. | Time | Arc.  | Time     | Arc. | Time | Arc.  |
| h      | o    | m        | o    | m    | o     | s        | '    | s    | '     |
| 1      | 15   | 1        | 0 15 | 31   | 7 45  | 1        | 0 15 | 31   | 7 45  |
| 2      | 30   | 2        | 0 30 | 32   | 8 0   | 2        | 0 30 | 32   | 8 0   |
| 3      | 45   | 3        | 0 45 | 33   | 8 15  | 3        | 0 45 | 33   | 8 15  |
| 4      | 60   | 4        | 1 0  | 34   | 8 30  | 4        | 1 0  | 34   | 8 30  |
| 5      | 75   | 5        | 1 15 | 35   | 8 45  | 5        | 1 15 | 35   | 8 45  |
| 6      | 90   | 6        | 1 30 | 36   | 9 0   | 6        | 1 30 | 36   | 9 0   |
| 7      | 105  | 7        | 1 45 | 37   | 9 15  | 7        | 1 45 | 37   | 9 15  |
| 8      | 120  | 8        | 2 0  | 38   | 9 30  | 8        | 2 0  | 38   | 9 30  |
| 9      | 135  | 9        | 2 15 | 39   | 9 45  | 9        | 2 15 | 39   | 9 45  |
| 10     | 150  | 10       | 2 30 | 40   | 10 0  | 10       | 2 30 | 40   | 10 0  |
| 11     | 165  | 11       | 2 45 | 41   | 10 15 | 11       | 2 45 | 41   | 10 15 |
| 12     | 180  | 12       | 3 0  | 42   | 10 30 | 12       | 3 0  | 42   | 10 30 |
| 13     | 195  | 13       | 3 15 | 43   | 10 45 | 13       | 3 15 | 43   | 10 45 |
| 14     | 210  | 14       | 3 30 | 44   | 11 0  | 14       | 3 30 | 44   | 11 0  |
| 15     | 225  | 15       | 3 45 | 45   | 11 15 | 15       | 3 45 | 45   | 11 15 |
| 16     | 240  | 16       | 4 0  | 46   | 11 30 | 16       | 4 0  | 46   | 11 30 |
| 17     | 255  | 17       | 4 15 | 47   | 11 45 | 17       | 4 15 | 47   | 11 45 |
| 18     | 270  | 18       | 4 30 | 48   | 12 0  | 18       | 4 30 | 48   | 12 0  |
| 19     | 285  | 19       | 4 45 | 49   | 12 15 | 19       | 4 45 | 49   | 12 15 |
| 20     | 300  | 20       | 5 0  | 50   | 12 30 | 20       | 5 0  | 50   | 13 30 |
| 21     | 315  | 21       | 5 15 | 51   | 12 45 | 21       | 5 15 | 51   | 13 45 |
| 22     | 330  | 22       | 5 30 | 52   | 13 0  | 22       | 5 30 | 52   | 13 0  |
| 23     | 345  | 23       | 5 45 | 53   | 13 15 | 23       | 5 45 | 53   | 13 15 |
| 24     | 360  | 24       | 6 0  | 54   | 13 30 | 24       | 6 0  | 54   | 13 30 |
|        |      | 25       | 6 15 | 55   | 13 45 | 25       | 6 15 | 55   | 13 45 |
|        |      | 26       | 6 30 | 56   | 14 0  | 26       | 6 30 | 56   | 14 0  |
|        |      | 27       | 6 45 | 57   | 14 15 | 27       | 6 45 | 57   | 14 15 |
|        |      | 28       | 7 0  | 58   | 14 30 | 28       | 7 0  | 58   | 14 30 |
|        |      | 29       | 7 15 | 59   | 14 45 | 29       | 7 15 | 59   | 14 45 |
|        |      | 30       | 7 30 | 60   | 15 0  | 30       | 7 30 | 60   | 15 0  |

*To convert Sidereal Time into parts of the Equator in Arc,  
or to convert Time into Terrestrial Longitude in Arc.*

## TENTHS OF SECONDS.

| Time. | Arc. | Time. | Arc. | Time. | Arc.  | Time.                         | Arc.  |
|-------|------|-------|------|-------|-------|-------------------------------|-------|
| s     | "    | s     | "    | s     | "     | s                             | "     |
| 0.01  | 0.15 | 0.31  | 4.65 | 0.61  | 9.15  | 0.91                          | 13.65 |
| 0.02  | 0.30 | 0.32  | 4.80 | 0.62  | 9.30  | 0.92                          | 13.80 |
| 0.03  | 0.45 | 0.33  | 4.95 | 0.63  | 9.45  | 0.93                          | 13.95 |
| 0.04  | 0.60 | 0.34  | 5.10 | 0.64  | 9.60  | 0.94                          | 14.10 |
| 0.05  | 0.75 | 0.35  | 5.25 | 0.65  | 9.75  | 0.95                          | 14.25 |
| 0.06  | 0.90 | 0.36  | 5.40 | 0.66  | 9.90  | 0.96                          | 14.40 |
| 0.07  | 1.05 | 0.37  | 5.55 | 0.67  | 10.05 | 0.97                          | 14.55 |
| 0.08  | 1.20 | 0.38  | 5.70 | 0.68  | 10.20 | 0.98                          | 14.70 |
| 0.09  | 1.35 | 0.39  | 5.85 | 0.69  | 10.35 | 0.99                          | 14.85 |
| 0.10  | 1.50 | 0.40  | 6.00 | 0.70  | 10.50 | 1.00                          | 15.00 |
| 0.11  | 1.65 | 0.41  | 6.15 | 0.71  | 10.65 | Thousands of seconds of Time. | Arc.  |
| 0.12  | 1.80 | 0.42  | 6.30 | 0.72  | 10.80 |                               |       |
| 0.13  | 1.95 | 0.43  | 6.45 | 0.73  | 10.95 |                               |       |
| 0.14  | 2.10 | 0.44  | 6.60 | 0.74  | 11.10 |                               |       |
| 0.15  | 2.25 | 0.45  | 6.75 | 0.75  | 11.25 |                               |       |
| 0.16  | 2.40 | 0.46  | 6.90 | 0.76  | 11.40 |                               |       |
| 0.17  | 2.55 | 0.47  | 7.05 | 0.77  | 11.55 |                               |       |
| 0.18  | 2.70 | 0.48  | 7.20 | 0.78  | 11.70 |                               |       |
| 0.19  | 2.85 | 0.49  | 7.35 | 0.79  | 11.85 |                               |       |
| 0.20  | 3.00 | 0.50  | 7.50 | 0.80  | 12.00 |                               |       |
| 0.21  | 3.15 | 0.51  | 7.65 | 0.81  | 12.15 | .001                          | 0.015 |
| 0.22  | 3.30 | 0.52  | 7.80 | 0.82  | 12.30 | .002                          | 0.030 |
| 0.23  | 3.45 | 0.53  | 7.95 | 0.83  | 12.45 | .003                          | 0.045 |
| 0.24  | 3.60 | 0.54  | 8.10 | 0.84  | 12.60 | .004                          | 0.060 |
| 0.25  | 3.75 | 0.55  | 8.25 | 0.85  | 12.75 | .005                          | 0.075 |
| 0.26  | 3.90 | 0.56  | 8.40 | 0.86  | 12.90 | .006                          | 0.090 |
| 0.27  | 4.05 | 0.57  | 8.55 | 0.87  | 13.05 | .007                          | 0.105 |
| 0.28  | 4.20 | 0.58  | 8.70 | 0.88  | 13.20 | .008                          | 0.120 |
| 0.29  | 4.35 | 0.59  | 8.85 | 0.89  | 13.35 | .009                          | 0.135 |
| 0.30  | 4.50 | 0.60  | 9.00 | 0.90  | 13.50 | .010                          | 0.150 |

*To convert Right Ascension in Arc into Mean Time.*

## DEGREES.

| R. A.<br>in Arc | Mean Time.  | R. A.<br>in Arc. | Mean Time.  | R. A.<br>in Arc | Mean Time.  |
|-----------------|-------------|------------------|-------------|-----------------|-------------|
| °               | h m s       | °                | h m s       | °               | h m s       |
| 1               | 0 3 59.345  | 31               | 2 3 39.686  | 61              | 4 3 20.027  |
| 2               | 0 7 59.689  | 32               | 2 7 39.030  | 62              | 4 7 19.371  |
| 3               | 0 11 59.034 | 33               | 2 11 38.375 | 63              | 5 11 18.716 |
| 4               | 0 15 57.379 | 34               | 2 15 37.720 | 64              | 4 15 18.061 |
| 5               | 0 19 56.724 | 35               | 2 19 37.064 | 65              | 4 19 17.405 |
| 6               | 0 23 56.068 | 36               | 2 23 36.409 | 66              | 4 23 16.750 |
| 7               | 0 27 55.413 | 37               | 2 27 35.754 | 67              | 4 27 16.095 |
| 8               | 0 31 54.758 | 38               | 2 31 35.099 | 68              | 4 31 15.639 |
| 9               | 0 35 54.102 | 39               | 2 35 34.443 | 69              | 4 35 14.784 |
| 10              | 0 39 53.447 | 40               | 2 39 33.788 | 70              | 4 39 14.129 |
| 11              | 0 43 52.792 | 41               | 2 43 33.133 | 71              | 4 43 13.474 |
| 12              | 0 47 52.136 | 42               | 2 47 32.477 | 72              | 4 47 12.818 |
| 13              | 0 51 51.481 | 43               | 2 51 31.822 | 73              | 4 51 12.163 |
| 14              | 0 55 50.826 | 44               | 2 55 31.167 | 74              | 4 55 11.508 |
| 15              | 0 59 50.170 | 45               | 2 59 30.511 | 75              | 4 59 10.852 |
| 16              | 1 3 49.515  | 46               | 3 3 29.856  | 76              | 5 3 10.197  |
| 17              | 1 7 48.860  | 47               | 3 7 29.201  | 77              | 5 7 9.542   |
| 18              | 1 11 48.205 | 48               | 3 11 28.545 | 78              | 5 11 8.886  |
| 19              | 1 15 47.549 | 49               | 3 15 27.890 | 79              | 5 15 8.231  |
| 20              | 1 19 46.894 | 50               | 3 19 27.235 | 80              | 5 19 7.576  |
| 21              | 1 23 46.239 | 51               | 3 23 26.580 | 81              | 5 23 6.920  |
| 22              | 1 27 45.583 | 52               | 3 27 25.924 | 82              | 5 27 6.265  |
| 23              | 1 31 44.928 | 53               | 3 31 25.269 | 83              | 5 31 5.610  |
| 24              | 1 35 44.273 | 54               | 3 35 24.614 | 84              | 5 35 4.955  |
| 25              | 1 39 43.617 | 55               | 3 39 23.958 | 85              | 5 39 4.299  |
| 26              | 1 43 42.962 | 56               | 3 43 23.303 | 86              | 5 43 3.644  |
| 27              | 1 47 42.307 | 57               | 3 47 22.648 | 87              | 5 47 2.989  |
| 28              | 1 51 41.652 | 58               | 3 51 21.992 | 88              | 5 51 2.333  |
| 29              | 1 55 40.996 | 59               | 3 55 21.337 | 89              | 5 55 1.678  |
| 30              | 1 59 40.341 | 60               | 3 59 20.682 | 90              | 5 59 1.023  |

*To convert Right Ascension in Arc into Mean Time.*

## DEGREES.

| R. A.<br>in Arc. | Mean Time.  | R. A.<br>in Arc. | Mean Time.  | R. A.<br>in Arc. | Mean Time.   |
|------------------|-------------|------------------|-------------|------------------|--------------|
| °                | h m s       | °                | h m s       | °                | h m s        |
| 91               | 6 3 0.367   | 121              | 8 2 40.708  | 151              | 10 2 21.049  |
| 92               | 6 6 59.712  | 122              | 8 6 40.053  | 152              | 10 6 20.394  |
| 93               | 6 10 59.057 | 123              | 8 10 39.398 | 153              | 10 10 19.738 |
| 94               | 6 14 58.401 | 124              | 8 14 38.742 | 154              | 10 14 19.083 |
| 95               | 6 18 57.746 | 125              | 8 18 38.087 | 155              | 10 18 18.428 |
| 96               | 6 22 57.091 | 126              | 8 22 37.432 | 156              | 10 22 17.773 |
| 97               | 6 26 56.436 | 127              | 8 26 36.776 | 157              | 10 26 17.117 |
| 98               | 6 30 55.780 | 128              | 8 30 36.121 | 158              | 10 30 16.462 |
| 99               | 6 34 55.125 | 129              | 8 34 35.466 | 159              | 10 34 15.807 |
| 100              | 6 38 54.470 | 130              | 8 38 34.810 | 160              | 10 38 15.151 |
| 101              | 6 42 53.814 | 131              | 8 42 34.155 | 161              | 10 42 14.496 |
| 102              | 6 46 53.159 | 132              | 8 46 33.500 | 162              | 10 46 13.841 |
| 103              | 6 50 52.504 | 133              | 8 50 32.845 | 163              | 10 50 13.185 |
| 104              | 6 54 51.848 | 134              | 8 54 32.189 | 164              | 10 54 12.530 |
| 105              | 6 58 51.193 | 135              | 8 58 31.534 | 165              | 10 58 11.875 |
| 106              | 7 2 50.538  | 136              | 9 2 30.879  | 166              | 11 2 11.220  |
| 107              | 7 6 49.883  | 137              | 9 6 30.223  | 167              | 11 6 10.564  |
| 108              | 7 10 49.227 | 138              | 9 10 29.568 | 168              | 11 10 9.909  |
| 109              | 7 14 48.572 | 139              | 9 14 28.913 | 169              | 11 14 9.254  |
| 110              | 7 18 47.917 | 140              | 9 18 28.257 | 170              | 11 18 8.598  |
| 111              | 7 22 47.261 | 141              | 9 22 27.602 | 171              | 11 22 7.943  |
| 112              | 7 26 46.606 | 142              | 9 26 26.947 | 172              | 11 26 7.288  |
| 113              | 7 30 45.951 | 143              | 9 30 26.292 | 173              | 11 30 6.632  |
| 114              | 7 34 45.295 | 144              | 9 34 25.636 | 174              | 11 34 5.977  |
| 115              | 7 38 44.640 | 145              | 9 38 24.981 | 175              | 11 38 5.322  |
| 116              | 7 42 43.985 | 146              | 9 42 24.326 | 176              | 11 42 4.666  |
| 117              | 7 46 43.329 | 147              | 9 46 23.670 | 177              | 11 46 4.011  |
| 118              | 7 50 42.674 | 148              | 9 50 23.015 | 178              | 11 50 3.356  |
| 119              | 7 54 42.019 | 149              | 9 54 22.360 | 179              | 11 54 2.701  |
| 120              | 7 58 41.364 | 150              | 9 58 21.704 | 180              | 11 58 2.045  |



*To convert Right Ascension in Arc into Mean Time.*

| MINUTES.         |            |                  |            | SECONDS.         |            |                  |            |
|------------------|------------|------------------|------------|------------------|------------|------------------|------------|
| R. A.<br>in Arc. | Mean Time. | R. A.<br>in Arc. | Mean Time. | R. A.<br>in Arc. | Mean Time. | R. A.<br>in Arc. | Mean Time. |
| /                | m. s.      | /                | m. s.      | "                | s.         | "                | s.         |
| 1                | 0 3.989    | 31               | 2 3.661    | 1                | 0.066      | 31               | 2.061      |
| 2                | 0 7.978    | 32               | 2 7.650    | 2                | 0.133      | 32               | 2.128      |
| 3                | 0 11.969   | 33               | 2 11.640   | 3                | 0.199      | 33               | 2.194      |
| 4                | 0 15.956   | 34               | 2 15.629   | 4                | 0.266      | 34               | 2.261      |
| 5                | 0 19.945   | 35               | 2 19.618   | 5                | 0.332      | 35               | 2.327      |
| 6                | 0 23.935   | 36               | 2 23.607   | 6                | 0.399      | 36               | 2.393      |
| 7                | 0 27.924   | 37               | 2 27.596   | 7                | 0.465      | 37               | 2.460      |
| 8                | 0 31.913   | 38               | 2 31.585   | 8                | 0.532      | 38               | 2.526      |
| 9                | 0 35.902   | 39               | 2 35.574   | 9                | 0.598      | 39               | 2.593      |
| 10               | 0 39.891   | 40               | 2 39.563   | 10               | 0.665      | 40               | 2.659      |
| 11               | 0 43.880   | 41               | 2 43.552   | 11               | 0.731      | 41               | 2.726      |
| 12               | 0 47.869   | 42               | 2 47.541   | 12               | 0.798      | 42               | 2.792      |
| 13               | 0 51.858   | 43               | 2 51.530   | 13               | 0.864      | 43               | 2.859      |
| 14               | 0 55.847   | 44               | 2 55.519   | 14               | 0.931      | 44               | 2.925      |
| 15               | 0 59.836   | 45               | 2 59.509   | 15               | 0.997      | 45               | 2.992      |
| 16               | 1 3.825    | 46               | 3 3.498    | 16               | 1.064      | 46               | 3.058      |
| 17               | 1 7.814    | 47               | 3 7.487    | 17               | 1.130      | 47               | 3.125      |
| 18               | 1 11.803   | 48               | 3 11.476   | 18               | 1.197      | 48               | 3.191      |
| 19               | 1 15.793   | 49               | 3 15.465   | 19               | 1.263      | 49               | 3.258      |
| 20               | 1 19.782   | 50               | 3 19.454   | 20               | 1.330      | 50               | 3.324      |
| 21               | 1 23.771   | 51               | 3 23.443   | 21               | 1.396      | 51               | 3.391      |
| 22               | 1 27.760   | 52               | 3 27.432   | 22               | 1.463      | 52               | 3.457      |
| 23               | 1 31.749   | 53               | 3 31.421   | 23               | 1.529      | 53               | 3.524      |
| 24               | 1 35.738   | 54               | 3 35.410   | 24               | 1.596      | 54               | 3.590      |
| 25               | 1 39.727   | 55               | 3 39.399   | 25               | 1.662      | 55               | 3.657      |
| 26               | 1 43.716   | 56               | 3 43.388   | 26               | 1.729      | 56               | 3.723      |
| 27               | 1 47.705   | 57               | 3 47.377   | 27               | 1.795      | 57               | 3.790      |
| 28               | 1 51.694   | 58               | 3 51.367   | 28               | 1.862      | 58               | 3.856      |
| 29               | 1 55.683   | 59               | 3 55.356   | 29               | 1.928      | 59               | 3.923      |
| 30               | 1 59.672   | 60               | 3 59.345   | 30               | 1.995      | 60               | 3.989      |

*To convert Mean Time into Right Ascension in Arc.*

| HOURS.     |               |    | MINUTES. |            |               |    |            |               |    |    |       |
|------------|---------------|----|----------|------------|---------------|----|------------|---------------|----|----|-------|
| Mean Time. | R. A. in Arc. |    |          | Mean Time. | R. A. in Arc. |    | Mean Time. | R. A. in Arc. |    |    |       |
| h          | °             | '  | "        | m          | °             | '  | "          | m             | °  | '  | "     |
| 1          | 15            | 2  | 27.85    | 1          | 0             | 15 | 2.46       | 31            | 7  | 46 | 16.39 |
| 2          | 30            | 4  | 52.69    | 2          | 0             | 30 | 4.93       | 32            | 8  | 1  | 18.85 |
| 3          | 45            | 7  | 23.54    | 3          | 0             | 45 | 30.39      | 33            | 8  | 16 | 21.31 |
| 4          | 60            | 9  | 51.39    | 4          | 1             | 0  | 9.86       | 34            | 8  | 31 | 23.78 |
| 5          | 75            | 12 | 19.24    | 5          | 1             | 15 | 12.32      | 35            | 8  | 46 | 26.24 |
| 6          | 90            | 14 | 47.08    | 6          | 1             | 30 | 14.79      | 36            | 9  | 1  | 28.71 |
| 7          | 105           | 17 | 14.93    | 7          | 1             | 45 | 17.25      | 37            | 9  | 16 | 31.17 |
| 8          | 120           | 19 | 42.78    | 8          | 2             | 0  | 19.71      | 38            | 9  | 31 | 33.64 |
| 9          | 135           | 22 | 10.62    | 9          | 2             | 15 | 22.18      | 39            | 9  | 46 | 36.10 |
| 10         | 150           | 24 | 38.47    | 10         | 2             | 30 | 24.64      | 40            | 10 | 1  | 38.57 |
| 11         | 165           | 27 | 6.32     | 11         | 2             | 45 | 27.11      | 41            | 10 | 16 | 41.03 |
| 12         | 180           | 29 | 34.16    | 12         | 3             | 0  | 29.57      | 42            | 10 | 31 | 43.39 |
| 13         | 195           | 32 | 2.01     | 13         | 3             | 15 | 32.03      | 43            | 10 | 46 | 45.96 |
| 14         | 210           | 34 | 29.86    | 14         | 3             | 30 | 34.50      | 44            | 11 | 1  | 48.42 |
| 15         | 225           | 36 | 57.70    | 15         | 3             | 45 | 36.96      | 45            | 11 | 16 | 50.89 |
| 16         | 240           | 39 | 25.55    | 16         | 4             | 0  | 39.43      | 46            | 11 | 31 | 53.35 |
| 17         | 255           | 41 | 53.40    | 17         | 4             | 15 | 41.89      | 47            | 11 | 46 | 55.81 |
| 18         | 270           | 44 | 21.24    | 18         | 4             | 30 | 44.35      | 48            | 12 | 1  | 58.38 |
| 19         | 285           | 46 | 49.09    | 19         | 4             | 45 | 46.82      | 49            | 12 | 17 | 0.74  |
| 20         | 300           | 49 | 16.94    | 20         | 5             | 0  | 49.28      | 50            | 12 | 32 | 3.21  |
| 21         | 315           | 51 | 44.78    | 21         | 5             | 15 | 51.75      | 51            | 12 | 47 | 5.57  |
| 22         | 330           | 54 | 12.63    | 22         | 5             | 30 | 54.21      | 52            | 13 | 2  | 8.13  |
| 23         | 345           | 56 | 40.48    | 23         | 5             | 45 | 56.67      | 53            | 13 | 17 | 10.60 |
| 24         | 360           | 59 | 8.33     | 24         | 6             | 0  | 59.14      | 54            | 13 | 32 | 13.06 |
|            |               |    |          | 25         | 6             | 16 | 1.60       | 55            | 13 | 47 | 15.53 |
|            |               |    |          | 26         | 6             | 31 | 4.07       | 56            | 14 | 2  | 17.99 |
|            |               |    |          | 27         | 6             | 46 | 6.53       | 57            | 14 | 17 | 20.45 |
|            |               |    |          | 28         | 7             | 1  | 9.00       | 58            | 14 | 32 | 22.92 |
|            |               |    |          | 29         | 7             | 16 | 11.46      | 59            | 14 | 47 | 25.38 |
|            |               |    |          | 30         | 7             | 31 | 13.92      | 60            | 15 | 2  | 27.85 |

*To convert Mean Time into Right Ascension in Arc.*

## SECONDS AND TENTHS.

| Mean Time. | R. A. in Arc. | Mean Time. | R. A. in Arc. | Mean Time. | R. A. in Arc. | Mean Time. | R. A. in Arc. |
|------------|---------------|------------|---------------|------------|---------------|------------|---------------|
| s          | ' "           | s          | ' "           | s          | "             | s          | "             |
| 1          | 0 15.04       | 31         | 7 46.27       | 0.01       | 0.15          | 0.31       | 4.66          |
| 2          | 0 30.08       | 32         | 8 1.31        | 0.02       | 0.30          | 0.32       | 4.81          |
| 3          | 0 45.12       | 33         | 8 16.36       | 0.03       | 0.45          | 0.33       | 4.96          |
| 4          | 1 0.16        | 34         | 8 31.40       | 0.04       | 0.60          | 0.34       | 5.12          |
| 5          | 1 15.21       | 35         | 8 46.44       | 0.05       | 0.75          | 0.35       | 5.27          |
| 6          | 1 30.25       | 36         | 9 1.48        | 0.06       | 0.90          | 0.36       | 5.42          |
| 7          | 1 45.29       | 37         | 9 16.52       | 0.07       | 1.05          | 0.37       | 5.57          |
| 8          | 2 0.33        | 38         | 9 31.56       | 0.08       | 1.20          | 0.38       | 5.72          |
| 9          | 2 15.37       | 39         | 9 46.60       | 0.09       | 1.35          | 0.39       | 5.87          |
| 10         | 2 30.41       | 40         | 10 1.64       | 0.10       | 1.50          | 0.40       | 6.02          |
| 11         | 2 45.45       | 41         | 10 16.68      | 0.11       | 1.65          | 0.41       | 6.17          |
| 12         | 3 0.49        | 42         | 10 31.73      | 0.12       | 1.81          | 0.42       | 6.32          |
| 13         | 3 15.53       | 43         | 10 46.77      | 0.13       | 1.96          | 0.43       | 6.47          |
| 14         | 3 30.58       | 44         | 11 1.81       | 0.14       | 2.11          | 0.44       | 6.62          |
| 15         | 3 45.62       | 45         | 11 16.85      | 0.15       | 2.26          | 0.45       | 6.77          |
| 16         | 4 0.66        | 46         | 11 31.89      | 0.16       | 2.41          | 0.46       | 6.92          |
| 17         | 4 15.70       | 47         | 11 46.93      | 0.17       | 2.56          | 0.47       | 7.07          |
| 18         | 4 30.74       | 48         | 12 1.97       | 0.18       | 2.71          | 0.48       | 7.22          |
| 19         | 4 45.78       | 49         | 12 17.01      | 0.19       | 2.86          | 0.49       | 7.37          |
| 20         | 5 0.82        | 50         | 12 32.05      | 0.20       | 3.01          | 0.50       | 7.52          |
| 21         | 5 15.86       | 51         | 12 47.09      | 0.21       | 3.16          | 0.51       | 7.67          |
| 22         | 5 30.90       | 52         | 13 2.14       | 0.22       | 3.31          | 0.52       | 7.82          |
| 23         | 5 45.94       | 53         | 13 17.18      | 0.23       | 3.46          | 0.53       | 7.97          |
| 24         | 6 1.00        | 54         | 13 32.22      | 0.24       | 3.61          | 0.54       | 8.12          |
| 25         | 6 16.03       | 55         | 13 47.26      | 0.25       | 3.76          | 0.55       | 8.27          |
| 26         | 6 31.07       | 56         | 14 2.30       | 0.26       | 3.91          | 0.56       | 8.43          |
| 27         | 6 46.11       | 57         | 14 17.34      | 0.27       | 4.06          | 0.57       | 8.58          |
| 28         | 7 1.15        | 58         | 14 32.38      | 0.28       | 4.21          | 0.58       | 8.73          |
| 29         | 7 16.19       | 59         | 14 47.42      | 0.29       | 4.36          | 0.59       | 8.88          |
| 30         | 7 31.23       | 60         | 15 2.46       | 0.30       | 4.51          | 0.60       | 9.03          |

*To convert Mean Time into Right Ascension in Arc.*

## SECONDS AND TENTHS.

| Mean Time. | R. A. in Arc. | Mean Time. | R. A. in Arc. | Mean Time. | R. A. in Arc. | Thousands of Seconds of Mean Time. | R. A. in Arc. |
|------------|---------------|------------|---------------|------------|---------------|------------------------------------|---------------|
| s          | "             | s          | "             | s          | "             |                                    |               |
| 0.61       | 9.18          | 0.76       | 11.43         | 0.91       | 13.69         |                                    |               |
| 0.62       | 9.33          | 0.77       | 11.58         | 0.92       | 13.84         |                                    |               |
| 0.63       | 9.48          | 0.78       | 11.74         | 0.93       | 13.99         |                                    |               |
| 0.64       | 9.63          | 0.79       | 11.89         | 0.94       | 14.14         |                                    |               |
| 0.65       | 9.78          | 0.80       | 12.04         | 0.95       | 14.29         |                                    |               |
| 0.66       | 9.93          | 0.81       | 12.19         | 0.96       | 14.44         | .001                               | 0.02          |
| 0.67       | 10.08         | 0.82       | 12.34         | 0.97       | 14.59         | .002                               | 0.03          |
| 0.68       | 10.23         | 0.83       | 12.49         | 0.98       | 14.74         | .003                               | 0.05          |
| 0.69       | 10.38         | 0.84       | 12.64         | 0.99       | 14.89         | .004                               | 0.06          |
| 0.70       | 10.53         | 0.85       | 12.79         | 1.00       | 15.05         | .005                               | 0.08          |
| 0.71       | 10.68         | 0.86       | 12.94         |            |               | .006                               | 0.09          |
| 0.72       | 10.83         | 0.87       | 13.09         |            |               | .007                               | 0.11          |
| 0.73       | 10.98         | 0.88       | 13.24         |            |               | .008                               | 0.12          |
| 0.74       | 11.13         | 0.89       | 13.39         |            |               | .009                               | 0.14          |
| 0.75       | 11.28         | 0.90       | 13.54         |            |               | .010                               | 0.15          |

|                                             | Logarithms. |
|---------------------------------------------|-------------|
| 12 hours, expressed in seconds = 43200.     | 4.6354837   |
| Complement to the same = .00002315          | 5.3645163   |
| 24 hours, expressed in seconds = 86400.     | 4.9365137   |
| Complement to the same = .00001157          | 5.0634863   |
| 360 degrees, expressed in seconds = 1296000 | 6.1126050   |
| To convert Sidereal time to M. solar time - | 9.9988126   |

FORM FOR

## SURVEY OF

## DETERMINATION OF TIME,

DATE AND STATION.—1843, October 13—*Mouth of the Big Black river,*INSTRUMENTS. { Sextant No. 2197, by Troughton & Simms, and  
{ Mean Solar Chronometer No. 76, by Charles

| NAMES OF STARS.               | Observed double altitudes of Star with Sextant. | True altitudes of Star affected by corrections for refraction and errors of Sextant = A. | Mean Solar time of observation deduced. | Time of observation noted by Chronometer. |
|-------------------------------|-------------------------------------------------|------------------------------------------------------------------------------------------|-----------------------------------------|-------------------------------------------|
|                               | O ' "                                           | O ' "                                                                                    | h. m. s.                                | h. m. s.                                  |
| <i>α Andromeda</i><br>(East.) | 91 43 40                                        | 45 52 58.8                                                                               | 7 05 47.69                              | 6 57 02.4                                 |
|                               | 92 18 00                                        | 46 10 09.3                                                                               | 7 07 28.67                              | 6 58 43.2                                 |
|                               | 92 41 15                                        | 46 21 47.3                                                                               | 7 08 37.15                              | 6 59 52.8                                 |
|                               | 93 04 05                                        | 46 33 12.6                                                                               | 7 09 44.37                              | 7 00 59.6                                 |
|                               | 93 45 20                                        | 46 53 50.8                                                                               | 7 11 45.92                              | 7 03 01.2                                 |
|                               | 94 13 45                                        | 47 08 03.7                                                                               | 7 13 09.73                              | 7 04 25.6                                 |
|                               | 94 40 50                                        | 47 21 36.6                                                                               | 7 14 29.64                              | 7 05 45                                   |
|                               | 95 07 25                                        | 47 34 54.5                                                                               | 7 15 48.14                              | 7 07 03.6                                 |

Mean result of 8 observations on *α Andromeda*, in the East,

|                          |          |            |            |           |
|--------------------------|----------|------------|------------|-----------|
|                          | O ' "    | O ' "      | h. m. s.   | h. m. s.  |
| <i>α Lyra</i><br>(West.) | 95 20 05 | 47 41 14.7 | 8 55 32.36 | 8 46 49.2 |
|                          | 95 00 00 | 47 31 11.6 | 8 56 32.06 | 8 47 50.4 |
|                          | 94 30 40 | 47 16 31.2 | 8 57 59.42 | 8 49 16   |
|                          | 94 12 20 | 47 07 21   | 8 58 54    | 8 50 10.8 |
|                          | 93 53 45 | 46 58 03.1 | 8 59 49.4  | 8 51 06.9 |
|                          | 93 29 20 | 46 45 50.2 | 9 01 02.1  | 8 52 19.4 |
|                          | 93 07 35 | 46 34 57.3 | 9 02 07    | 8 53 24.8 |
|                          | 92 46 50 | 46 24 34.5 | 9 03 09    | 8 54 26   |
|                          | 92 28 45 | 46 15 31.7 | 9 04 02.96 | 8 55 21.2 |

Mean result of nine observations on the Star *α Lyra* in the WestMean result of eight observations on the Star *α Andromeda* in the East as above.

CHRONOMETER ERROR.—Slow of Mean Solar time at 8 h. p. m., by a mean of these results from E. and W. Stars.

## RECORD AND COMPUTATION.

*by observed double altitudes of East and West Stars.*

*a tributary to the river St. John, Maine.*

artificial horizon of Mercury.

Young.

| Chronometer (C. Y.<br>76) slow of mean<br>solar time by each<br>observation. | REMARKS.                                                                      |
|------------------------------------------------------------------------------|-------------------------------------------------------------------------------|
| <i>h. m. s.</i>                                                              | Index error of Sextant = + 2' 40"                                             |
| 0 08 45.29                                                                   | Error of eccentricity of Sextant = + 1' 32"                                   |
| 8 45.47                                                                      | Thermometer 31°.5 Fahr.                                                       |
| 8 44.35                                                                      | Barometer 29.14 inches.                                                       |
| 8 44.77                                                                      | Apparent A.R. of Star, = 0 <sup>h</sup> 00 <sup>m</sup> 21 <sup>s</sup> .72   |
| 8 44.72                                                                      | Apparent declination of Star, = 28° 13' 59".5 N.                              |
| 8 44.13                                                                      | App't N. Polar distance of Star = 61 46 00.5 = Δ                              |
| 8 44.64                                                                      | Approximate lat. of this Station = 46 57 00 N. = L                            |
| 8 44.54                                                                      | Approximate longitude of do. = 4 <sup>h</sup> 37 <sup>m</sup> 47 <sup>s</sup> |
|                                                                              | Sider'l time of mean noon at Station = 13 26 20.83                            |
| 0 <sup>h</sup> 08 <sup>m</sup> 44 <sup>s</sup> .74                           |                                                                               |
| <i>h. m. s.</i>                                                              |                                                                               |
| 0 08 43.16                                                                   | Thermometer 29° Fahr.                                                         |
| 8 41.66                                                                      | Barometer 29.14 inches.                                                       |
| 8 43.42                                                                      | Apparent A. R. of Star, = 18 <sup>h</sup> 31 <sup>m</sup> 39 <sup>s</sup> .16 |
| 8 43.20                                                                      | Apparent declination of Star N. = 38° 38' 46".5                               |
| 8 42.50                                                                      | App't N. Polar distance of Star = 51 21 13.5 = Δ                              |
| 8 42.70                                                                      | Index error of Sextant = + 2' 40"                                             |
| 8 42.20                                                                      | Error of eccentricity of Sextant = + 1' 32"                                   |
| 8 43.00                                                                      |                                                                               |
| 8 41.76                                                                      |                                                                               |
| 0 <sup>h</sup> 08 <sup>m</sup> 42 <sup>s</sup> .6                            |                                                                               |
| 0 08 44.7                                                                    |                                                                               |
| 0 <sup>h</sup> 08 <sup>m</sup> 43 <sup>s</sup> .6                            | Observer, <i>Major J. D. Graham.</i><br>Computer, <i>Private F. Herbst.</i>   |

*Computation of the 5th of the preceding altitudes of  $\alpha$  Andromeda. Formula page 143.*

|                                                                                                                       |                      |                                                   |                                                      |
|-----------------------------------------------------------------------------------------------------------------------|----------------------|---------------------------------------------------|------------------------------------------------------|
| Observed double altitude                                                                                              |                      | =                                                 | 93° 45' 20"                                          |
| Index error, sextant                                                                                                  |                      | =                                                 | + 2 40                                               |
| Excentricity, sextant                                                                                                 |                      | =                                                 | + 1 32                                               |
| Double altitude, corrected                                                                                            |                      | =                                                 | 93 49 32                                             |
| Altitude                                                                                                              |                      | =                                                 | 46 54 46                                             |
| Refraction (Therm. 31°.5—Bar. 29.1)                                                                                   |                      | =                                                 | — 55.2                                               |
| True altitude of $\star$ = A                                                                                          |                      | =                                                 | 46° 53' 50".8                                        |
| $2m = L + \Delta + A$                                                                                                 |                      |                                                   |                                                      |
| L = 46° 57'                                                                                                           | ..... Cos            |                                                   | = 9.8341894                                          |
| $\Delta = 61\ 46\ 00.5$                                                                                               | ..... Sin            |                                                   | = 9.9449899                                          |
| A = 46 53 50.8                                                                                                        | Cos L . Sin $\Delta$ | =                                                 | 9.7791793                                            |
| $2m = 155^\circ 36' 51''.3$                                                                                           |                      |                                                   |                                                      |
| m = 77 48 25 .6                                                                                                       | ..... Cos            |                                                   | = 9.3247069                                          |
| (m—A) = 30 54 34 .8                                                                                                   | ..... Sin            |                                                   | = 9.7106984                                          |
|                                                                                                                       | Cos m Sin (m—A)      | =                                                 | 9.0354053                                            |
| $\text{Sin}^2 \frac{1}{2} p = \frac{\text{Cos } m \cdot \text{Sin } (m - A)}{\text{Cos } L \cdot \text{Sin } \Delta}$ | .....                | =                                                 | 19.2562259                                           |
|                                                                                                                       | Sin $\frac{1}{2} p$  | =                                                 | 9.6281129                                            |
|                                                                                                                       | $\frac{1}{2} p$      | =                                                 | 25° 08' 00".7                                        |
|                                                                                                                       | p in arc             | =                                                 | 50 16 01.4                                           |
| (page 146)                                                                                                            | p in time            | =                                                 | — 3 <sup>h</sup> 21 <sup>m</sup> 04 <sup>s</sup> .09 |
|                                                                                                                       | AR . $\star$         | =                                                 | 24 00 21.72                                          |
| Sidereal time of observation                                                                                          | = AR $\pm$ p         | =                                                 | 20 39 17.63                                          |
| Sidereal time, mean noon, at place, (Naut. Alm.)                                                                      |                      | =                                                 | 13 26 20.83                                          |
| Sidereal interval past mean noon                                                                                      |                      | =                                                 | 7 12 56.8                                            |
| Retardation of mean on sidereal interval, (page 144)                                                                  |                      | =                                                 | — 1 10.9                                             |
| Mean solar interval past mean noon, or mean<br>time, P. M., of observation.....}                                      |                      | 7 <sup>h</sup> 11 <sup>m</sup> 45 <sup>s</sup> .9 |                                                      |
| Time of observation by Chronometer                                                                                    |                      | 7 03 01.2                                         |                                                      |
| Chronometer slow                                                                                                      |                      | 8 <sup>m</sup> 44 <sup>s</sup> .7                 |                                                      |

### III. To find the time by equal Altitudes of the Sun.

Correction in time, to be applied as an equation to the mean of the times of observed equal altitudes of the sun, in order to obtain the time of its meridional passage.

$$x = \frac{\delta}{48^a} \times \frac{T}{30} \left( \frac{\text{tang } D}{\text{tang } 7\frac{1}{2} T} - \frac{\text{tang } L}{\sin 7\frac{1}{2} T} \right)$$

$$= \delta \cdot \text{tang } D \frac{T}{1440 \text{ tang } 7\frac{1}{2} T} - \delta \text{ tang } L \frac{T}{1440 \sin 7\frac{1}{2} T}$$

make  $\frac{T}{1440 \sin 7\frac{1}{2} T} = A$

$$\frac{T}{1440 \text{ tang } 7\frac{1}{2} T} = B$$

$$x = \mp A \cdot \delta \cdot \text{tang } L \pm B \cdot \delta \cdot \text{tang } D$$

$$\text{apparent noon} = \frac{1}{2} (t + t') + x$$

$t, t'$  = the times of observation.

$T = (t' - t)$  = the interval of time between the observations, expressed in hours and decimals.

$L$  = the latitude of the place of observation : (*minus* when south.)

$D$  = the declination, at the time of noon, on the given day: (*minus* when south.)

$\delta$  = the double daily variation in the declination, deduced from the noon of the preceding day to noon of the following day: (*minus* when the Sun is proceeding towards the south.)

$x$  = required correction in *seconds*: where  $A$  is to be *minus* when time of noon is required, and *plus* when time of midnight is required, *i. e.* when the first observation is made in the afternoon, and the corresponding one the morning following.

Log. values of  $A$  and  $B$  are given in the tables.



*Equations to equal Altitudes.*

| Interval. | Log A. | Log B. | Interval | Log A. | Log B. |
|-----------|--------|--------|----------|--------|--------|
| H. M.     |        |        | H. M.    |        |        |
| 2 0       | 7.7297 | 7.7146 | 3 0      | 7.7359 | 7.7015 |
| 2         | .7298  | .7143  | 2        | .7362  | .7010  |
| 4         | .7300  | .7139  | 4        | .7364  | .7005  |
| 6         | .7302  | .7136  | 6        | .7367  | .6999  |
| 8         | .7304  | .7132  | 8        | .7369  | .6993  |
| 10        | .7305  | .7128  | 10       | .7372  | .6988  |
| 12        | .7307  | .7125  | 12       | .7374  | .6982  |
| 14        | .7309  | .7121  | 14       | .7377  | .6976  |
| 16        | .7311  | .7117  | 16       | .7380  | .6970  |
| 18        | .7313  | .7113  | 18       | .7383  | .6964  |
| 20        | .7315  | .7109  | 20       | .7386  | .6958  |
| 22        | .7317  | .7105  | 22       | .7388  | .6952  |
| 24        | .7319  | .7101  | 24       | .7391  | .6946  |
| 26        | .7321  | .7097  | 26       | .7394  | .6940  |
| 28        | .7323  | .7092  | 28       | .7397  | .6934  |
| 30        | .7325  | .7088  | 30       | .7400  | .6927  |
| 32        | .7327  | .7083  | 32       | .7403  | .6921  |
| 34        | .7329  | .7079  | 34       | .7406  | .6914  |
| 36        | .7331  | .7075  | 36       | .7409  | .6908  |
| 38        | .7333  | .7070  | 38       | .7412  | .6901  |
| 40        | .7336  | .7065  | 40       | .7415  | .6894  |
| 42        | .7338  | .7061  | 42       | .7418  | .6888  |
| 44        | .7340  | .7056  | 44       | .7421  | .6881  |
| 46        | .7342  | .7051  | 46       | .7424  | .6874  |
| 48        | .7345  | .7046  | 48       | .7428  | .6867  |
| 50        | .7347  | .7041  | 50       | .7431  | .6859  |
| 52        | .7349  | .7036  | 52       | .7434  | .6852  |
| 54        | .7352  | .7031  | 54       | .7437  | .6845  |
| 56        | .7354  | .7026  | 56       | .7441  | .6838  |
| 58        | 7.7357 | 7.7021 | 58       | 7.7444 | 7.6830 |

$$x = \mp A \delta \tan L + B \delta \tan D.$$

*Equations to equal Altitudes.*

| Interval. | Log A. | Log B. | Interval. | Log A. | Log B. |
|-----------|--------|--------|-----------|--------|--------|
| H. M.     |        |        | H. M.     |        |        |
| 4 0       | 7.7447 | 7.6823 | 5 0       | 7.7562 | 7.6556 |
| 2         | .7451  | .6815  | 2         | .7566  | .6546  |
| 4         | .7454  | .6807  | 4         | .7570  | .6536  |
| 6         | .7458  | .6800  | 6         | .7575  | .6525  |
| 8         | .7461  | .6792  | 8         | .7579  | .6514  |
| 10        | .7464  | .6784  | 10        | .7583  | .6504  |
| 12        | .7468  | .6776  | 12        | .7588  | .6493  |
| 14        | .7472  | .6768  | 14        | .7592  | .6482  |
| 16        | .7475  | .6759  | 16        | .7597  | .6471  |
| 18        | .7479  | .6751  | 18        | .7601  | .6460  |
| 20        | .7482  | .6743  | 20        | .7606  | .6448  |
| 22        | .7486  | .6734  | 22        | .7610  | .6437  |
| 24        | .7490  | .6726  | 24        | .7615  | .6425  |
| 26        | .7494  | .6717  | 26        | .7620  | .6414  |
| 28        | .7497  | .6708  | 28        | .7624  | .6402  |
| 30        | .7501  | .6700  | 30        | .7629  | .6390  |
| 32        | .7505  | .6691  | 32        | .7634  | .6378  |
| 34        | .7509  | .6682  | 34        | .7638  | .6366  |
| 36        | .7513  | .6673  | 36        | .7643  | .6354  |
| 38        | .7517  | .6663  | 38        | .7648  | .6342  |
| 40        | .7521  | .6654  | 40        | .7653  | .6329  |
| 42        | .7525  | .6645  | 42        | .7658  | .6317  |
| 44        | .7529  | .6635  | 44        | .7663  | .6304  |
| 46        | .7533  | .6626  | 46        | .7668  | .6291  |
| 48        | .7537  | .6616  | 48        | .7673  | .6278  |
| 50        | .7541  | .6606  | 50        | .7678  | .6265  |
| 52        | .7545  | .6597  | 52        | .7683  | .6252  |
| 54        | .7549  | .6587  | 54        | .7688  | .6239  |
| 56        | .7553  | .6577  | 56        | .7693  | .6225  |
| 58        | 7.7557 | 7.6567 | 58        | 7.7698 | 7.6212 |

$$x = \mp A \delta \text{ tang } L + B \delta \text{ tang } D.$$

*Equations to Equal Altitudes.*

| Interval. | Log A. | Log B. | Interval. | Log A. | Log B. |
|-----------|--------|--------|-----------|--------|--------|
| H. M.     |        |        | H. M.     |        |        |
| 6 0       | 7.7703 | 7.6198 | 7 0       | 7.7873 | 7.5717 |
| 2         | .7708  | .6184  | 2         | .7879  | .5699  |
| 4         | .7713  | .6170  | 4         | .7885  | .5680  |
| 6         | .7719  | .6156  | 6         | .7891  | .5661  |
| 8         | .7724  | .6142  | 8         | .7898  | .5641  |
| 10        | .7729  | .6127  | 10        | .7904  | .5622  |
| 12        | .7735  | .6113  | 12        | .7910  | .5602  |
| 14        | .7740  | .6098  | 14        | .7916  | .5582  |
| 16        | .7745  | .6083  | 16        | .7923  | .5562  |
| 18        | .7751  | .6068  | 18        | .7929  | .5542  |
| 20        | .7756  | .6053  | 20        | .7936  | .5522  |
| 22        | .7762  | .6038  | 22        | .7942  | .5501  |
| 24        | .7767  | .6023  | 24        | .7949  | .5480  |
| 26        | .7773  | .6007  | 26        | .7955  | .5459  |
| 28        | .7779  | .5991  | 28        | .7962  | .5437  |
| 30        | .7784  | .5975  | 30        | .7969  | .5416  |
| 32        | .7790  | .5959  | 32        | .7975  | .5394  |
| 34        | .7796  | .5943  | 34        | .7982  | .5372  |
| 36        | .7801  | .5927  | 36        | .7989  | .5350  |
| 38        | .7807  | .5910  | 38        | .7995  | .5327  |
| 40        | .7813  | .5894  | 40        | .8002  | .5304  |
| 42        | .7819  | .5877  | 42        | .8009  | .5281  |
| 44        | .7825  | .5860  | 44        | .8016  | .5258  |
| 46        | .7831  | .5843  | 46        | .8023  | .5234  |
| 48        | .7836  | .5825  | 48        | .8030  | .5211  |
| 50        | .7842  | .5808  | 50        | .8037  | .5186  |
| 52        | .7848  | .5790  | 52        | .8044  | .5162  |
| 54        | .7854  | .5772  | 54        | .8051  | .5137  |
| 56        | .7860  | .5754  | 56        | .8058  | .5112  |
| 58        | 7.7867 | 7.5736 | 58        | 7.8065 | 7.5087 |

$$x = \mp A \delta \tan L \pm B \delta \tan D.$$

*Equations to Equal Altitudes.*

| Interval. | Log A. | Log B. | Interval. | Log A. | Log B.  |
|-----------|--------|--------|-----------|--------|---------|
| H. M.     |        |        | H. M.     |        |         |
| 8 0       | 7.8072 | 7.5062 | 15 0      | 8.0521 | -7.6350 |
| 2         | .8079  | .5036  | 2         | .0539  | .6413   |
| 4         | .8086  | .5010  | 4         | .0556  | .6475   |
| 6         | .8094  | .4983  | 6         | .0574  | .6537   |
| 8         | .8101  | .4957  | 8         | .0592  | .6599   |
| 10        | .8108  | .4930  | 10        | .0610  | .6660   |
| 12        | .8116  | .4902  | 12        | .0628  | .6721   |
| 14        | .8123  | .4874  | 14        | .0646  | .6781   |
| 16        | .8130  | .4846  | 16        | .0664  | .6841   |
| 18        | .8138  | .4818  | 18        | .0682  | .6900   |
| 20        | .8145  | .4789  | 20        | .0700  | .6959   |
| 22        | .8153  | .4760  | 22        | .0718  | .7018   |
| 24        | .8160  | .4731  | 24        | .0737  | .7077   |
| 26        | .8168  | .4701  | 26        | .0755  | .7135   |
| 28        | .8176  | .4671  | 28        | .0774  | .7192   |
| 30        | .8183  | .4640  | 30        | .0792  | .7249   |
| 32        | .8191  | .4609  | 32        | .0811  | .7306   |
| 34        | .8199  | .4578  | 34        | .0830  | .7363   |
| 36        | .8206  | .4546  | 36        | .0849  | .7419   |
| 38        | .8214  | .4514  | 38        | .0868  | .7475   |
| 40        | .8222  | .4482  | 40        | .0887  | .7531   |
| 42        | .8230  | .4449  | 42        | .0906  | .7586   |
| 44        | .8238  | .4415  | 44        | .0925  | .7641   |
| 46        | .8246  | .4381  | 46        | .0945  | .7696   |
| 48        | .8254  | .4347  | 48        | .0964  | .7751   |
| 50        | .8262  | .4312  | 50        | .0983  | .7805   |
| 52        | .8270  | .4277  | 52        | .1003  | .7859   |
| 54        | .8278  | .4241  | 54        | .1023  | .7912   |
| 56        | .8286  | .4205  | 56        | .1042  | .7966   |
| 58        | 7.8294 | 7.4168 | 58        | 8.1062 | -7.8019 |

$$x = \mp A \delta \text{ tang } L + B \delta \text{ tang } D.$$

*Equations to Equal Altitudes.*

| Interval. | Log A. | Log B.  | Interval. | Log A. | Log B.  |
|-----------|--------|---------|-----------|--------|---------|
| H. M.     |        |         | H. M.     |        |         |
| 16 0      | 8.1082 | -7.8072 | 17 0      | 8.1726 | -7.9571 |
| 2         | .1102  | .8125   | 2         | .1749  | .9618   |
| 4         | .1122  | .8177   | 4         | .1773  | .9666   |
| 6         | .1143  | .8229   | 6         | .1796  | .9713   |
| 8         | .1163  | .8281   | 8         | .1819  | .9761   |
| 10        | .1183  | .8333   | 10        | .1843  | .9808   |
| 12        | .1204  | .8385   | 12        | .1867  | .9855   |
| 14        | .1224  | .8436   | 14        | .1890  | .9902   |
| 16        | .1245  | .8487   | 16        | .1914  | .9949   |
| 18        | .1266  | .8538   | 18        | .1938  | -7.9996 |
| 20        | .1287  | .8589   | 20        | .1963  | -8.0043 |
| 22        | .1308  | .8640   | 22        | .1987  | .0090   |
| 24        | .1329  | .8690   | 24        | .2011  | .0137   |
| 26        | .1350  | .8740   | 26        | .2036  | .0184   |
| 28        | .1371  | .8790   | 28        | .2061  | .0230   |
| 30        | .1393  | .8840   | 30        | .2086  | .0277   |
| 32        | .1414  | .8890   | 32        | .2111  | .0323   |
| 34        | .1436  | .8939   | 34        | .2136  | .0370   |
| 36        | .1458  | .8989   | 36        | .2161  | .0416   |
| 38        | .1479  | .9038   | 38        | .2186  | .0462   |
| 40        | .1501  | .9087   | 40        | .2212  | .0508   |
| 42        | .1523  | .9136   | 42        | .2237  | .0555   |
| 44        | .1545  | .9185   | 44        | .2263  | .0601   |
| 46        | .1568  | .9234   | 46        | .2289  | .0647   |
| 48        | .1590  | .9282   | 48        | .2315  | .0693   |
| 50        | .1612  | .9330   | 50        | .2341  | .0739   |
| 52        | .1635  | .9379   | 52        | .2367  | .0785   |
| 54        | .1658  | .9427   | 54        | .2394  | .0831   |
| 56        | .1680  | .9475   | 56        | .2420  | .0877   |
| 58        | 8.1703 | -7.9523 | 58        | 8.2447 | -8.0923 |

$$x = \mp A \delta \tan L \pm B \delta \tan D.$$

*Equations to Equal Altitudes.*

| Interval. | Log A. | Log B.  | Interval. | Log A. | Log B.  |
|-----------|--------|---------|-----------|--------|---------|
| H. M.     |        |         | H. M.     |        |         |
| 18 0      | 8.2474 | -8.0969 | 19 0      | 8.3359 | -8.2354 |
| 2         | .2501  | .1015   | 2         | .3392  | .2401   |
| 4         | .2529  | .1061   | 4         | .3424  | .2448   |
| 6         | .2556  | .1107   | 6         | .3457  | .2495   |
| 8         | .2583  | .1153   | 8         | .3490  | .2542   |
| 10        | .2611  | .1199   | 10        | .3524  | .2589   |
| 12        | .2639  | .1245   | 12        | .3557  | .2637   |
| 14        | .2667  | .1291   | 14        | .3591  | .2684   |
| 16        | .2695  | .1336   | 16        | .3625  | .2732   |
| 18        | .2723  | .1382   | 18        | .3659  | .2779   |
| 20        | .2752  | .1428   | 20        | .3694  | .2827   |
| 22        | .2781  | .1474   | 22        | .3728  | .2875   |
| 24        | .2809  | .1520   | 24        | .3763  | .2923   |
| 26        | .2838  | .1566   | 26        | .3798  | .2971   |
| 28        | .2868  | .1612   | 28        | .3834  | .3019   |
| 30        | .2897  | .1658   | 30        | .3869  | .3068   |
| 32        | .2926  | .1704   | 32        | .3905  | .3116   |
| 34        | .2956  | .1750   | 34        | .3941  | .3165   |
| 36        | .2986  | .1797   | 36        | .3978  | .3214   |
| 38        | .3016  | .1842   | 38        | .4015  | .3263   |
| 40        | .3046  | .1889   | 40        | .4052  | .3312   |
| 42        | .3077  | .1935   | 42        | .4089  | .3361   |
| 44        | .3107  | .1981   | 44        | .4126  | .3410   |
| 46        | .3138  | .2028   | 46        | .4164  | .3460   |
| 48        | .3169  | .2074   | 48        | .4202  | .3510   |
| 50        | .3200  | .2121   | 50        | .4241  | .3560   |
| 52        | .3232  | .2167   | 52        | .4279  | .3610   |
| 54        | .3263  | .2214   | 54        | .4318  | .3660   |
| 56        | .3295  | .2261   | 56        | .4357  | .3711   |
| 58        | 8.3327 | -8.2307 | 58        | 8.4397 | -8.3761 |

$$x = \mp A \delta \tan L + B \delta \tan D.$$

*Equations to Equal Altitudes.*

| Interval. | Log A. | Log B.  | Interval. | Log A. | Log B.  |
|-----------|--------|---------|-----------|--------|---------|
| H. M.     |        |         | H. M.     |        |         |
| 20 0      | 8.4437 | -8.3812 | 21 0      | 8.5810 | -8.5466 |
| 2         | .4477  | .3863   | 2         | .5863  | .5527   |
| 4         | .4518  | .3915   | 4         | .5917  | .5588   |
| 6         | .4559  | .3966   | 6         | .5971  | .5650   |
| 8         | .4600  | .4018   | 8         | .6025  | .5712   |
| 10        | .4641  | .4070   | 10        | .6081  | .5775   |
| 12        | .4683  | .4122   | 12        | .6136  | .5838   |
| 14        | .4726  | .4175   | 14        | .6193  | .5902   |
| 16        | .4768  | .4227   | 16        | .6250  | .5966   |
| 18        | .4811  | .4280   | 18        | .6308  | .6031   |
| 20        | .4854  | .4334   | 20        | .6366  | .6096   |
| 22        | .4898  | .4387   | 22        | .6426  | .6162   |
| 24        | .4942  | .4441   | 24        | .6486  | .6229   |
| 26        | .4987  | .4495   | 26        | .6546  | .6296   |
| 28        | .5032  | .4549   | 28        | .6608  | .6364   |
| 30        | .5077  | .4604   | 30        | .6670  | .6433   |
| 32        | .5123  | .4659   | 32        | .6733  | .6502   |
| 34        | .5169  | .4714   | 34        | .6796  | .6572   |
| 36        | .5215  | .4770   | 36        | .6861  | .6643   |
| 38        | .5262  | .4826   | 38        | .6927  | .6715   |
| 40        | .5310  | .4882   | 40        | .6993  | .6788   |
| 42        | .5357  | .4939   | 42        | .7060  | .6860   |
| 44        | .5406  | .4996   | 44        | .7128  | .6934   |
| 46        | .5455  | .5053   | 46        | .7197  | .7009   |
| 48        | .5504  | .5111   | 48        | .7268  | .7085   |
| 50        | .5554  | .5169   | 50        | .7339  | .7162   |
| 52        | .5604  | .5228   | 52        | .7411  | .7239   |
| 54        | .5655  | .5287   | 54        | .7484  | .7318   |
| 56        | .5706  | .5346   | 56        | .7558  | .7398   |
| 58        | 8.5758 | -8.5406 | 58        | 8.7634 | -8.7478 |

$$x = \mp A \delta \tan L \pm B \delta \tan D.$$

*Equations to Equal Altitudes.*

| Interval. | Log A. | Log B.  | Interval. | Log A. | Log B.  |
|-----------|--------|---------|-----------|--------|---------|
| H. M.     |        |         | H. M.     |        |         |
| 22 0      | 8.7711 | —8.7560 | 23 0      | 9.0877 | —9.0839 |
| 2         | .7789  | .7643   | 2         | .1029  | .0995   |
| 4         | .7868  | .7727   | 4         | .1187  | .1155   |
| 6         | .7948  | .7813   | 6         | .1351  | .1321   |
| 8         | .8030  | .7899   | 8         | .1520  | .1492   |
| 10        | .8113  | .7987   | 10        | .1696  | .1670   |
| 12        | .8198  | .8076   | 12        | .1879  | .1855   |
| 14        | .8284  | .8167   | 14        | .2069  | .2047   |
| 16        | .8372  | .8259   | 16        | .2268  | .2248   |
| 18        | .8461  | .8353   | 18        | .2476  | .2456   |
| 20        | .8553  | .8448   | 20        | .2693  | .2677   |
| 22        | .8645  | .8545   | 22        | .2922  | .2907   |
| 24        | .8740  | .8644   | 24        | .3162  | .3149   |
| 26        | .8837  | .8745   | 26        | .3416  | .3404   |
| 28        | .8935  | .8847   | 28        | .3685  | .3674   |
| 30        | .9036  | .8952   | 30        | .3971  | .3962   |
| 32        | .9139  | .9058   | 32        | .4276  | .4268   |
| 34        | .9244  | .9167   | 34        | .4604  | .4597   |
| 36        | .9351  | .9278   | 36        | .4957  | .4952   |
| 38        | .9461  | .9391   | 38        | .5341  | .5336   |
| 40        | .9574  | .9507   | 40        | .5761  | .5757   |
| 42        | .9689  | .9626   | 42        | .6224  | .6221   |
| 44        | .9807  | .9747   | 44        | .6742  | .6739   |
| 46        | 8.9928 | .9871   | 46        | .7328  | .7326   |
| 48        | 9.0052 | —8.9999 | 48        | .8003  | .8001   |
| 50        | .0180  | —9.0129 | 50        | .8801  | .8800   |
| 52        | .0311  | .0263   | 52        | 9.9776 | —9.9775 |
| 54        | .0446  | .0401   | 54        | 0.1031 | —0.1031 |
| 56        | .0585  | .0543   | 56        | .2798  | .2798   |
| 58        | 9.0729 | —9.0689 | 58        | 0.5814 | —0.5814 |

$$x = \mp A \delta \text{ tang } L + B \delta \text{ tang } D.$$



## SURVEY OF

DETERMINATION OF THE TIME,  
*Chronometer*DATE AND STATION.—1844, August 9—*American Camp, near Tasche-*INSTRUMENTS. { Sextant No. 2197, by *Troughton & Simms*, and  
{ *Mean Solar Chronometer* No. 2440, by *Parkinson*

| Observed double altitudes of the Sun's upper and lower limbs. | Times by Chronometer, of observed equal altitudes.<br><i>August 9th.</i> |                 | $t' - t =$ the elapsed time;<br>$= T.$ | Equation of equal altitudes<br>$= x.$ |
|---------------------------------------------------------------|--------------------------------------------------------------------------|-----------------|----------------------------------------|---------------------------------------|
|                                                               | A. M. = $t.$                                                             | P. M. = $t'.$   |                                        |                                       |
| <i>Upper Limb.</i>                                            | <i>h. m. s.</i>                                                          | <i>h. m. s.</i> | <i>h. m.</i>                           | <i>s.</i>                             |
| 78° 50' 00"                                                   | 1 28 23                                                                  | 8 03 16.5       | 6 33                                   | +10.63                                |
| 79 19 30                                                      | 1 28 52.8                                                                | 8 01 46.5       |                                        |                                       |
| <i>Lower Limb.</i>                                            |                                                                          |                 |                                        |                                       |
| 83° 10' 00"                                                   | 1 45 01                                                                  | 7 46 40.5       | 5 59½                                  | +10.24                                |
| 83 40 00                                                      | 1 46 34.5                                                                | 7 45 06.2       |                                        |                                       |
| 84 00 00                                                      | 1 47 38                                                                  | 7 44 04         |                                        |                                       |
| <i>Upper Limb.</i>                                            |                                                                          |                 |                                        |                                       |
| 85° 36' 00"                                                   | 1 49 23                                                                  | 7 42 18         | 5 48                                   | +10.1                                 |
| 87 02 10                                                      | 1 53 55.5                                                                | 7 37 46.2       |                                        |                                       |

CHRONOMETER ERROR.—*Fast* of mean solar time at apparent noon of August 9, 1844, by a mean of 7 pairs of equal altitudes of the Sun,

*by observed equal altitudes of the Sun's limbs, to correct the at noon.*

*reau's house, on the highland boundary between Maine and Canada.*

artificial horizon of Mercury.

& *Frodsham.*

| Chronometer No.<br>2440, Fast of mean<br>time at appt. noon,<br>by each pair of<br>equal altitudes. | REMARKS.                                                                |
|-----------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------|
| h. m. s.                                                                                            | Index error of Sextant . . . . .                                        |
| 4 40 51.29                                                                                          | Error of excentricity of Sextant . . . .                                |
| 4 40 51.17                                                                                          | Thermr. (A. M.) 70° Fahr. Barom. . . .                                  |
|                                                                                                     | Thermr. (P. M.) 69° Fahr. Barom. . . .                                  |
| 4 40 51.9                                                                                           | Sun's appt. declination at appt. noon (D) = 15°43' 12" N.               |
| 4 40 51.5                                                                                           | Double daily variation of Sun's declination ( $\delta$ ) = 34' 54"      |
| 4 40 52.15                                                                                          | = 2094" in arc.                                                         |
|                                                                                                     | Equation of time at apparent noon + 5 <sup>m</sup> 09 <sup>s</sup> . 09 |
| 4 40 51.51                                                                                          | Latitude of station (approximate) + 45° 48' = (L.)                      |
| 4 40 51.86                                                                                          |                                                                         |
| 4 <sup>h</sup> 40 <sup>m</sup> 51 <sup>s</sup> . 6                                                  | Observer, <i>Major J. D. Graham,</i><br>Computer, <i>Do.</i>            |

*Computation of the equation of equal altitudes to correct the chronometer for noon of August 9, 1844, by the first of the preceding equal altitudes of the Sun's upper and lower limbs.*

$$x = (-A. \delta. \tan g L) + (B. \delta. \tan g D.)$$

1st Set.

|                                                       |             |              |             |
|-------------------------------------------------------|-------------|--------------|-------------|
| T = 6 <sup>h</sup> 33 <sup>m</sup> , log A (page 164) | = - 7.77930 | log B        | = 7.59510   |
| $\delta$ = 2094, log $\delta$                         | = - 3.32097 | log $\delta$ | = - 3.32097 |
| L = 45° 48', log tang                                 | = + 0.01213 | log tang D   | = 9.44933   |
| 1st term = + 12.95                                    | = + 1.11240 | - 2.32       | = - 0.36540 |
| 2d term = - 2.32                                      |             |              |             |

$$x = + 10.63 \text{ Equation of equal altitudes.}$$

*Computation of the first two of the foregoing pairs of equal altitudes of the Sun's limbs.*

|                                                           |       | 1st pair.                            | 2d pair.                             |
|-----------------------------------------------------------|-------|--------------------------------------|--------------------------------------|
| A. M.                                                     | =     | $t = 1^h 28^m 23.0$                  | $1^h 29^m 52.8$                      |
| P. M.                                                     | =     | $t' = 8 \ 03 \ 16.5$                 | $8 \ 01 \ 46.5$                      |
|                                                           |       | $t + t' = 9 \ 31 \ 39.5$             | $9 \ 31 \ 39.3$                      |
|                                                           |       | $\frac{t + t'}{2} = 4 \ 45 \ 49.75$  | $4 \ 45 \ 39.65$                     |
| Equat'n of equal altitudes =                              | $x =$ | + 10.63                              | 10.63                                |
| Time by chron. of appt. noon                              | =     | 4 46 00.38                           | 4 46 00.28                           |
| Correct mean time at apparent noon<br>(Naut. Alm.)        | =     | 0 05 09.09                           | 0 05 09.09                           |
| Chron. fast of mean time at appt.<br>noon, August 9, 1844 | =     | 4 <sup>h</sup> 40 <sup>m</sup> 51.29 | 4 <sup>h</sup> 40 <sup>m</sup> 51.17 |

*Sun's Parallax in Altitude.*

| Sun's Altit. | Sun's Horizontal Parallax. |      |      |      |      | Sun's Altit. | Sun's Horizontal Parallax. |      |      |      |      |
|--------------|----------------------------|------|------|------|------|--------------|----------------------------|------|------|------|------|
|              | 8".4                       | 8".5 | 8".6 | 8".7 | 8".8 |              | 8".4                       | 8".5 | 8".6 | 8".7 | 8".8 |
| 0            | 8.40                       | 8.50 | 8.60 | 8.70 | 8.80 | 45           | 5.94                       | 6.01 | 6.08 | 6.15 | 6.22 |
| 5            | 8.37                       | 8.47 | 8.57 | 8.67 | 8.77 | 50           | 5.40                       | 5.46 | 5.53 | 5.59 | 5.66 |
| 10           | 8.27                       | 8.37 | 8.47 | 8.57 | 8.67 | 55           | 4.82                       | 4.88 | 4.93 | 4.99 | 5.05 |
| 15           | 8.11                       | 8.21 | 8.31 | 8.40 | 8.50 | 60           | 4.20                       | 4.25 | 4.30 | 4.35 | 4.40 |
| 20           | 7.89                       | 7.99 | 8.08 | 8.18 | 8.27 | 65           | 3.55                       | 3.59 | 3.63 | 3.68 | 3.72 |
| 25           | 7.61                       | 7.70 | 7.79 | 7.88 | 7.98 | 70           | 2.87                       | 2.91 | 2.94 | 2.98 | 3.01 |
| 30           | 7.28                       | 7.36 | 7.45 | 7.53 | 7.62 | 75           | 2.17                       | 2.20 | 2.23 | 2.25 | 2.28 |
| 35           | 6.88                       | 6.96 | 7.04 | 7.13 | 7.21 | 80           | 1.46                       | 1.48 | 1.49 | 1.51 | 1.53 |
| 40           | 6.44                       | 6.51 | 6.59 | 6.66 | 6.74 | 85           | 0.73                       | 0.74 | 0.75 | 0.76 | 0.77 |
| 45           | 5.94                       | 6.01 | 6.08 | 6.15 | 6.22 | 90           | 0.00                       | 0.00 | 0.00 | 0.00 | 0.00 |

Parallax in Altitude = Hor. Par  $\times$  Cos. Altitude.

*Decimals of an Hour.*

| MINUTES. |        |    |        | SECONDS. |         |    |        |
|----------|--------|----|--------|----------|---------|----|--------|
| M.       | Decm.  | M. | Decm.  | s.       | Decm.   | s. | Decm.  |
| 1        | .01667 | 21 | .35000 | 41       | .68333  | 1  | .00028 |
| 2        | .03333 | 22 | .36667 | 42       | .70000  | 2  | .00056 |
| 3        | .05000 | 23 | .38333 | 43       | .71667  | 3  | .00083 |
| 4        | .06667 | 24 | .40000 | 44       | .73333  | 4  | .00111 |
| 5        | .08333 | 25 | .41667 | 45       | .75000  | 5  | .00139 |
| 6        | .10000 | 26 | .43333 | 46       | .76667  | 6  | .00167 |
| 7        | .11667 | 27 | .45000 | 47       | .78333  | 7  | .00194 |
| 8        | .13333 | 28 | .46667 | 48       | .80000  | 8  | .00222 |
| 9        | .15000 | 29 | .48333 | 49       | .81667  | 9  | .00250 |
| 10       | .16667 | 30 | .50000 | 50       | .83333  | 10 | .00278 |
| 11       | .18333 | 31 | .51667 | 51       | .85000  | 11 | .00306 |
| 12       | .20000 | 32 | .53333 | 52       | .86667  | 12 | .00333 |
| 13       | .21667 | 33 | .55000 | 53       | .88333  | 13 | .00361 |
| 14       | .23333 | 34 | .56667 | 54       | .90000  | 14 | .00389 |
| 15       | .25000 | 35 | .58333 | 55       | .91667  | 15 | .00417 |
| 16       | .26667 | 36 | .60000 | 56       | .93333  | 16 | .00444 |
| 17       | .28333 | 37 | .61667 | 57       | .95000  | 17 | .00472 |
| 18       | .30000 | 38 | .63333 | 58       | .96667  | 18 | .00500 |
| 19       | .31667 | 39 | .65000 | 59       | .98333  | 19 | .00528 |
| 20       | .33333 | 40 | .66667 | 60       | 1.00000 | 20 | .00556 |

*Fahrenheit's Thermometer 50°. Barometer 30 Inches.*

| Alt.  | r.     | Log. r. | Diff. | Alt.  | r.      | Log. r. | Diff. |
|-------|--------|---------|-------|-------|---------|---------|-------|
| 0     | '      |         |       | 0     | '       |         |       |
| 90 00 | 0 0.00 | 0.0000  |       | 83 00 | 0 7.17  | 0.8557  | 102   |
| 89 50 | 0.17   | 9.2304  | 3011  | 82 50 | 7.34    | 0.8659  | 101   |
| 40    | 0.34   | 9.5315  | 1761  | 40    | 7.52    | 0.8760  | 99    |
| 30    | 0.51   | 9.7076  | 1249  | 30    | 7.69    | 0.8859  | 97    |
| 20    | 0.68   | 9.8325  | 969   | 20    | 7.86    | 0.8956  | 95    |
| 10    | 0.85   | 9.9294  | 791   | 10    | 8.04    | 0.9051  | 93    |
| 89 00 | 0 1.02 | 0.0085  | 670   | 82 00 | 0 8.21  | 0.9144  | 90    |
| 88 50 | 1.19   | 0.0755  | 580   | 81 50 | 8.38    | 0.9234  | 89    |
| 40    | 1.36   | 0.1335  | 512   | 40    | 8.56    | 0.9323  | 87    |
| 30    | 1.53   | 0.1847  | 457   | 30    | 8.73    | 0.9410  | 85    |
| 20    | 1.70   | 0.2304  | 414   | 20    | 8.90    | 0.9495  | 84    |
| 10    | 1.87   | 0.2718  | 379   | 10    | 9.08    | 0.9579  | 84    |
| 88 00 | 0 2.04 | 0.3097  | 347   | 81 00 | 0 9.25  | 0.9663  | 80    |
| 87 50 | 2.21   | 0.3444  | 322   | 80 50 | 9.42    | 0.9743  | 80    |
| 40    | 2.38   | 0.3766  | 301   | 40    | 9.60    | 0.9823  | 78    |
| 30    | 2.55   | 0.4067  | 280   | 30    | 9.77    | 0.9901  | 77    |
| 20    | 2.72   | 0.4347  | 263   | 20    | 9.95    | 0.9978  | 76    |
| 10    | 2.89   | 0.4610  | 250   | 10    | 10.12   | 1.0054  | 75    |
| 87 00 | 0 3.06 | 0.4860  | 235   | 80 00 | 10.30   | 1.0129  | 72    |
| 86 50 | 3.23   | 0.5095  | 224   | 79 50 | 0 10.47 | 1.0201  | 72    |
| 40    | 3.40   | 0.5319  | 211   | 40    | 10.65   | 1.0273  | 71    |
| 30    | 3.57   | 0.5530  | 203   | 30    | 10.82   | 1.0344  | 70    |
| 20    | 3.74   | 0.5733  | 193   | 20    | 11.00   | 1.0414  | 69    |
| 10    | 3.91   | 0.5926  | 186   | 10    | 11.17   | 1.0483  | 69    |
| 86 00 | 0 4.08 | 0.6112  | 178   | 79 00 | 0 11.35 | 1.0552  | 66    |
| 85 50 | 4.26   | 0.6290  | 171   | 78 50 | 11.53   | 1.0618  | 66    |
| 40    | 4.43   | 0.6461  | 165   | 40    | 11.71   | 1.0684  | 66    |
| 30    | 4.60   | 0.6626  | 158   | 30    | 11.89   | 1.0750  | 65    |
| 20    | 4.77   | 0.6784  | 153   | 20    | 12.06   | 1.0815  | 64    |
| 10    | 4.94   | 0.6937  | 149   | 10    | 12.24   | 1.0879  | 62    |
| 85 00 | 0 5.11 | 0.7086  | 142   | 78 00 | 0 12.42 | 1.0941  | 62    |
| 84 50 | 5.28   | 0.7228  | 139   | 77 50 | 12.60   | 1.1003  | 61    |
| 40    | 5.45   | 0.7367  | 135   | 40    | 12.78   | 1.1064  | 60    |
| 30    | 5.63   | 0.7502  | 131   | 30    | 12.95   | 1.1124  | 60    |
| 20    | 5.80   | 0.7633  | 127   | 20    | 13.13   | 1.1184  | 58    |
| 10    | 5.97   | 0.7760  | 122   | 10    | 13.31   | 1.1242  | 58    |
| 84 00 | 0 6.14 | 0.7882  | 120   | 77 00 | 0 13.49 | 1.1300  | 57    |
| 83 50 | 6.31   | 0.8002  | 116   | 76 50 | 13.67   | 1.1357  | 57    |
| 40    | 6.48   | 0.8118  | 114   | 40    | 13.85   | 1.1414  | 55    |
| 30    | 6.66   | 0.8232  | 111   | 30    | 14.02   | 1.1469  | 55    |
| 20    | 6.83   | 0.8343  | 108   | 20    | 14.20   | 1.1524  | 54    |
| 10    | 7.00   | 0.8451  | 106   | 10    | 14.38   | 1.1578  | 54    |
| 83.00 | 0 7.17 | 0.8557  | 102   | 76.00 | 0 14.56 | 1.1632  | 54    |

*Fahrenheit's Thermometer 50°. Barometer 30 Inches.*

| Alt.  | r.      | Log. r. | Diff. | Alt.  | r.      | Log. r. | Diff. |
|-------|---------|---------|-------|-------|---------|---------|-------|
| ° ' " | ' "     |         |       | ° ' " | ' "     |         |       |
| 76 00 | 0 14.56 | 1.1632  | 54    | 69 00 | 0 22.42 | 1.3507  | 37    |
| 75 50 | 14.74   | 1.1686  | 54    | 68 50 | 22.62   | 1.3544  | 38    |
| 40    | 14.93   | 1.1740  | 53    | 40    | 22.81   | 1.3582  | 37    |
| 30    | 15.11   | 1.1793  | 52    | 30    | 23.01   | 1.3619  | 37    |
| 20    | 15.29   | 1.1845  | 52    | 20    | 23.21   | 1.3656  | 37    |
| 10    | 15.48   | 1.1897  | 50    | 10    | 23.40   | 1.3693  | 36    |
| 75 00 | 0 15.66 | 1.1947  | 51    | 68 00 | 0 23.60 | 1.3729  | 37    |
| 74 50 | 15.84   | 1.1998  | 50    | 67 50 | 23.80   | 1.3766  | 36    |
| 40    | 16.03   | 1.2048  | 50    | 40    | 24.00   | 1.3802  | 36    |
| 30    | 16.21   | 1.2098  | 49    | 30    | 24.20   | 1.3838  | 36    |
| 20    | 16.39   | 1.2147  | 48    | 20    | 24.40   | 1.3874  | 35    |
| 10    | 16.58   | 1.2195  | 46    | 10    | 24.60   | 1.3909  | 36    |
| 74 00 | 0 16.75 | 1.2241  | 46    | 67 00 | 0 24.80 | 1.3945  | 36    |
| 73 50 | 16.93   | 1.2287  | 47    | 66 50 | 25.00   | 1.3981  | 34    |
| 40    | 17.12   | 1.2334  | 46    | 40    | 25.20   | 1.4015  | 34    |
| 30    | 17.30   | 1.2380  | 46    | 30    | 25.41   | 1.4049  | 35    |
| 20    | 17.48   | 1.2426  | 46    | 20    | 25.61   | 1.4084  | 34    |
| 10    | 17.67   | 1.2472  | 47    | 10    | 25.81   | 1.4118  | 33    |
| 73 00 | 0 17.86 | 1.2519  | 45    | 66 00 | 0 26.01 | 1.4151  | 34    |
| 72 50 | 18.05   | 1.2564  | 45    | 65 50 | 26.21   | 1.4185  | 34    |
| 40    | 18.23   | 1.2609  | 44    | 40    | 26.42   | 1.4219  | 34    |
| 30    | 18.42   | 1.2653  | 44    | 30    | 26.62   | 1.4253  | 33    |
| 20    | 18.61   | 1.2697  | 43    | 20    | 26.83   | 1.4286  | 33    |
| 10    | 18.79   | 1.2740  | 44    | 10    | 27.03   | 1.4319  | 33    |
| 72 00 | 0 18.98 | 1.2784  | 42    | 65 00 | 0 27.24 | 1.4352  | 33    |
| 71 50 | 19.17   | 1.2826  | 42    | 64 50 | 27.45   | 1.4385  | 33    |
| 40    | 19.36   | 1.2868  | 42    | 40    | 27.66   | 1.4418  | 33    |
| 30    | 19.55   | 1.2910  | 42    | 30    | 27.86   | 1.4451  | 32    |
| 20    | 19.73   | 1.2952  | 42    | 20    | 28.07   | 1.4483  | 32    |
| 10    | 19.92   | 1.2994  | 42    | 10    | 28.28   | 1.4515  | 32    |
| 71 00 | 0 20.11 | 1.3036  | 39    | 64 00 | 0 28.49 | 1.4547  | 32    |
| 70 50 | 20.30   | 1.3075  | 39    | 63 50 | 28.70   | 1.4579  | 32    |
| 40    | 20.49   | 1.3116  | 41    | 40    | 28.91   | 1.4611  | 32    |
| 30    | 20.69   | 1.3157  | 41    | 30    | 29.13   | 1.4643  | 31    |
| 20    | 20.88   | 1.3197  | 40    | 20    | 29.34   | 1.4674  | 32    |
| 10    | 21.07   | 1.3237  | 40    | 10    | 29.55   | 1.4706  | 30    |
| 70 00 | 0 21.26 | 1.3277  | 38    | 63 00 | 0 29.76 | 1.4736  | 32    |
| 69 50 | 21.45   | 1.3315  | 39    | 62 50 | 29.97   | 1.4768  | 31    |
| 40    | 21.65   | 1.3354  | 39    | 40    | 30.19   | 1.4799  | 30    |
| 30    | 22.84   | 1.3393  | 38    | 30    | 30.40   | 1.4829  | 31    |
| 20    | 22.03   | 1.3431  | 38    | 20    | 30.62   | 1.4860  | 30    |
| 10    | 22.23   | 1.3469  | 38    | 10    | 30.83   | 1.4890  | 31    |
| 69 00 | 0 22.42 | 1.3507  | 37    | 62 00 | 0 31.05 | 1.4921  | 31    |

*Fahrenheit's Thermometer 50°. Barometer 30 Inches.*

| Alt.  | r.      | Log. r. | Diff. | Alt.  | r.      | Log. r. | Diff. |
|-------|---------|---------|-------|-------|---------|---------|-------|
| ° ' " | ' "     |         |       | ° ' " | ' "     |         |       |
| 62 00 | 0 31.05 | 1.4921  | 31    | 55 00 | 0 40.89 | 1.6116  | 27    |
| 61 50 | 31.27   | 1.4952  | 30    | 54 50 | 41.14   | 1.6143  | 27    |
| 40    | 31.49   | 1.4982  | 31    | 40    | 41.40   | 1.6170  | 27    |
| 30    | 31.72   | 1.5013  | 30    | 30    | 41.65   | 1.6197  | 26    |
| 20    | 31.94   | 1.5043  | 30    | 20    | 41.91   | 1.6223  | 26    |
| 10    | 32.16   | 1.5073  | 29    | 10    | 42.16   | 1.6250  | 27    |
| 61 00 | 0 32.38 | 1.5102  | 31    | 54 00 | 0 42.42 | 1.6276  | 27    |
| 60 50 | 32.60   | 1.5133  | 29    | 53 50 | 42.68   | 1.6303  | 27    |
| 40    | 32.83   | 1.5162  | 30    | 40    | 42.95   | 1.6330  | 26    |
| 30    | 33.05   | 1.5192  | 29    | 30    | 43.21   | 1.6356  | 26    |
| 20    | 33.27   | 1.5221  | 29    | 20    | 43.47   | 1.6382  | 26    |
| 10    | 33.50   | 1.5250  | 29    | 10    | 43.74   | 1.6408  | 27    |
| 60 00 | 0 33.72 | 1.5279  | 29    | 53 00 | 0 44.00 | 1.6435  | 26    |
| 59 50 | 33.95   | 1.5308  | 29    | 52 50 | 44.27   | 1.6461  | 26    |
| 40    | 34.18   | 1.5337  | 29    | 40    | 44.54   | 1.6487  | 26    |
| 30    | 34.40   | 1.5366  | 29    | 30    | 44.80   | 1.6513  | 26    |
| 20    | 34.63   | 1.5395  | 29    | 20    | 45.07   | 1.6539  | 26    |
| 10    | 34.86   | 1.5423  | 29    | 10    | 45.34   | 1.6565  | 26    |
| 59 00 | 0 35.09 | 1.5452  | 29    | 52 00 | 0 45.61 | 1.6591  | 26    |
| 58 50 | 35.32   | 1.5481  | 29    | 51 50 | 45.89   | 1.6617  | 26    |
| 40    | 35.56   | 1.5510  | 28    | 40    | 46.16   | 1.6643  | 26    |
| 30    | 35.79   | 1.5538  | 28    | 30    | 46.44   | 1.6669  | 26    |
| 20    | 36.02   | 1.5566  | 28    | 20    | 46.72   | 1.6695  | 25    |
| 10    | 36.26   | 1.5594  | 28    | 10    | 46.99   | 1.6720  | 26    |
| 58 00 | 0 36.49 | 1.5622  | 28    | 51 00 | 0 47.27 | 1.6746  | 26    |
| 57 50 | 36.73   | 1.5650  | 28    | 50 50 | 47.56   | 1.6772  | 26    |
| 40    | 36.97   | 1.5678  | 29    | 40    | 47.84   | 1.6798  | 26    |
| 30    | 37.21   | 1.5707  | 28    | 30    | 48.13   | 1.6824  | 26    |
| 20    | 37.45   | 1.5735  | 27    | 20    | 48.42   | 1.6850  | 26    |
| 10    | 37.69   | 1.5762  | 28    | 10    | 48.70   | 1.6876  | 26    |
| 57 00 | 0 37.93 | 1.5790  | 28    | 50 00 | 0 48.99 | 1.6901  | 257   |
| 56 50 | 38.17   | 1.5818  | 27    | 49 50 | 49.28   | 1.69267 | 256   |
| 40    | 38.42   | 1.5845  | 28    | 40    | 49.58   | 1.69523 | 257   |
| 30    | 38.66   | 1.5873  | 27    | 30    | 49.87   | 1.69780 | 257   |
| 20    | 38.90   | 1.5900  | 27    | 20    | 50.16   | 1.70037 | 256   |
| 10    | 39.15   | 1.5927  | 27    | 10    | 50.46   | 1.70293 | 257   |
| 56 00 | 0 39.39 | 1.5954  | 27    | 49 00 | 0 50.75 | 1.70550 | 254   |
| 55 50 | 39.64   | 1.5981  | 28    | 48 50 | 51.06   | 1.70804 | 254   |
| 40    | 39.89   | 1.6009  | 27    | 40    | 51.36   | 1.71058 | 253   |
| 30    | 40.14   | 1.6036  | 27    | 30    | 51.66   | 1.71311 | 253   |
| 20    | 40.39   | 1.6063  | 27    | 20    | 51.96   | 1.71564 | 254   |
| 10    | 40.64   | 1.6090  | 26    | 10    | 52.27   | 1.71818 | 252   |
| 55 00 | 0 40.89 | 1.6116  | 27    | 48 00 | 0 52.57 | 1.72070 | 252   |

*Fahrenheit's Thermometer 50°. Barometer 30 Inches.*

| Alt.  | r.      | Log. r. | Diff. | Alt.  | r.      | Log. r. | Diff. |
|-------|---------|---------|-------|-------|---------|---------|-------|
| 0     | ' "     |         |       | 0     | ' "     |         |       |
| 48 00 | 0 52.57 | 1.72070 | 252   | 41 00 | 1 7.11  | 1.82078 | 255   |
| 47 50 | 52.88   | 1.72222 | 252   | 40 50 | 7.51    | 1.82933 | 255   |
| 40    | 53.19   | 1.72574 | 252   | 40    | 7.91    | 1.83188 | 255   |
| 30    | 53.50   | 1.72826 | 252   | 30    | 8.32    | 1.83443 | 255   |
| 20    | 53.81   | 1.73078 | 251   | 20    | 8.72    | 1.83698 | 255   |
| 10    | 54.12   | 1.73329 | 251   | 10    | 9.12    | 1.83953 | 255   |
| 47 00 | 0 54.43 | 1.73580 | 253   | 40 00 | 1 9.52  | 1.84208 | 256   |
| 46 50 | 54.75   | 1.73832 | 254   | 39 50 | 9.94    | 1.84464 | 257   |
| 40    | 55.07   | 1.74087 | 253   | 40    | 10.35   | 1.84721 | 256   |
| 30    | 55.40   | 1.74340 | 253   | 30    | 10.77   | 1.84977 | 257   |
| 20    | 55.72   | 1.74593 | 254   | 20    | 11.19   | 1.85234 | 256   |
| 10    | 56.04   | 1.74847 | 253   | 10    | 11.60   | 1.85490 | 257   |
| 46 00 | 0 56.35 | 1.75100 | 252   | 39 00 | 1 12.02 | 1.85747 | 258   |
| 45 50 | 56.68   | 1.75352 | 252   | 38 50 | 12.46   | 1.86005 | 259   |
| 40    | 57.02   | 1.75604 | 252   | 40    | 12.89   | 1.86264 | 258   |
| 30    | 57.35   | 1.75856 | 252   | 30    | 13.33   | 1.86522 | 259   |
| 20    | 57.69   | 1.76108 | 252   | 20    | 13.77   | 1.86781 | 258   |
| 10    | 58.02   | 1.76360 | 251   | 10    | 14.20   | 1.87039 | 259   |
| 45 00 | 0 58.36 | 1.76611 | 252   | 38 00 | 1 14.64 | 1.87298 | 260   |
| 44 50 | 58.70   | 1.76863 | 252   | 37 50 | 15.10   | 1.87558 | 261   |
| 40    | 59.05   | 1.77115 | 252   | 40    | 15.55   | 1.87819 | 261   |
| 30    | 59.39   | 1.77367 | 252   | 30    | 16.01   | 1.88080 | 261   |
| 20    | 59.74   | 1.77619 | 252   | 20    | 16.47   | 1.88341 | 260   |
| 10    | 1 0.08  | 1.77871 | 252   | 10    | 16.92   | 1.88601 | 262   |
| 44 00 | 1 0.43  | 1.78123 | 252   | 37 00 | 1 17.38 | 1.88863 | 262   |
| 43 50 | 0.79    | 1.78375 | 253   | 36 50 | 17.86   | 1.89125 | 262   |
| 40    | 1.15    | 1.78628 | 252   | 40    | 18.33   | 1.89387 | 263   |
| 30    | 1.50    | 1.78880 | 252   | 30    | 18.81   | 1.89650 | 263   |
| 20    | 1.86    | 1.79132 | 253   | 20    | 19.29   | 1.89913 | 263   |
| 10    | 2.21    | 1.79385 | 252   | 10    | 19.76   | 1.90176 | 264   |
| 43 00 | 1 2.57  | 1.79637 | 253   | 36 00 | 1 20.24 | 1.90440 | 265   |
| 42 50 | 2.94    | 1.79890 | 253   | 35 50 | 20.74   | 1.90705 | 265   |
| 40    | 3.31    | 1.80143 | 253   | 40    | 21.24   | 1.90970 | 266   |
| 30    | 3.69    | 1.80396 | 253   | 30    | 21.75   | 1.91236 | 266   |
| 20    | 4.06    | 1.80649 | 253   | 20    | 22.25   | 1.91502 | 267   |
| 10    | 4.43    | 1.80902 | 253   | 10    | 22.75   | 1.91769 | 267   |
| 42 00 | 1 4.80  | 1.81155 | 254   | 35 00 | 1 23.25 | 1.92036 | 268   |
| 41 50 | 5.18    | 1.81409 | 254   | 34 50 | 23.78   | 1.92304 | 269   |
| 40    | 5.57    | 1.81663 | 253   | 40    | 24.30   | 1.92573 | 268   |
| 30    | 5.95    | 1.81916 | 254   | 30    | 24.83   | 1.92841 | 271   |
| 20    | 6.34    | 1.82170 | 254   | 20    | 25.36   | 1.93112 | 270   |
| 10    | 6.72    | 1.82424 | 254   | 10    | 25.88   | 1.93382 | 270   |
| 41 00 | 1 7.11  | 1.82678 | 255   | 34 00 | 1 26.41 | 1.93653 | 271   |



*Fahrenheit's Thermometer 50°. Barometer 30 Inches.*

| Alt.  | r.      | Log. r. | Diff. | Alt.  | r.      | Log. r. | Diff. |
|-------|---------|---------|-------|-------|---------|---------|-------|
| O /   | ' "     |         |       | O /   | ' "     |         |       |
| 34 00 | 1 26.41 | 1.93653 | 271   | 27 00 | 1 54.17 | 2.05754 | 310   |
| 33 50 | 26.96   | 1.93924 | 272   | 26 50 | 54.99   | 2.06064 | 312   |
| 40    | 27.52   | 1.94196 | 273   | 40    | 55.81   | 3.06376 | 312   |
| 30    | 28.07   | 1.94469 | 273   | 30    | 56.66   | 2.06688 | 315   |
| 20    | 28.62   | 1.94742 | 274   | 20    | 57.50   | 2.07003 | 315   |
| 10    | 29.18   | 1.95016 | 275   | 10    | 58.36   | 2.07318 | 317   |
| 33 00 | 1 29.73 | 1.95291 | 275   | 26 00 | 1 59.22 | 2.07635 | 318   |
| 32 50 | 30.31   | 1.95566 | 277   | 25 50 | 2 0.09  | 2.07953 | 320   |
| 40    | 30.90   | 1.95843 | 277   | 40    | 0.99    | 2.08273 | 321   |
| 30    | 31.48   | 1.96120 | 278   | 30    | 1.88    | 2.08594 | 323   |
| 20    | 32.06   | 1.96397 | 279   | 20    | 2.80    | 2.08917 | 324   |
| 10    | 32.65   | 1.96676 | 279   | 10    | 3.71    | 2.09241 | 326   |
| 32 00 | 1 33.23 | 1.96955 | 280   | 25 00 | 2 4.65  | 2.09567 | 327   |
| 31 50 | 33.85   | 1.97235 | 281   | 24 50 | 5.59    | 2.09894 | 330   |
| 40    | 34.46   | 1.97516 | 281   | 40    | 6.54    | 2.10224 | 330   |
| 30    | 35.08   | 1.97797 | 283   | 30    | 7.51    | 2.10554 | 332   |
| 20    | 35.70   | 1.98080 | 282   | 20    | 8.49    | 2.10886 | 334   |
| 10    | 36.31   | 1.98362 | 284   | 10    | 9.48    | 2.11220 | 335   |
| 31 00 | 1 36.93 | 1.98646 | 285   | 24 00 | 2 10.48 | 2.11555 | 337   |
| 30 50 | 37.58   | 1.99931 | 285   | 23 50 | 11.50   | 2.11892 | 339   |
| 40    | 38.24   | 1.99216 | 287   | 40    | 12.52   | 2.12231 | 340   |
| 30    | 38.89   | 1.99503 | 287   | 30    | 13.57   | 2.12571 | 342   |
| 20    | 39.54   | 1.99790 | 289   | 20    | 14.62   | 2.12913 | 345   |
| 10    | 40.20   | 2.00079 | 289   | 10    | 15.70   | 2.13258 | 345   |
| 30 00 | 1 40.85 | 2.00368 | 290   | 23 00 | 2 16.78 | 2.13603 | 348   |
| 29.50 | 41.52   | 2.00658 | 291   | 22 50 | 17.88   | 2.13951 | 349   |
| 40    | 42.21   | 2.00949 | 292   | 40    | 19.00   | 2.14300 | 352   |
| 30    | 42.90   | 2.01241 | 293   | 30    | 20.13   | 2.14652 | 354   |
| 20    | 43.59   | 2.01535 | 294   | 20    | 21.28   | 2.15006 | 355   |
| 10    | 44.30   | 2.01829 | 295   | 10    | 22.43   | 2.15361 | 358   |
| 29 00 | 1 45.01 | 2.02124 | 296   | 22 00 | 2 23.61 | 2.15719 | 359   |
| 28 50 | 45.73   | 2.02420 | 298   | 21 50 | 24.81   | 2.16078 | 362   |
| 40    | 46.46   | 2.02718 | 299   | 40    | 26.02   | 2.16440 | 364   |
| 30    | 47.18   | 2.03016 | 300   | 30    | 27.25   | 2.16804 | 366   |
| 20    | 47.93   | 2.03316 | 301   | 20    | 28.50   | 2.17171 | 368   |
| 10    | 48.68   | 2.03617 | 301   | 10    | 29.76   | 2.17539 | 371   |
| 28 00 | 1 49.44 | 2.03918 | 303   | 21 00 | 2 31.04 | 2.17910 | 373   |
| 27 50 | 50.21   | 2.04221 | 304   | 20 50 | 32.34   | 2.18283 | 375   |
| 40    | 50.99   | 3.04525 | 305   | 40    | 33.67   | 2.18658 | 378   |
| 30    | 51.77   | 2.04830 | 307   | 30    | 35.01   | 2.19036 | 381   |
| 20    | 52.57   | 2.05137 | 308   | 20    | 36.37   | 2.19417 | 383   |
| 10    | 53.36   | 2.05445 | 309   | 10    | 37.76   | 2.19800 | 385   |
| 27 00 | 1 54.17 | 2.05754 | 310   | 20 00 | 2 39.16 | 2.20185 | 388   |

*Fahrenheit's Thermometer 50°. Barometer 30 Inches.*

| Alt.  | r.      | Log. r. | Diff. | Alt.  | r.      | Log. r. | Diff. |
|-------|---------|---------|-------|-------|---------|---------|-------|
| 20 00 | 2 39.16 | 2.20165 | 388   | 13 00 | 4 7.91  | 2.39430 | 557   |
| 19 50 | 40.59   | 2.20573 | 390   | 12 50 | 11.11   | 2.39987 | 563   |
| 40    | 42.04   | 2.20963 | 393   | 40    | 14.39   | 2.40550 | 569   |
| 30    | 43.52   | 2.21356 | 396   | 30    | 17.74   | 2.41119 | 576   |
| 20    | 45.02   | 2.21752 | 398   | 20    | 21.19   | 2.41695 | 583   |
| 10    | 46.53   | 2.22150 | 402   | 10    | 24.72   | 2.42278 | 589   |
| 19 00 | 2 48.08 | 2.22552 | 404   | 12 00 | 4 28.33 | 2.42867 | 596   |
| 18 50 | 49.65   | 2.22956 | 407   | 11 50 | 32.04   | 2.43463 | 603   |
| 40    | 51.25   | 2.23363 | 410   | 40    | 35.84   | 2.44066 | 611   |
| 30    | 52.87   | 2.23773 | 413   | 30    | 39.75   | 2.44677 | 618   |
| 20    | 54.53   | 2.24186 | 417   | 20    | 43.76   | 2.45295 | 626   |
| 10    | 56.21   | 2.24603 | 419   | 10    | 47.88   | 2.45921 | 635   |
| 18 00 | 2 57.92 | 2.25022 | 423   | 11 00 | 4 52.12 | 2.46556 | 642   |
| 17 50 | 59.66   | 2.25445 | 425   | 10 50 | 56.47   | 2.47198 | 650   |
| 40    | 3 1.43  | 2.25870 | 429   | 40    | 5 0.94  | 2.47848 | 659   |
| 30    | 3.23    | 2.26299 | 433   | 30    | 5.54    | 2.48507 | 669   |
| 20    | 5.06    | 2.26732 | 436   | 20    | 10.28   | 2.49176 | 677   |
| 10    | 6.93    | 2.27168 | 440   | 10    | 15.16   | 2.49853 | 688   |
| 17 00 | 3 8.83  | 2.27608 | 443   | 10 00 | 5 20.19 | 2.50541 | 696   |
| 16 50 | 10.77   | 2.28051 | 447   | 9 50  | 25.86   | 2.51237 | 707   |
| 40    | 12.74   | 2.28498 | 450   | 40    | 30.70   | 2.51944 | 716   |
| 30    | 14.75   | 2.28948 | 454   | 30    | 36.20   | 2.52660 | 727   |
| 20    | 16.80   | 2.29402 | 458   | 20    | 41.88   | 2.53387 | 738   |
| 10    | 18.88   | 2.29860 | 462   | 10    | 47.74   | 2.54125 | 749   |
| 16 00 | 3 21.01 | 2.30322 | 467   | 9 00  | 5 53.79 | 2.54874 | 759   |
| 15 50 | 23.18   | 2.30789 | 470   | 8 50  | 6 0.04  | 2.55635 | 772   |
| 40    | 25.39   | 2.31259 | 475   | 40    | 6.50    | 2.56407 | 785   |
| 30    | 27.66   | 2.31734 | 479   | 30    | 13.18   | 2.57192 | 797   |
| 20    | 29.95   | 2.32213 | 483   | 20    | 20.09   | 2.57989 | 811   |
| 10    | 32.30   | 2.32696 | 488   | 10    | 27.26   | 2.58800 | 824   |
| 15 00 | 3 34.70 | 2.33184 | 493   | 8 00  | 6 34.68 | 2.59624 | 838   |
| 14 50 | 37.16   | 2.33677 | 497   | 7 50  | 42.37   | 2.60462 | 851   |
| 40    | 39.65   | 2.34174 | 502   | 40    | 50.33   | 2.61313 | 866   |
| 30    | 42.21   | 2.34676 | 507   | 30    | 58.59   | 2.62179 | 883   |
| 20    | 44.82   | 2.35183 | 512   | 20    | 7 7.19  | 2.63062 | 899   |
| 10    | 47.48   | 2.35695 | 517   | 10    | 16.13   | 2.63961 | 914   |
| 14 00 | 3 50.21 | 2.36212 | 523   | 7 00  | 7 25.40 | 2.64875 | 931   |
| 13 50 | 53.00   | 2.36735 | 528   | 6 50  | 35.05   | 2.65806 | 949   |
| 40    | 55.85   | 2.37263 | 533   | 40    | 45.10   | 2.66755 | 967   |
| 30    | 58.76   | 2.37796 | 538   | 30    | 55.58   | 2.67722 | 986   |
| 20    | 4 1.74  | 2.38334 | 545   | 20    | 8 6.50  | 2.68708 | 1006  |
| 10    | 4.79    | 2.38879 | 551   | 10    | 17.90   | 2.69714 | 1026  |
| 13 00 | 4 7.91  | 2.39430 | 557   | 6 00  | 8 29.80 | 2.70740 | 1047  |

*Fahrenheit's Thermometer 50°. Barometer 30 Inches.*

| Alt.  | r.       | Log. r. | Diff. | Alt.  | r.       | Log. r. | Diff. |
|-------|----------|---------|-------|-------|----------|---------|-------|
| ° ' " |          |         |       | ° ' " |          |         |       |
| 6 00  | 8 29.80  | 2.70740 | 1047  | 3 00  | 14 26.04 | 2.93754 | 1608  |
| 5 50  | 42.24    | 2.71787 | 1069  | 2 50  | 58.71    | 2.95362 | 1654  |
| 40    | 55.25    | 2.72856 | 1092  | 40    | 15 33.60 | 2.97016 | 1701  |
| 30    | 9 8.88   | 2.73948 | 1115  | 30    | 16 10.89 | 2.98717 | 1749  |
| 20    | 23.16    | 2.75063 | 1139  | 20    | 50.8     | 3.00466 | 1801  |
| 10    | 38.12    | 2.76202 | 1165  | 10    | 17 33.6  | 3.02267 | 1855  |
| 5 00  | 9 53.84  | 2.77367 | 1191  | 2 00  | 18 19.6  | 3.04122 | 1909  |
| 4 50  | 10 10.35 | 2.78558 | 1219  | 1 50  | 19 9.0   | 3.06031 | 1967  |
| 40    | 27.73    | 2.79777 | 1248  | 40    | 20 2.2   | 3.07998 | 2026  |
| 30    | 46.03    | 2.81025 | 1277  | 30    | 59.6     | 3.10024 | 2089  |
| 20    | 11 5.30  | 2.82302 | 1309  | 20    | 22 1.7   | 3.12113 | 2155  |
| 10    | 25.66    | 2.83611 | 1340  | 10    | 23 8.9   | 3.14268 | 2221  |
| 4 00  | 11 47.15 | 2.84951 | 1374  | 1 00  | 24 21.8  | 3.16489 | 2290  |
| 3 50  | 12 9.68  | 2.86325 | 1410  | 0 50  | 25 40.9  | 3.18779 | 2361  |
| 40    | 33.97    | 2.87735 | 1447  | 40    | 27 7.1   | 3.21140 | 2434  |
| 30    | 59.51    | 2.89182 | 1484  | 30    | 28 40.8  | 3.23574 | 2509  |
| 20    | 13 26.61 | 2.90666 | 1523  | 20    | 30 23.2  | 3.26083 | 2584  |
| 10    | 55.40    | 2.92189 | 1565  | 10    | 32 15.0  | 3.28667 | 2667  |
| 3 00  | 14 26.04 | 2.93754 | 1608  | 0 00  | 34 17.5  | 3.31334 |       |

In ordinary cases it will be sufficient to apply to the observed altitude the Mean Refraction standing against it in the adjoining column. Where greater accuracy is required, the corresponding log.  $r$  must be taken. In the Table of Corrections on the following page, for the Barometer and Thermometers, the proportional parts of log.  $t$ , for tenths of a degree of Fahrenheit, will be found in the column adjoining that of log.  $t$ , standing against the corresponding units of the argument. In the same manner the proportional parts of log.  $\beta$ , for hundredths of an inch, will be found standing against the corresponding tenths. These must be added or subtracted according to the sign at the top of the column. The proportional parts of log.  $\tau$ , for tenths of a degree, will be found at the bottom. The sum of logs.  $r$ ,  $t$ ,  $\beta$ , and  $\tau$ , will be the log. of the refraction, which must be subtracted from the observed altitude, or added to the observed zenith distance.

The column *Barometer* contains the Logarithms of  $\frac{p}{30}$ ,  $p$  being the height of the Barometer in English Inches.

*Corrections, depending on the state of the Thermometer and Barometer, to be applied to the foregoing Mean Refractions.*

| External Thermometer. |         |       |     |         |       | Barometer. |                |       | Internal Thermometer. |               |     |             |
|-----------------------|---------|-------|-----|---------|-------|------------|----------------|-------|-----------------------|---------------|-----|-------------|
| Th.                   | Log. t. | P. P. | Th. | Log. t. | P. P. | Bar.       | Log. $\beta$ . | P. P. | Th.                   | Log. $\tau$ . | Th. | Log. $\tau$ |
| °                     |         |       | °   |         |       |            |                |       | °                     |               | °   |             |
| 10                    | 0.03779 | —     | 50  | 0.00000 | —     | 26.6       | 9.94776        |       | 10                    | 0.00173       | 50  | 0.00000     |
| 1                     | 0.03680 | 10    | 1   | 9.99910 | 9     | 7          | 9.94939        |       | 11                    | 0.00169       | 51  | 9.99996     |
| 2                     | 0.03582 | 20    | 2   | 9.99820 | 18    | 8          | 9.95101        |       | 12                    | 0.00164       | 52  | 9.99991     |
| 3                     | 0.03484 | 30    | 3   | 9.99730 | 27    | 9          | 9.95263        |       | 13                    | 0.00160       | 53  | 9.99987     |
| 4                     | 0.03386 | 39    | 4   | 9.99640 | 36    |            |                |       | 14                    | 0.00156       | 54  | 9.99983     |
| 5                     | 0.03288 | 49    | 5   | 9.99550 | 45    | 27.0       | 9.95484        |       | 15                    | 0.00151       | 55  | 9.99978     |
| 6                     | 0.03191 | 59    | 6   | 9.99460 | 54    | 1          | 9.95584        |       | 16                    | 0.00147       | 56  | 9.99974     |
| 7                     | 0.03094 | 69    | 7   | 9.99371 | 63    | 2          | 9.95745        |       | 17                    | 0.00143       | 57  | 9.99970     |
| 8                     | 0.02997 | 78    | 8   | 9.99282 | 72    | 3          | 9.95904        |       | 18                    | 0.00138       | 58  | 9.99965     |
| 9                     | 0.02900 | 88    | 9   | 9.99193 | 81    | 4          | 9.96063        |       | 19                    | 0.00134       | 59  | 9.99961     |
|                       |         |       |     |         |       | 5          | 9.96221        |       |                       |               |     |             |
| 90                    | 0.02803 |       | 60  | 0.99104 |       | 6          | 9.96379        |       | 20                    | 0.00130       | 60  | 9.99957     |
| 1                     | 0.02706 | 10    | 1   | 9.99016 | 9     | 7          | 9.96536        |       | 21                    | 0.00126       | 61  | 9.99953     |
| 2                     | 0.02609 | 19    | 2   | 9.98927 | 18    | 8          | 9.96692        |       | 22                    | 0.00121       | 62  | 9.99948     |
| 3                     | 0.02514 | 29    | 3   | 9.98839 | 26    | 9          | 9.96848        |       | 23                    | 0.00117       | 63  | 9.99944     |
| 4                     | 0.02418 | 38    | 4   | 9.98751 | 35    |            |                |       | 24                    | 0.00113       | 64  | 9.99940     |
| 5                     | 0.02323 | 48    | 5   | 9.98663 | 44    | 28.0       | 9.97004        | +     | 25                    | 0.00108       | 65  | 9.99935     |
| 6                     | 0.02227 | 58    | 6   | 9.98575 | 53    | 1          | 9.97158        | 15    | 26                    | 0.00104       | 66  | 9.99931     |
| 7                     | 0.02132 | 67    | 7   | 9.98488 | 62    | 2          | 9.97313        | 30    | 27                    | 0.00100       | 67  | 9.99927     |
| 8                     | 0.02037 | 77    | 8   | 9.98401 | 70    | 3          | 9.97466        | 46    | 28                    | 0.00095       | 68  | 9.99922     |
| 9                     | 0.01942 | 86    | 9   | 9.98314 | 79    | 4          | 9.97620        | 61    | 29                    | 0.00091       | 69  | 9.99918     |
|                       |         |       |     |         |       | 5          | 9.97772        | 76    |                       |               |     |             |
| 30                    | 0.01848 |       | 70  | 9.98227 |       | 6          | 9.97924        | 91    | 30                    | 0.00087       | 70  | 9.99913     |
| 1                     | 0.01754 | 9     | 1   | 9.98140 | 9     | 7          | 9.98076        | 106   | 31                    | 0.00083       | 71  | 9.99909     |
| 2                     | 0.01660 | 19    | 2   | 9.98054 | 17    | 8          | 9.98227        | 122   | 32                    | 0.00078       | 72  | 9.99904     |
| 3                     | 0.01566 | 28    | 3   | 9.97967 | 26    | 9          | 9.98378        | 137   | 33                    | 0.00074       | 73  | 9.99900     |
| 4                     | 0.01472 | 38    | 4   | 9.97881 | 34    |            |                |       | 34                    | 0.00070       | 74  | 9.99896     |
| 5                     | 0.01379 | 47    | 5   | 9.97795 | 43    | 29.0       | 9.98528        |       | 35                    | 0.00065       | 75  | 9.99891     |
| 6                     | 0.01285 | 56    | 6   | 9.97709 | 52    | 1          | 9.98677        | 15    | 36                    | 0.00061       | 76  | 9.99887     |
| 7                     | 0.01192 | 66    | 7   | 9.97623 | 60    | 2          | 9.98826        | 29    | 37                    | 0.00057       | 77  | 9.99883     |
| 8                     | 0.01099 | 75    | 8   | 9.97537 | 69    | 3          | 9.98975        | 44    | 38                    | 0.00052       | 78  | 9.99878     |
| 9                     | 0.01006 | 85    | 9   | 9.97452 | 77    | 4          | 9.99123        | 59    | 39                    | 0.00048       | 79  | 9.99874     |
|                       |         |       |     |         |       | 5          | 9.99270        | 73    |                       |               |     |             |
| 40                    | 0.00914 |       | 80  | 9.97367 |       | 6          | 9.99417        | 88    | 40                    | 0.00043       | 80  | 9.99870     |
| 1                     | 0.00822 | 9     | 1   | 9.97282 | 8     | 7          | 9.99563        | 103   | 41                    | 0.00039       | 81  | 9.99866     |
| 2                     | 0.00730 | 18    | 2   | 9.97197 | 17    | 8          | 9.99709        | 118   | 42                    | 0.00034       | 82  | 9.99861     |
| 3                     | 0.00638 | 28    | 3   | 9.97112 | 25    | 9          | 9.99855        | 132   | 43                    | 0.00030       | 83  | 9.99857     |
| 4                     | 0.00546 | 37    | 4   | 9.97027 | 34    |            |                |       | 44                    | 0.00026       | 84  | 9.99853     |
| 5                     | 0.00455 | 46    | 5   | 9.96943 | 42    | 30.0       | 0.00000        |       | 45                    | 0.00021       | 85  | 9.99848     |
| 6                     | 0.00363 | 55    | 6   | 9.96859 | 50    | 1          | 0.00145        | 14    | 46                    | 0.00017       | 86  | 9.99844     |
| 7                     | 0.00272 | 64    | 7   | 9.96775 | 59    | 2          | 0.00289        | 29    | 47                    | 0.00013       | 87  | 9.99840     |
| 8                     | 0.00181 | 74    | 8   | 9.96691 | 67    | 3          | 0.00432        | 43    | 48                    | 0.00008       | 88  | 9.99835     |
| 9                     | 0.00090 | 83    | 9   | 9.96607 | 76    | 4          | 0.00575        | 57    | 49                    | 0.00004       | 89  | 9.99831     |
| 50                    | 0.00000 |       | 90  | 9.96524 |       | 5          | 0.00718        | 71    | 50                    | 0.00000       | 90  | 9.99827     |
|                       |         |       |     |         |       | 6          | 0.00860        | 86    |                       |               |     |             |
|                       |         |       |     |         |       | 7          | 0.01002        | 100   |                       |               |     |             |
|                       |         |       |     |         |       | 8          | 0.01143        | 114   |                       |               |     |             |
|                       |         |       |     |         |       | 9          | 0.01284        | 129   |                       |               |     |             |
|                       |         |       |     |         |       | 31.0       | 0.01424        |       |                       |               |     |             |

P. P. to tenths of a Degree.  
 .1 .2 .3 .4 .5 .6 .7 .8 .9  
 — 0 1 1 2 3 3 3 3 4

IV. *The Transit Instrument.*

Knowing the apparent right ascension of a star, to compute the corrections to its observed transit on account of the three principal errors of the Transit instrument—in Azimuth, in the Inclination of the axis, and in Collimation—in order to obtain the correct clock error.

$$E = T + a \cdot \frac{\sin(L-D)}{\cos D} + b \frac{\cos(L-D)}{\cos D} + \frac{c}{\cos D} - AR$$

$E$  = the error of the clock ; *minus* when slow.

$T$  = the observed time of transit.

$L$  = the latitude of the place.

$D$  = the declination of the star : *plus* when North, and *minus* when South, for the upper culminations ; and *vice versa* for the lower culminations.

$a$  = the deviation of the telescope is azimuth ; *plus* when (pointing to the South) the vertical which it describes falls to the East ; and *minus* when it falls to the West ; and *vice versa* when pointing to the North.

$b$  = the bias or inclination of the axis of the telescope : *plus*, when the west end of the axis is too high.

$c$  = the error in collimation : *plus*, when the circle, described by the optical axis of the telescope (pointing to the South) falls to the East ; and *minus*, when it falls to the West ; and *vice versa* when pointing to the North.

$AR$  = the Right Ascension of the star ; when the clock marks mean solar time, the mean time of transit of the object over the meridian must be substituted for  $AR$ .

1. To determine the value (*in time*) of the co-efficients  $a$ ,  $b$ ,  $c$ , in the preceding formula.

*For inclination of the axis of the telescope :*

$$b = \frac{d}{60} \left\{ (w + w') - (e + e') \right\}$$

Where  $w'$  and  $e'$  denote respectively the values of  $w$  and  $e$ , after *reversing the level*,

$d$  = the value of each division of the level, in seconds of space.

$w$  = the inclination of the level to the West.

$e$  = the inclination of the level to the East.

*For collimation :*

$$c = \frac{1}{2} (t' - t) \cos D + \frac{1}{2} (b' - b) \cos (L - D.)$$

Where  $t'$  and  $b'$  denote respectively the values of  $t$  and  $b$ , after *reversing the instrument*,

$D$  = the declination of a circumpolar star.

$t$  = the time of the transit of the circumpolar star, deduced from an observation at a given *side wire* of the instrument.

*For the deviation in azimuth :*

By observations of a circumpolar star :

$$a = \frac{12^h - (T' - T)}{2 \cos L \tan D} + \frac{b \cos (L - D) - b' \cos (L + D) + 2c}{2 \cos L \sin D}$$

Where  $T'$  and  $b'$  denote respectively the values of  $T$  and  $b$ , at the *lower culmination*.

Deviation in azimuth by transits of a high and low star.

$$a = \left\{ (AR' - AR) - (T' - T) \right\} \times \frac{\cos D' \cos D}{\cos L \sin (D' - D)}$$

Where  $T'$ ,  $AR'$ , and  $D'$ , denote respectively the values of  $T$ ,  $AR$ , and  $D$  of the *second* star observed,

or make  $\frac{\sin (L - D)}{\cos D}$  for the *first* star =  $n$

and  $\frac{\sin (L - D')}{\cos D'}$  for the *second* star =  $n'$

$$\text{then } a = \frac{(AR' - AR) - (T' - T)}{n' - n}$$

$n$  is negative for a star north of the zenith.

2. To find the equatorial interval of each wire from the central wire, observe the transit of a star of any declination  $D$ , then

Equatorial interval = observed interval  $\times \cos D$ .

3. When the intervals on each side of the central wire are equal, the mean of the times of transit over each wire will denote the transit over the middle wire. But should they not be equal, a correction must be applied to obtain a correct mean.

Call I. II; IV. V, the equatorial intervals of each wire from the central wire, the instrument having, say 5 wires, then

$$\text{Reduction to middle wire} = \frac{(I + II) - (IV + V)}{5 \cos D}$$

*Numerical values of  $\frac{\sin (L - D)}{\cos D}$ ;  $\frac{\cos (L - D)}{\cos D}$ ;  $\frac{1}{\cos D}$   
for facilitating the method of determining the deviation  
of the Transit Instrument in Azimuth, by means of "high  
and low stars."*

| For<br>Deviation.       | Star's Declination = $\pm D$ |       |       |       |       |       |       | For Level.              |
|-------------------------|------------------------------|-------|-------|-------|-------|-------|-------|-------------------------|
| Star's Z D<br>= (L - D) | 1°                           | 10°   | 20°   | 30°   | 40°   | 50°   | 60°   | Star's Z D<br>= (L - D) |
| 1°                      | .02                          | .02   | .02   | .02   | .02   | .03   | .03   | 89°                     |
| 5                       | .08                          | .08   | .09   | .10   | .11   | .13   | .17   | 85                      |
| 10                      | .17                          | .17   | .18   | .20   | .23   | .27   | .35   | 80                      |
| 15                      | .26                          | .26   | .27   | .30   | .34   | .40   | .52   | 75                      |
| 20                      | .34                          | .34   | .36   | .39   | .45   | .53   | .68   | 70                      |
| 25                      | .42                          | .43   | .45   | .48   | .55   | .66   | .84   | 65                      |
| 30                      | .50                          | .51   | .53   | .57   | .65   | .77   | 1.00  | 60                      |
| 35                      | .57                          | .58   | .61   | .66   | .75   | .89   | 1.15  | 55                      |
| 40                      | .64                          | .65   | .68   | .74   | .84   | 1.00  | 1.28  | 50                      |
| 45                      | .71                          | .72   | .75   | .81   | .92   | 1.10  | 1.41  | 45                      |
| 50                      | .76                          | .78   | .81   | .88   | 1.00  | 1.19  | 1.53  | 40                      |
| 55                      | .82                          | .83   | .87   | .94   | 1.07  | 1.27  | 1.64  | 35                      |
| 60                      | .86                          | .88   | .92   | 1.00  | 1.13  | 1.35  | 1.73  | 30                      |
| 65                      | .90                          | .92   | .96   | 1.05  | 1.18  | 1.41  | 1.81  | 25                      |
| 70                      | .94                          | .95   | 1.00  | 1.08  | 1.23  | 1.46  | 1.88  | 20                      |
| 75                      | .96                          | .98   | 1.03  | 1.11  | 1.26  | 1.50  | 1.93  | 15                      |
| 80                      | .98                          | 1.00  | 1.05  | 1.14  | 1.28  | 1.53  | 1.97  | 10                      |
| 85                      | .99                          | 1.01  | 1.06  | 1.15  | 1.30  | 1.55  | 1.99  | 5                       |
| 89                      | 1.00                         | 1.01  | 1.06  | 1.15  | 1.30  | 1.55  | 1.99  | 1                       |
| For Collimation.        | 1.000                        | 1.015 | 1.064 | 1.154 | 1.305 | 1.555 | 2.000 | $\frac{1}{\cos D}$      |



**STATION**

*Computation of the corrections a and b, in the preceding Transits.*

Declination of  $\pi$  Capri. =  $18^{\circ} 42' S.$   
 Latitude of Station = L =  $43^{\circ} 13'$       14 Capri. =  $15^{\circ} 29' S.$   
                                                                $\alpha$  Cygni =  $44^{\circ} 44' N.$

**Level correction of  $\pi$  Capricorni.**

|                                                                            |                                        |                 |
|----------------------------------------------------------------------------|----------------------------------------|-----------------|
| L = 43° 13'                                                                | E. 32.2                                | W. 33           |
| D = -18° 42'                                                               | 32.2                                   | 33              |
| (L - D) = 61° 55'                                                          | 64.4                                   | 66              |
| from table page 185.                                                       |                                        |                 |
|                                                                            |                                        | 66 - 64.4 = 1.6 |
| $\cos \frac{(L-D)}{\cos D} = 0.50$                                         | $b = \frac{7.5}{60} \times 1.6 = 0.20$ |                 |
| Level correction = $b \frac{\cos (L-D)}{\cos D} = 0.20 \times 0.50 = 0.10$ |                                        |                 |

### *Deviation in Azimuth.*

$$a = \frac{(AR' - AR) - (T' - T)}{n' - n}$$

**T'** and **T** being the times of transit corrected for level and collimation.  
Combining  $\pi$  Capri. and  $\alpha$  Cygni.

$$\begin{array}{rcl} \text{H. M. S.} & & \text{H. M. S.} \\ \text{AR}' = 20 \ 36 \ 15.80 & & \text{T}' = 20 \ 35 \ 52.22 \\ \text{AR} = 20 \ 18 \ 36.66 & & \text{T} = 20 \ 18 \ 12.91 \\ \hline & & 17 \ 39.31 \\ & & \hline & & 17 \ 39.31 \\ (\text{AR}' - \text{AR}) - (\text{T}' - \text{T}) = -0.17 & n' = \frac{(\sin L - D')}{\cos D'} = \frac{\sin (-1^\circ 31')}{\cos 44^\circ 44'} = -0.03 \\ & n = \frac{\sin (L - D)}{\cos D} = \frac{\sin 61^\circ 55'}{\cos 18^\circ 42'} = +0.93 \\ a = \frac{-0.17}{-0.03 - 0.93} = \frac{.17}{.96} = +0.18 \end{array}$$

Combining 14 Capri. and  $\alpha$  Cygni,  $a = +0^{\circ}.19$ .

$$\text{Correction for deviation in Azimuth of } \pi \text{ Capricorni} = a \frac{\sin (L-D)}{\cos D} = 0^{\circ}.18 \times 0.93 = 0^{\circ}.17$$

*Transit Instrument—Continued.*

*Rules for the direction of the deviation in azimuth, in the method of fixing a Transit Instrument in the meridian by "high and low stars."*

| Position of Stars.                                                         | Culmination.                          | Precedence.                     | Relative magnitude of Intervals. | Deviation. |
|----------------------------------------------------------------------------|---------------------------------------|---------------------------------|----------------------------------|------------|
| Both south, or both north, or one south and the other north of the zenith. | Both upper                            | Highest or nearest to the Pole. | Obs'd greater.                   | W. of S.   |
|                                                                            | "                                     | "                               | Obs'd less.                      | E. of S.   |
|                                                                            | "                                     | Furthest from the Pole.         | Obs'd greater.                   | E. of S.   |
|                                                                            | "                                     | "                               | Obs'd less.                      | W. of S.   |
| One north, and the other south of the zenith.                              | The northern being the lower culm'n.  | Nearest to the Pole.            | Obs'd less.                      | E. of N.   |
|                                                                            |                                       |                                 | Obs'd greater.                   | W. of N.   |
|                                                                            | The southern being upper culmination. | Farthest from the Pole.         | Obs'd less.                      | W. of N.   |
|                                                                            |                                       |                                 | Obs'd greater.                   | E. of N.   |
| Both north of the zenith.                                                  | One upper and one lower.              | Upper.                          | Obs'd greater.                   | E. of N.   |
|                                                                            |                                       | Upper.                          | Obs'd less.                      | W. of N.   |
|                                                                            |                                       | Lower.                          | Obs'd greater.                   | W. of N.   |
|                                                                            |                                       | Lower.                          | Obs'd less.                      | E. of N.   |

## LATITUDE.

*V. To determine the Latitude from the meridional altitude of an object whose declination is known.*

1. When the object observed is south of the zenith:

$$L = 90^\circ + D - A = Z + D = 90^\circ + Z - \Delta = 180^\circ - (A + \Delta)$$

2. When the star is between the zenith and the pole:

$$L = A - \Delta = D - Z = 90^\circ - (Z + \Delta) = A + D - 90^\circ$$

3. When the star is between the pole and the horizon to the north:

$$L = A + \Delta = 90^\circ + \Delta - Z = 90^\circ + A - D = 180^\circ - (Z + D)$$

where  $L$  = the latitude sought.

$D$  = the declination of the object, *minus* when south,

$\Delta$  = its north polar distance,

$A$  = its meridional altitude,

$Z$  = its meridional zenith distance,

$A$  and  $Z$  must be corrected for refraction ; when the sun is the object observed,  $A$  = observed altitude — (refraction — parallax)  $\pm$  semi-diam.

VI. *Determination of the Latitude of a place by the method of circum-meridian altitudes.*

Reduction to meridian =

$$x = k \left\{ i \frac{\cos l \cos D}{\cos a} \right\} - m \tan a \left\{ i \frac{\cos l \cos D}{\cos a} \right\}^2$$

$$k = \frac{2 \sin^2 \frac{1}{2} p}{\sin 1''} \quad m = \frac{2 \sin^4 \frac{1}{2} p}{\sin 1''}$$

$$a = 90^\circ + D - l$$

$A = a + x$  = the meridional altitude of the object,

$a$  = its observed altitude—(refraction—parallax)  $\pm$  semi-diameter.

$p$  = its correct hour angle,

$D$  = its declination,

$l$  = the assumed latitude of the place,

$x$  = the required correction in seconds.

When a *star* is the object observed and the chronometer marks *mean* time,  $i = 1.005473$ ,  $\log i = 0.0023708$

When the *sun* is observed and the chronometer marks *sidereal* time,  $i = 0.99455418$ ,  $\log i = 9.9976285$ ; and generally, when the chronometer has a large losing rate,  $x$  must be multiplied by  $1 + 0.90002315 r$ ; when it has a gaining rate it must be divided by  $1 + 0.0002315 r$ ;  $r$  being the rate in 24 hours, which must be assumed *minus* when *gaining*, and *plus* when *losing*.

The values of  $k$  and  $m$  for each value of  $p$ , are given in the following tables.

The meridian altitude  $A = a + x$  for each observation; for any number of observations  $n$ ,  $\frac{a' + a'' + \dots}{n} + \frac{x' + x'' + \dots}{n} =$  the mean,  $a$ , of all the observed altitudes  $+$  the mean,  $x$ , of all the corrections. Consequently,

1. Measure several successive altitudes of the object both before and after its meridional passage.

2. Note the times of each observation, and compute the time of the object's culmination; the differences between this and the times of each successive observation are the values of  $p'$ ,  $p''$ , etc., in time, for which the corresponding values of  $k'$ ,  $k''$ , etc., and  $m'$ ,  $m''$ , etc., must be taken from the tables.

3. The means  $k$  and  $m$  of these results will be introduced into the equation for the value of the correction,  $x$ , to be applied to  $a$  to obtain the meridional altitude,  $A$ , of the object.

4. If the final latitude differ much from the assumed, the computation should be repeated with the new value for  $l$ .

5. It is not necessary that the time of the object's culmination should be known with great precision, provided an equal number of altitudes be taken upon each side of the meridian, and at nearly equal distances from it.

6. The second correction,  $m$ , is seldom necessary, unless great accuracy is desired, and the object is observed more than ten minutes of time from the meridian.

*Reduction to the Meridian; values of  $k = \frac{2 \sin^2 \frac{1}{2} p}{\sin 1''}$*

| Sec. | 0 <sup>m</sup> | 1 <sup>m</sup> | 2 <sup>m</sup> | 3 <sup>m</sup> | 4 <sup>m</sup> | 5 <sup>m</sup> | 6 <sup>m</sup> | 7 <sup>m</sup> |
|------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
|      | "              | "              | "              | "              | "              | "              | "              | "              |
| 0    | 0.0            | 2.0            | 7.8            | 17.7           | 31.4           | 49.1           | 70.7           | 96.2           |
| 1    | 0.0            | 2.0            | 8.0            | 17.9           | 31.7           | 49.4           | 71.1           | 96.7           |
| 2    | 0.0            | 2.1            | 8.1            | 18.1           | 31.9           | 49.7           | 71.5           | 97.1           |
| 3    | 0.0            | 2.2            | 8.2            | 18.3           | 32.2           | 50.1           | 71.9           | 97.6           |
| 4    | 0.0            | 2.2            | 8.4            | 18.5           | 32.5           | 50.4           | 72.3           | 98.0           |
| 5    | 0.0            | 2.3            | 8.5            | 18.7           | 32.7           | 50.7           | 72.7           | 98.5           |
| 6    | 0.0            | 2.4            | 8.7            | 18.9           | 33.0           | 51.1           | 73.1           | 99.0           |
| 7    | 0.0            | 2.4            | 8.8            | 19.1           | 33.3           | 51.4           | 73.5           | 99.4           |
| 8    | 0.0            | 2.5            | 8.9            | 19.3           | 33.5           | 51.7           | 73.9           | 99.9           |
| 9    | 0.0            | 2.6            | 9.1            | 19.5           | 33.8           | 52.1           | 74.3           | 100.4          |
| 10   | 0.1            | 2.7            | 9.2            | 19.7           | 34.1           | 52.4           | 74.7           | 100.8          |
| 11   | 0.1            | 2.7            | 9.4            | 19.9           | 34.4           | 52.7           | 75.1           | 101.3          |
| 12   | 0.1            | 2.8            | 9.5            | 20.1           | 34.6           | 53.1           | 75.5           | 101.8          |
| 13   | 0.1            | 2.9            | 9.6            | 20.3           | 34.9           | 53.4           | 75.9           | 102.3          |
| 14   | 0.1            | 3.0            | 9.8            | 20.5           | 35.2           | 53.8           | 76.3           | 102.7          |
| 15   | 0.1            | 3.1            | 9.9            | 20.7           | 35.5           | 54.1           | 76.7           | 103.2          |
| 16   | 0.1            | 3.1            | 10.1           | 20.9           | 35.7           | 54.5           | 77.1           | 103.7          |
| 17   | 0.2            | 3.2            | 10.2           | 21.2           | 36.0           | 54.8           | 77.5           | 104.2          |
| 18   | 0.2            | 3.3            | 10.4           | 21.4           | 36.3           | 55.1           | 77.9           | 104.6          |
| 19   | 0.2            | 3.4            | 10.5           | 21.6           | 36.6           | 55.5           | 78.3           | 105.1          |
| 20   | 0.2            | 3.5            | 10.7           | 21.8           | 36.9           | 55.8           | 78.8           | 105.6          |
| 21   | 0.2            | 3.6            | 10.8           | 22.0           | 37.2           | 56.2           | 79.2           | 106.1          |
| 22   | 0.3            | 3.7            | 11.0           | 22.3           | 37.4           | 56.5           | 79.6           | 106.6          |
| 23   | 0.3            | 3.8            | 11.2           | 22.5           | 37.7           | 56.9           | 80.0           | 107.0          |
| 24   | 0.3            | 3.8            | 11.3           | 22.7           | 38.0           | 57.3           | 80.4           | 107.5          |
| 25   | 0.3            | 3.9            | 11.5           | 22.9           | 38.3           | 57.6           | 80.8           | 108.0          |
| 26   | 0.4            | 4.0            | 11.6           | 23.1           | 38.6           | 58.0           | 81.3           | 108.5          |
| 27   | 0.4            | 4.1            | 11.8           | 23.4           | 38.9           | 58.3           | 81.7           | 109.0          |
| 28   | 0.4            | 4.2            | 11.9           | 23.6           | 39.2           | 58.7           | 82.1           | 109.5          |
| 29   | 0.5            | 4.3            | 12.1           | 23.8           | 39.5           | 59.0           | 82.5           | 110.0          |

*Reduction to the Meridian; values of  $k = \frac{2 \sin^2 \frac{1}{2} p}{\sin 1''}$*

| Sec. | 0 <sup>m</sup> | 1 <sup>m</sup> | 2 <sup>m</sup> | 3 <sup>m</sup> | 4 <sup>m</sup> | 5 <sup>m</sup> | 6 <sup>m</sup> | 7 <sup>m</sup> |
|------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
|      | "              | "              | "              | "              | "              | "              | "              | "              |
| 30   | 0.5            | 4.4            | 12.3           | 24.0           | 39.8           | 59.4           | 83.0           | 110.4          |
| 31   | 0.5            | 4.5            | 12.4           | 24.3           | 40.1           | 59.8           | 83.4           | 110.9          |
| 32   | 0.6            | 4.6            | 12.6           | 24.5           | 40.3           | 60.1           | 83.8           | 111.4          |
| 33   | 0.6            | 4.7            | 12.8           | 24.7           | 40.6           | 60.5           | 84.2           | 111.9          |
| 34   | 0.6            | 4.8            | 12.9           | 25.0           | 40.9           | 60.8           | 84.7           | 112.4          |
| 35   | 0.7            | 4.9            | 13.1           | 25.2           | 41.2           | 61.2           | 85.1           | 112.9          |
| 36   | 0.7            | 5.0            | 13.3           | 25.4           | 41.5           | 61.6           | 85.5           | 113.4          |
| 37   | 0.7            | 5.1            | 13.4           | 25.7           | 41.8           | 61.9           | 86.0           | 113.9          |
| 38   | 0.8            | 5.2            | 13.6           | 25.9           | 42.1           | 62.3           | 86.4           | 114.4          |
| 39   | 0.8            | 5.3            | 13.8           | 26.2           | 42.5           | 62.7           | 86.8           | 114.9          |
| 40   | 0.9            | 5.4            | 14.0           | 26.4           | 42.8           | 63.0           | 87.3           | 115.4          |
| 41   | 0.9            | 5.6            | 14.1           | 26.6           | 43.1           | 63.4           | 87.7           | 115.9          |
| 42   | 1.0            | 5.7            | 14.3           | 26.9           | 43.4           | 63.8           | 88.1           | 116.4          |
| 43   | 1.0            | 5.8            | 14.5           | 27.1           | 43.7           | 64.2           | 88.6           | 116.9          |
| 44   | 1.1            | 5.9            | 14.7           | 27.4           | 44.0           | 64.5           | 89.0           | 117.4          |
| 45   | 1.1            | 6.0            | 14.8           | 27.6           | 44.3           | 64.9           | 89.5           | 117.9          |
| 46   | 1.2            | 6.1            | 15.0           | 27.9           | 44.6           | 65.3           | 89.9           | 118.4          |
| 47   | 1.2            | 6.2            | 15.2           | 28.1           | 44.9           | 65.7           | 90.3           | 118.9          |
| 48   | 1.3            | 6.4            | 15.4           | 28.3           | 45.2           | 66.0           | 90.8           | 119.5          |
| 49   | 1.3            | 6.5            | 15.6           | 28.6           | 45.5           | 66.4           | 91.2           | 120.0          |
| 50   | 1.4            | 6.6            | 15.8           | 28.8           | 45.9           | 66.8           | 91.7           | 120.5          |
| 51   | 1.4            | 6.7            | 15.9           | 29.1           | 46.2           | 67.2           | 92.1           | 121.0          |
| 52   | 1.5            | 6.8            | 16.1           | 29.4           | 46.5           | 67.6           | 92.6           | 121.5          |
| 53   | 1.5            | 7.0            | 16.3           | 29.6           | 46.8           | 68.0           | 93.0           | 122.0          |
| 54   | 1.6            | 7.1            | 16.5           | 29.9           | 47.1           | 68.3           | 93.5           | 122.5          |
| 55   | 1.6            | 7.2            | 16.7           | 30.1           | 47.5           | 68.7           | 93.9           | 123.1          |
| 56   | 1.7            | 7.3            | 16.9           | 30.4           | 47.8           | 69.1           | 94.4           | 123.6          |
| 57   | 1.8            | 7.5            | 17.1           | 30.6           | 48.1           | 69.5           | 94.8           | 124.1          |
| 58   | 1.8            | 7.6            | 17.3           | 30.9           | 48.4           | 69.9           | 95.2           | 124.6          |
| 59   | 1.9            | 7.7            | 17.5           | 31.1           | 48.8           | 70.3           | 95.7           | 125.1          |



*Reduction to the Meridian; values of  $k = \frac{2 \sin^2 \frac{1}{2} p}{\sin 1''}$*

| Sec. | 8 <sup>m</sup> | 9 <sup>m</sup> | 10 <sup>m</sup> | 11 <sup>m</sup> | 12 <sup>m</sup> | 13 <sup>m</sup> | 14 <sup>m</sup> |
|------|----------------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
|      | "              | "              | "               | "               | "               | "               | "               |
| 0    | 125.7          | 159.0          | 196.3           | 237.5           | 282.7           | 331.8           | 384.7           |
| 1    | 126.2          | 159.6          | 197.0           | 238.3           | 283.5           | 332.6           | 385.6           |
| 2    | 126.7          | 160.2          | 197.6           | 239.0           | 284.2           | 333.4           | 386.6           |
| 3    | 127.2          | 160.8          | 198.3           | 239.7           | 285.0           | 334.3           | 387.5           |
| 4    | 127.8          | 161.4          | 198.9           | 240.4           | 285.8           | 335.2           | 388.4           |
| 5    | 128.3          | 162.0          | 199.6           | 241.2           | 286.6           | 336.0           | 389.3           |
| 6    | 128.8          | 162.6          | 200.3           | 241.9           | 287.4           | 336.9           | 390.2           |
| 7    | 129.3          | 163.2          | 200.9           | 242.6           | 288.2           | 337.7           | 391.1           |
| 8    | 129.9          | 163.8          | 201.6           | 243.3           | 289.0           | 338.6           | 392.1           |
| 9    | 130.4          | 164.4          | 202.2           | 244.1           | 289.8           | 339.4           | 393.0           |
| 10   | 131.0          | 165.0          | 202.9           | 244.8           | 290.6           | 340.3           | 393.9           |
| 11   | 131.5          | 165.6          | 203.6           | 245.5           | 291.4           | 341.2           | 394.8           |
| 12   | 132.0          | 166.2          | 204.2           | 246.3           | 292.2           | 342.0           | 395.8           |
| 13   | 132.6          | 166.8          | 204.9           | 247.0           | 293.0           | 342.9           | 396.7           |
| 14   | 133.1          | 167.4          | 205.6           | 247.7           | 293.8           | 343.7           | 397.6           |
| 15   | 133.6          | 168.0          | 206.3           | 248.5           | 294.6           | 344.6           | 398.6           |
| 16   | 134.2          | 168.6          | 206.9           | 249.2           | 295.4           | 345.5           | 399.5           |
| 17   | 134.7          | 169.2          | 207.6           | 249.9           | 296.2           | 346.4           | 400.5           |
| 18   | 135.3          | 169.8          | 208.3           | 250.7           | 297.0           | 347.2           | 401.4           |
| 19   | 135.8          | 170.4          | 208.9           | 251.4           | 297.8           | 348.1           | 402.3           |
| 20   | 136.3          | 171.0          | 209.6           | 252.2           | 298.6           | 349.0           | 403.3           |
| 21   | 136.9          | 171.6          | 210.3           | 253.0           | 299.4           | 349.8           | 404.2           |
| 22   | 137.4          | 172.2          | 211.0           | 253.6           | 300.2           | 350.7           | 405.1           |
| 23   | 138.0          | 172.9          | 211.7           | 254.4           | 301.0           | 351.6           | 406.0           |
| 24   | 138.5          | 173.5          | 212.3           | 255.1           | 301.8           | 352.5           | 407.0           |
| 25   | 139.1          | 174.1          | 213.0           | 255.9           | 302.6           | 353.3           | 408.0           |
| 26   | 139.6          | 174.7          | 213.7           | 256.6           | 303.5           | 354.2           | 408.9           |
| 27   | 140.2          | 175.3          | 214.4           | 257.4           | 304.3           | 355.1           | 409.9           |
| 28   | 140.7          | 175.9          | 215.1           | 258.1           | 305.1           | 356.0           | 410.8           |
| 29   | 141.3          | 176.6          | 215.8           | 258.9           | 305.9           | 356.9           | 411.7           |

*Reduction to the Meridian; values of  $k = \frac{2 \sin^2 \frac{1}{2} p}{\sin 1''}$*

| Sec. | 8 <sup>m</sup> | 9 <sup>m</sup> | 10 <sup>m</sup> | 11 <sup>m</sup> | 12 <sup>m</sup> | 13 <sup>m</sup> | 14 <sup>m</sup> |
|------|----------------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
|      | "              | "              | "               | "               | "               | "               | "               |
| 30   | 141.8          | 177.2          | 216.4           | 259.6           | 306.7           | 357.7           | 412.7           |
| 31   | 142.4          | 177.8          | 217.1           | 260.4           | 307.5           | 358.6           | 413.6           |
| 32   | 143.0          | 178.4          | 217.8           | 261.1           | 308.4           | 359.5           | 414.6           |
| 33   | 143.5          | 179.0          | 218.5           | 261.9           | 309.2           | 360.4           | 415.5           |
| 34   | 144.1          | 179.7          | 219.2           | 262.6           | 310.0           | 361.3           | 416.5           |
| 35   | 144.6          | 180.3          | 219.9           | 263.4           | 310.8           | 362.2           | 417.5           |
| 36   | 145.2          | 180.9          | 220.6           | 264.1           | 311.6           | 363.1           | 418.4           |
| 37   | 145.8          | 181.6          | 221.3           | 264.9           | 312.5           | 364.0           | 419.4           |
| 38   | 146.3          | 182.2          | 222.0           | 265.7           | 313.3           | 364.8           | 420.3           |
| 39   | 146.9          | 182.8          | 222.7           | 266.4           | 314.1           | 365.7           | 421.3           |
| 40   | 147.5          | 183.5          | 223.4           | 267.2           | 315.0           | 366.6           | 422.2           |
| 41   | 148.0          | 184.1          | 224.1           | 267.9           | 315.8           | 367.5           | 423.2           |
| 42   | 148.6          | 184.7          | 224.8           | 268.7           | 316.6           | 368.4           | 424.2           |
| 43   | 149.2          | 185.4          | 225.5           | 269.5           | 317.4           | 369.3           | 425.1           |
| 44   | 149.7          | 186.0          | 226.2           | 270.3           | 318.3           | 370.2           | 426.1           |
| 45   | 150.3          | 186.6          | 226.9           | 271.0           | 319.1           | 371.1           | 427.0           |
| 46   | 150.9          | 187.3          | 227.6           | 271.8           | 319.9           | 372.0           | 428.0           |
| 47   | 151.5          | 187.9          | 228.3           | 272.6           | 320.8           | 372.9           | 429.0           |
| 48   | 152.0          | 188.5          | 229.0           | 273.3           | 321.6           | 373.8           | 429.9           |
| 49   | 152.6          | 189.2          | 229.7           | 274.1           | 322.4           | 374.7           | 430.9           |
| 50   | 153.2          | 189.8          | 230.4           | 274.9           | 323.3           | 375.6           | 431.9           |
| 51   | 153.8          | 190.5          | 231.1           | 275.6           | 324.1           | 376.5           | 432.8           |
| 52   | 154.4          | 191.1          | 231.8           | 276.4           | 325.0           | 377.4           | 433.8           |
| 53   | 154.9          | 191.8          | 232.5           | 277.2           | 325.8           | 378.3           | 434.8           |
| 54   | 155.5          | 192.4          | 233.2           | 278.0           | 326.7           | 379.3           | 435.8           |
| 55   | 156.1          | 193.1          | 234.0           | 278.8           | 327.5           | 380.2           | 436.7           |
| 56   | 156.7          | 193.7          | 234.7           | 279.5           | 328.4           | 381.1           | 437.7           |
| 57   | 157.3          | 194.4          | 235.4           | 280.3           | 329.2           | 382.0           | 438.7           |
| 58   | 157.8          | 195.0          | 236.1           | 281.1           | 330.0           | 382.9           | 439.7           |
| 59   | 158.4          | 195.7          | 236.8           | 281.9           | 330.9           | 383.8           | 440.6           |

*Reduction to the Meridian; values of  $k = \frac{2 \sin^2 \frac{1}{2} p}{\sin 1''}$*

| Sec. | 15 <sup>m</sup> | 16 <sup>m</sup> | 17 <sup>m</sup> | 18 <sup>m</sup> | 19 <sup>m</sup> | 20 <sup>m</sup> | 21 <sup>m</sup> |
|------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
|      | "               | "               | "               | "               | "               | "               | "               |
| 0    | 441.6           | 502.5           | 567.2           | 635.9           | 708.4           | 784.9           | 865.3           |
| 1    | 442.6           | 503.5           | 568.3           | 637.0           | 709.7           | 786.2           | 866.6           |
| 2    | 443.6           | 504.6           | 569.4           | 638.2           | 710.9           | 787.5           | 868.0           |
| 3    | 444.6           | 505.6           | 570.5           | 639.4           | 712.1           | 788.8           | 869.4           |
| 4    | 445.6           | 506.7           | 571.6           | 640.6           | 713.4           | 790.1           | 870.8           |
| 5    | 446.5           | 507.7           | 572.8           | 641.7           | 714.6           | 791.4           | 872.1           |
| 6    | 447.5           | 508.8           | 573.9           | 642.9           | 715.9           | 792.7           | 873.5           |
| 7    | 448.5           | 509.8           | 575.0           | 644.1           | 717.1           | 794.0           | 874.9           |
| 8    | 449.5           | 510.9           | 576.1           | 645.3           | 718.4           | 795.4           | 876.3           |
| 9    | 450.5           | 511.9           | 577.2           | 646.5           | 719.6           | 796.7           | 877.6           |
| 10   | 451.5           | 513.0           | 578.4           | 647.7           | 720.9           | 798.0           | 879.0           |
| 11   | 452.5           | 514.0           | 579.5           | 648.9           | 722.1           | 799.3           | 880.4           |
| 12   | 453.5           | 515.1           | 580.6           | 650.0           | 723.4           | 800.7           | 881.8           |
| 13   | 454.5           | 516.1           | 581.7           | 651.2           | 724.6           | 802.0           | 883.2           |
| 14   | 455.5           | 517.2           | 582.9           | 652.4           | 725.9           | 803.3           | 884.6           |
| 15   | 456.5           | 518.3           | 584.0           | 653.6           | 727.2           | 804.6           | 886.0           |
| 16   | 457.5           | 519.3           | 585.1           | 654.8           | 728.4           | 806.0           | 887.4           |
| 17   | 458.5           | 520.4           | 586.2           | 656.0           | 729.7           | 807.3           | 888.8           |
| 18   | 459.5           | 521.5           | 587.4           | 657.2           | 730.9           | 808.6           | 890.2           |
| 19   | 460.5           | 522.5           | 588.5           | 658.4           | 732.2           | 809.9           | 891.6           |
| 20   | 461.5           | 523.6           | 589.6           | 659.6           | 733.5           | 811.3           | 893.0           |
| 21   | 462.5           | 524.6           | 590.8           | 660.8           | 734.7           | 812.6           | 894.4           |
| 22   | 463.5           | 525.7           | 591.9           | 662.0           | 736.0           | 813.9           | 895.8           |
| 23   | 464.5           | 526.8           | 593.0           | 663.2           | 737.3           | 815.2           | 897.2           |
| 24   | 465.5           | 527.9           | 594.2           | 664.4           | 738.5           | 816.6           | 898.6           |
| 25   | 466.5           | 528.9           | 595.3           | 665.6           | 739.8           | 817.9           | 900.0           |
| 26   | 467.5           | 530.0           | 596.5           | 666.8           | 741.1           | 819.2           | 901.4           |
| 27   | 468.5           | 531.1           | 597.6           | 668.0           | 742.3           | 820.5           | 902.8           |
| 28   | 469.5           | 532.2           | 598.7           | 669.2           | 743.6           | 821.9           | 904.2           |
| 29   | 470.5           | 533.2           | 599.9           | 670.4           | 744.9           | 823.2           | 905.6           |

*Reduction to the Meridian; values of  $k = \frac{2 \sin^2 \frac{1}{2} p}{\sin 1''}$*

| Sec. | 15 <sup>m</sup> | 16 <sup>m</sup> | 17 <sup>m</sup> | 18 <sup>m</sup> | 19 <sup>m</sup> | 20 <sup>m</sup> | 21 <sup>m</sup> |
|------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
|      | "               | "               | "               | "               | "               | "               | "               |
| 30   | 471.5           | 534.3           | 601.0           | 671.6           | 746.2           | 824.6           | 907.0           |
| 31   | 472.6           | 535.4           | 602.2           | 672.8           | 747.4           | 825.9           | 908.4           |
| 32   | 473.6           | 536.5           | 603.3           | 674.1           | 748.7           | 827.3           | 909.8           |
| 33   | 474.6           | 537.6           | 604.5           | 675.3           | 750.0           | 828.6           | 911.2           |
| 34   | 475.6           | 538.7           | 605.6           | 676.5           | 751.3           | 829.9           | 912.6           |
| 35   | 476.6           | 539.7           | 606.8           | 677.7           | 752.6           | 831.2           | 914.0           |
| 36   | 477.6           | 540.8           | 607.9           | 678.9           | 753.8           | 832.6           | 915.5           |
| 37   | 478.7           | 541.9           | 609.1           | 680.1           | 755.1           | 833.9           | 916.9           |
| 38   | 479.7           | 543.0           | 610.2           | 681.3           | 756.4           | 835.3           | 918.3           |
| 39   | 480.7           | 544.1           | 611.4           | 682.6           | 757.7           | 836.6           | 919.7           |
| 40   | 481.7           | 545.2           | 612.5           | 683.8           | 759.0           | 838.0           | 921.1           |
| 41   | 482.8           | 546.3           | 613.7           | 685.0           | 760.2           | 839.3           | 922.5           |
| 42   | 483.8           | 547.4           | 614.8           | 686.2           | 761.5           | 840.7           | 923.9           |
| 43   | 484.8           | 548.4           | 616.0           | 687.4           | 762.8           | 842.0           | 925.3           |
| 44   | 485.8           | 549.5           | 617.2           | 688.7           | 764.1           | 843.4           | 926.8           |
| 45   | 486.9           | 550.6           | 618.3           | 689.9           | 765.4           | 844.7           | 928.2           |
| 46   | 487.9           | 551.7           | 619.5           | 691.1           | 766.7           | 846.1           | 929.6           |
| 47   | 488.9           | 552.8           | 620.6           | 692.4           | 768.0           | 847.5           | 931.0           |
| 48   | 490.0           | 553.9           | 621.8           | 693.6           | 769.3           | 848.9           | 932.4           |
| 49   | 491.0           | 555.0           | 623.0           | 694.8           | 770.6           | 850.2           | 933.8           |
| 50   | 492.0           | 556.1           | 624.1           | 696.0           | 771.9           | 851.6           | 935.2           |
| 51   | 493.1           | 557.2           | 625.3           | 697.3           | 773.1           | 852.9           | 936.6           |
| 52   | 494.1           | 558.3           | 626.5           | 698.5           | 774.5           | 854.3           | 938.1           |
| 53   | 495.2           | 559.4           | 627.6           | 699.7           | 775.8           | 855.7           | 939.5           |
| 54   | 496.2           | 560.5           | 628.8           | 701.0           | 777.1           | 857.1           | 940.9           |
| 55   | 497.2           | 561.6           | 630.0           | 702.2           | 778.4           | 858.4           | 942.3           |
| 56   | 498.3           | 562.7           | 631.2           | 703.5           | 779.7           | 859.8           | 943.8           |
| 57   | 499.3           | 563.9           | 632.3           | 704.7           | 781.0           | 861.1           | 945.2           |
| 58   | 500.3           | 565.0           | 633.5           | 705.9           | 782.3           | 862.5           | 946.6           |
| 59   | 501.4           | 566.1           | 634.7           | 707.1           | 783.6           | 863.9           | 948.1           |

*Reduction to the Meridian; values of  $k = \frac{2 \sin^2 \frac{1}{2} p}{\sin 1''}$*

| Sec. | 22 <sup>m</sup> | 23 <sup>m</sup> | 24 <sup>m</sup> | Sec. | 22 <sup>m</sup> | 23 <sup>m</sup> | 24 <sup>m</sup> |
|------|-----------------|-----------------|-----------------|------|-----------------|-----------------|-----------------|
|      | "               | "               | "               |      | "               | "               | "               |
| 0    | 949.6           | 1037.8          | 1129.9          | 30   | 993.2           | 1083.3          | 1177.5          |
| 1    | 951.0           | 1039.3          | 1131.4          | 31   | 994.7           | 1084.8          | 1179.1          |
| 2    | 952.4           | 1040.8          | 1133.0          | 32   | 996.2           | 1086.4          | 1180.7          |
| 3    | 953.8           | 1042.3          | 1134.6          | 33   | 997.6           | 1087.9          | 1182.3          |
| 4    | 955.3           | 1043.8          | 1136.2          | 34   | 999.1           | 1089.5          | 1183.9          |
| 5    | 956.7           | 1045.3          | 1137.8          | 35   | 1000.6          | 1091.0          | 1185.5          |
| 6    | 958.2           | 1046.8          | 1139.3          | 36   | 1002.1          | 1092.6          | 1187.1          |
| 7    | 959.6           | 1048.3          | 1140.9          | 37   | 1003.5          | 1094.1          | 1188.7          |
| 8    | 961.1           | 1049.8          | 1142.5          | 38   | 1005.0          | 1095.7          | 1190.3          |
| 9    | 962.5           | 1051.3          | 1144.0          | 39   | 1006.5          | 1097.2          | 1191.9          |
| 10   | 963.9           | 1052.8          | 1145.6          | 40   | 1008.0          | 1098.8          | 1193.5          |
| 11   | 965.4           | 1054.3          | 1147.2          | 41   | 1009.4          | 1100.3          | 1195.1          |
| 12   | 966.9           | 1055.9          | 1148.8          | 42   | 1010.9          | 1101.9          | 1196.7          |
| 13   | 968.3           | 1057.4          | 1150.4          | 43   | 1012.4          | 1103.4          | 1198.3          |
| 14   | 969.8           | 1058.9          | 1152.0          | 44   | 1013.9          | 1105.0          | 1199.9          |
| 15   | 971.2           | 1060.4          | 1153.6          | 45   | 1015.4          | 1106.5          | 1201.5          |
| 16   | 972.7           | 1062.0          | 1155.2          | 46   | 1016.9          | 1108.1          | 1203.1          |
| 17   | 974.1           | 1063.5          | 1156.8          | 47   | 1018.4          | 1109.6          | 1204.7          |
| 18   | 975.5           | 1065.0          | 1158.3          | 48   | 1019.9          | 1111.2          | 1206.4          |
| 19   | 977.0           | 1066.5          | 1159.9          | 49   | 1021.4          | 1112.7          | 1208.0          |
| 20   | 978.5           | 1068.1          | 1161.5          | 50   | 1022.8          | 1114.3          | 1209.6          |
| 21   | 979.9           | 1069.6          | 1163.1          | 51   | 1024.3          | 1115.8          | 1211.2          |
| 22   | 981.4           | 1071.1          | 1164.7          | 52   | 1025.8          | 1117.4          | 1212.9          |
| 23   | 982.9           | 1072.6          | 1166.3          | 53   | 1027.3          | 1118.9          | 1214.5          |
| 24   | 984.4           | 1074.2          | 1167.9          | 54   | 1028.8          | 1120.5          | 1216.1          |
| 25   | 985.8           | 1075.7          | 1169.5          | 55   | 1030.3          | 1122.0          | 1217.7          |
| 26   | 987.3           | 1077.2          | 1171.1          | 56   | 1031.8          | 1123.6          | 1219.4          |
| 27   | 988.8           | 1078.7          | 1172.7          | 57   | 1033.3          | 1125.1          | 1221.0          |
| 28   | 990.3           | 1080.3          | 1174.3          | 58   | 1034.8          | 1126.7          | 1222.6          |
| 29   | 991.8           | 1081.8          | 1175.9          | 59   | 1036.3          | 1128.3          | 1224.2          |

*Second part of the Reduction to the Meridian;*

$$\text{values of } m = \frac{2 \sin^4 \frac{1}{2} p}{\sin 1''}$$

| Minutes. | 0°    | 10°   | 20°   | 30°   | 40°   | 50°   |
|----------|-------|-------|-------|-------|-------|-------|
|          | "     | "     | "     | "     | "     | "     |
| 5        | 0.01  | 0.01  | 0.01  | 0.01  | 0.01  | 0.01  |
| 6        | 0.01  | 0.01  | 0.01  | 0.02  | 0.02  | 0.02  |
| 7        | 0.02  | 0.02  | 0.03  | 0.03  | 0.03  | 0.04  |
| 8        | 0.04  | 0.04  | 0.05  | 0.05  | 0.05  | 0.06  |
| 9        | 0.06  | 0.06  | 0.08  | 0.08  | 0.08  | 0.09  |
| 10       | 0.09  | 0.10  | 0.11  | 0.11  | 0.12  | 0.13  |
| 11       | 0.14  | 0.15  | 0.15  | 0.16  | 0.17  | 0.18  |
| 12       | 0.19  | 0.20  | 0.22  | 0.23  | 0.24  | 0.25  |
| 13       | 0.27  | 0.28  | 0.30  | 0.31  | 0.33  | 0.34  |
| 14       | 0.36  | 0.38  | 0.39  | 0.41  | 0.43  | 0.45  |
| 15       | 0.47  | 0.49  | 0.52  | 0.54  | 0.56  | 0.59  |
| 16       | 0.61  | 0.64  | 0.67  | 0.69  | 0.72  | 0.75  |
| 17       | 0.78  | 0.81  | 0.84  | 0.88  | 0.91  | 0.95  |
| 18       | 0.98  | 1.02  | 1.06  | 1.09  | 1.13  | 1.18  |
| 19       | 1.22  | 1.26  | 1.30  | 1.35  | 1.40  | 1.44  |
| 20       | 1.49  | 1.54  | 1.60  | 1.65  | 1.70  | 1.76  |
| 21       | 1.82  | 1.87  | 1.93  | 1.99  | 2.06  | 2.12  |
| 22       | 2.19  | 2.25  | 2.32  | 2.39  | 2.46  | 2.54  |
| 23       | 2.61  | 2.69  | 2.77  | 2.85  | 2.93  | 3.01  |
| 24       | 3.10  | 3.18  | 3.27  | 3.36  | 3.45  | 3.55  |
| 25       | 3.64  | 3.74  | 3.84  | 3.94  | 4.05  | 4.15  |
| 26       | 4.26  | 4.37  | 4.48  | 4.60  | 4.72  | 4.83  |
| 27       | 4.96  | 5.08  | 5.20  | 5.33  | 5.46  | 5.60  |
| 28       | 5.73  | 5.87  | 6.01  | 6.15  | 6.30  | 6.44  |
| 29       | 6.59  | 6.75  | 6.90  | 7.06  | 7.22  | 7.38  |
| 30       | 7.55  | 7.72  | 7.89  | 8.06  | 8.24  | 8.42  |
| 31       | 8.61  | 8.79  | 8.98  | 9.17  | 9.37  | 9.57  |
| 32       | 9.77  | 9.97  | 10.18 | 10.39 | 10.61 | 10.82 |
| 33       | 11.04 | 11.27 | 11.50 | 11.73 | 11.96 | 12.20 |
| 34       | 12.44 | 12.69 | 12.94 | 13.19 | 13.45 | 13.71 |
| 35       | 13.97 | 14.24 | 14.51 | 14.78 | 15.06 | 15.35 |

## FORM FOR RECORD

SURVEY OF

DETERMINATION OF THE LATITUDE,  
*North and South*DATE AND STATION.—1843, October 13—*Mouth of the Big Black river,*NAME OF STAR,  $\gamma$  *Pegasi, South of the Zenith.*INSTRUMENTS. { Sextant No. 2197, by *Troughton & Simms*, and  
{ *Mean Solar Chronometer* No. 76, by *Charles*

| No. for reference. | Times of observation by Chronometer. | MERIDIAN DISTANCES, = $p$ . |                   | $\frac{2 \sin^2 \frac{1}{2} p}{\sin 1''}$<br>= $k$ | $\cos l. \cos D.$<br>Co sine $a$ | Reduction to the meridian (in arc) = $x$ . |
|--------------------|--------------------------------------|-----------------------------|-------------------|----------------------------------------------------|----------------------------------|--------------------------------------------|
|                    |                                      | In mean Solar time.         | In Sidereal time. |                                                    |                                  |                                            |
|                    | $h \quad m \quad s$                  | $m \quad s$                 | $m \quad s$       | "                                                  | Constant multiple 1.227          | ' "                                        |
| 1                  | 10 18 40.4                           | 9 44.2                      | 9 45.8            | 187.3                                              |                                  | 3 49.8                                     |
| 2                  | 19 44.4                              | 8 40.2                      | 8 41.6            | 148.3                                              |                                  | 2 51.9                                     |
| 3                  | 20 48                                | 7 36.5                      | 7 37.7            | 114.2                                              |                                  | 2 27.3                                     |
| 4                  | 21 46.4                              | 6 38.2                      | 6 39.3            | 86.9                                               |                                  | 1 47.6                                     |
| 5                  | 22 44.4                              | 5 40.2                      | 5 41.1            | 63.4                                               |                                  | 1 17.8                                     |
| 6                  | 23 54                                | 4 30.5                      | 4 31.2            | 40.1                                               |                                  | 0 49.2                                     |
| 7                  | 25 12                                | 3 12.6                      | 3 13.1            | 20.3                                               |                                  | 0 24.9                                     |
| 8                  | 26 46                                | 1 38.6                      | 1 38.8            | 5.2                                                |                                  | 0 06.3                                     |
| 9                  | 28 16.4                              | 0 08.2                      | 0 08.2            | 0.0                                                |                                  | 0 00.0                                     |
| 10                 | 29 42                                | 1 17.4                      | 1 17.6            | 3.2                                                |                                  | 0 03.9                                     |
| 11                 | 31 42                                | 3 17.4                      | 3 17.9            | 21.4                                               |                                  | 0 26.2                                     |
| 12                 | 32 54.4                              | 4 29.8                      | 4 30.5            | 40.0                                               |                                  | 0 49                                       |
| 13                 | 34 18                                | 5 53.4                      | 5 54.3            | 68.5                                               |                                  | 1 24                                       |
| 14                 | 36 14.2                              | 7 49.6                      | 7 50.9            | 123.5                                              |                                  | 2 31.5                                     |
| 15                 | 38 32.2                              | 10 07.6                     | 10 09.2           | 202.3                                              |                                  | 4 08.2                                     |
| 16                 | 40 06                                | 11 41.4                     | 11 43.3           | 269.9                                              |                                  | 5 31.1                                     |

Observer, *Major J. D. Graham.*Computer, *do. do.*

## AND COMPUTATION.

*from observed double circum-meridian altitudes of Stars,  
of the Zenith.*

*a tributary to the river St. John, Maine.*

artificial horizon of Mercury.

Young.

| Obser'd double<br>circum - meri-<br>dian altitudes<br>of Star. | True circum-meridi-<br>an altitude of Star,<br>as corrected for re-<br>fraction and errors<br>of instrument,<br>= $a$ . | True meridian al-<br>titudes deduced,<br>= $(a + x) = A$ | Latitude,<br>deduced from<br>each observa-<br>tion = $L =$<br>$(90^\circ + D - A)$ |
|----------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------|------------------------------------------------------------------------------------|
| O ' "                                                          | O ' "                                                                                                                   | O ' "                                                    | O ' "                                                                              |
| 114 34 15                                                      | 57 18 38.5                                                                                                              | 57 22 28.3                                               | 46 56 42.55                                                                        |
| 36 15                                                          | 57 19 38.5                                                                                                              | 57 22 30.4                                               | 56 40.45                                                                           |
| 37 10                                                          | 57 20 06                                                                                                                | 57 22 33.3                                               | 56 37.55                                                                           |
| 38 10                                                          | 57 20 36                                                                                                                | 57 22 23.6                                               | 56 47.25                                                                           |
| 39 30                                                          | 57 21 16                                                                                                                | 57 22 33.8                                               | 56 37.05                                                                           |
| 40 30                                                          | 57 21 46                                                                                                                | 57 22 35.2                                               | 56 35.65                                                                           |
| 41 05                                                          | 57 22 03.5                                                                                                              | 57 22 28.4                                               | 56 42.45                                                                           |
| 41 50                                                          | 57 22 26                                                                                                                | 57 22 32.3                                               | 56 34.55                                                                           |
| 41 50                                                          | 57 22 26                                                                                                                | 57 22 26                                                 | 56 40.85                                                                           |
| 41 50                                                          | 57 22 26                                                                                                                | 57 22 29.9                                               | 56 36.95                                                                           |
| 41 00                                                          | 57 22 01                                                                                                                | 57 22 27.2                                               | 56 39.65                                                                           |
| 39 45                                                          | 57 21 23.5                                                                                                              | 57 22 12.5                                               | 56 58.35                                                                           |
| 38 40                                                          | 57 20 51                                                                                                                | 57 22 15                                                 | 56 55.85                                                                           |
| 36 30                                                          | 57 19 46                                                                                                                | 57 22 17.5                                               | 56 53.55                                                                           |
| 33 20                                                          | 57 18 11                                                                                                                | 57 22 19.2                                               | 56 51.85                                                                           |
| 30 50                                                          | 57 16 56                                                                                                                | 57 22 27.1                                               | 46 56 39.75                                                                        |

LATITUDE—Deduced from a mean of 16 altitudes of

Star  $\gamma$  Pegasi . . . . . 46° 56' 43".4

Deduced from a mean of 10 altitudes of

Star  $\gamma$  Cephei, observed this night with

same Sextant . . . . . 46 57 10.7

Mean; or Latitude adopted . . . . . 46° 56' 57"



|                                                                        |                                                   |             |
|------------------------------------------------------------------------|---------------------------------------------------|-------------|
| D = apparent declination of Star $14^{\circ} 19' 10''.85$ N.           | Log cos                                           | 9.98629     |
| l = approximate Lat. of place $46^{\circ} 57'$                         | Log cos                                           | 9.83418     |
|                                                                        | Sum                                               | 19.82048    |
| a = approximate merid. alt. of Star $57^{\circ} 22' 10''$              | Log cos                                           | 9.73176     |
| $\frac{\cos l \cos D}{\cos a}$ = constant multiple = 1.227             | Log                                               | 0.08872     |
| Refraction (Ther. $28^{\circ}$ , Bar. 29.14 in.) for mean obs'd alts.  |                                                   | — 39"       |
| Index error of Sextant                                                 |                                                   | + 2' 40"    |
| *Error of excentricity, &c., of Sextant                                |                                                   | + 1' 40"    |
| Apparent AR. of the Star $\gamma$ Pegasi                               | $\begin{smallmatrix} h & m & s \end{smallmatrix}$ | 0 05 14.09  |
| Sidereal time at mean noon at this station                             |                                                   | 13 26 20.83 |
| Sidereal interval from mean noon, of Star's culmination                |                                                   | 10 38 53.16 |
| Retardation of mean on Sidereal time                                   |                                                   | — 1 44.96   |
| Mean time of culmination of Star $\gamma$ Pegasi                       |                                                   | 10 37 08.2  |
| Chronometer (C. Y. 76) <i>slow</i> of mean time at time of observation |                                                   | — 08 43.6   |
| Time by Chronometer of culmination of Star $\gamma$ Pegasi             |                                                   | 10 28 24.6  |

On this night, Oct. 13, 1843, Major Graham obtained for the Latitude of this station, from 75 observations on 5 stars South of the zenith, combined with 21 observations on  $\gamma$  Cephei and Polaris, to the North . . .  $46^{\circ} 56' 56''.3$

On the night of Oct. 24, by 43 observations on 4 southern stars, combined with 2 observations on  $\gamma$  Cephei, the Latitude deduced was . . .  $46 56 57.2$

On Sept. 17, 1844, 66 observations on N. and S. stars gave for the Latitude of this station . . .  $46 56 60.4$

\*NOTE.—The error of excentricity is approximately ascertained by comparing Latitudes, well determined, by observations on N. and S. stars, with that which will result from N. or S. stars individually of various meridional altitudes. It varies with the altitudes observed. That is to say, it is different for different parts of the limb of the instrument.

VII. To determine the Latitude by an altitude of a star near the pole, at any hour.

$L = A - (\Delta \cos p) + \alpha (\Delta \sin p)^2 \tan A - \beta (\Delta \sin p)^2 (\Delta \cos p)$   
 where  $A$  = the observed altitude, corrected for refraction, etc.

$\Delta$  = the polar distance of the star, in seconds of arc.

$\alpha = \frac{1}{2} \sin 1''$ ,  $\log \alpha = 4.3845449$ ,

$\beta = \frac{1}{3} \sin^2 1''$ ,  $\log \beta = 8.89403$ ,

$p$  = the hour angle of the star.

$\pm p$  = sidereal time  $- AR^*$  = solar time  $+ AR^\odot - AR^*$   
 $p$  is *plus* when the star is west, and *minus* when it is east of the meridian.

The sign of  $\cos p$  should also be attended to, for when  $p$  is greater than  $6^{\text{hrs}}$  or  $90^\circ$ , the cosine is negative, and the second and fourth terms change the sign *minus* to *plus*.

The fourth term may be generally omitted; its greatest value being only  $0''.55$ .

This formula is only applicable to stars within a very few degrees of the pole.

For other circumpolar stars,

$$\tan x = \tan \Delta \cos p$$

$$\sin y = \frac{\cos x \sin A}{\cos \Delta}$$

$$L = y \mp x$$

In which the upper sign is used when the star is above the pole, the under when below the pole.

## FORM FOR

## SURVEY OF

## DETERMINATION OF THE

DATE AND STATION.—1843, September 6—Woodstock, New Brunswick,

NAME OF STAR.—*Polaris* ( $\alpha$  *Ursæ Minoris*), observed on, between four andINSTRUMENTS. { Sextant No. 2197, by Troughton & Simms, and arti-  
{ Mean Solar Chronometer No. 2440, by Parkinson &

| No. for ref. | Times of observation by<br>Mean Solar<br>Chronometer<br>No. 2440. | True Sidereal<br>times of ob-<br>servation. | MERIDIAN DISTANCES.     |                  | $-\Delta \cos p.$<br>' |
|--------------|-------------------------------------------------------------------|---------------------------------------------|-------------------------|------------------|------------------------|
|              |                                                                   |                                             | In Sid'l time<br>= $p.$ | In arc<br>= $p.$ |                        |
|              | <i>h. m. s.</i>                                                   | <i>h. m. s.</i>                             | <i>h. m. s.</i>         | <i>o ' "</i>     | <i>' "</i>             |
| 1            | 1 33 02.5                                                         | 20 05 34.1                                  | 4 58 23.2               | 74 35 48         | —24 18.1               |
| 2            | 1 34 28                                                           | 20 06 59.8                                  | 4 56 57.5               | 74 14 22.5       | —24 54.5               |
| 3            | 1 35 42.7                                                         | 20 08 14.7                                  | 4 55 42.6               | 73 55 39         | —25 19.8               |
| 4            | 1 36 38.2                                                         | 20 09 10.4                                  | 4 54 46.9               | 73 41 43.5       | —25 41.4               |
| 5            | 1 39 07.5                                                         | 20 11 40.1                                  | 4 52 17.2               | 73 04 18         | —26 34.7               |
| 6            | 1 41 11.2                                                         | 20 13 44.1                                  | 4 50 13.2               | 72 33 22.5       | —27 27.1               |
| 7            | 1 44 28.2                                                         | 20 17 01.7                                  | 4 46 55.6               | 71 43 54         | —28 40.8               |

Observer, *Major J. D. Graham.*Computer, *Do.*

RECORD AND COMPUTATION.

LATITUDE, from observed double altitudes of *Polaris*.

(*Grover's Inn.*)

five hours before its upper meridian passage.

ificial horizon of Mercury.

*Frodsham.*

| $+ a (\Delta \sin p)^2$<br><i>tang A.</i> | $-\beta (\Delta \sin p)^2$<br><i>(Δ cos p.)</i> | Observed double<br>alts. of<br><i>Polaris</i> out<br>of the Meri-<br>dian. | True altitudes<br>of Star, as cor-<br>rected for re-<br>fraction and<br>errors of in-<br>strument,<br>= $\Delta$ . | Latitude de-<br>duced from<br>each obser-<br>vation<br>= $L$ . |
|-------------------------------------------|-------------------------------------------------|----------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------|
| ' "                                       | '                                               | ° ' "                                                                      | ° ' "                                                                                                              | ° ' "                                                          |
| + 1 11.63                                 | — 0.32                                          | 93 01.30                                                                   | 46 31 58.6                                                                                                         | 46 08 51.8                                                     |
| + 1 11.41                                 | — 0.33                                          | 93 02.45                                                                   | 46 32 36                                                                                                           | 46 08 52.6                                                     |
| + 1 11.20                                 | — 0.33                                          | 93 03.50                                                                   | 46 33 08.6                                                                                                         | 46 08 59.7                                                     |
| + 1 11.04                                 | — 0.33                                          | 93 04.40                                                                   | 46 33 33.6                                                                                                         | 46 09 02.9                                                     |
| + 1 10.63                                 | — 0.34                                          | 93 06.15                                                                   | 46 34 21                                                                                                           | 46 08 56.6                                                     |
| + 1 10.28                                 | — 0.35                                          | 93 08.20                                                                   | 46 35 23.5                                                                                                         | 46 09 06.3                                                     |
| + 1 09.68                                 | — 0.37                                          | 93 10.50                                                                   | 46 36 38.5                                                                                                         | 46 09 07                                                       |

LATITUDE—deduced from a mean of 7 altitudes of Star }  
*Polaris* . . . . . } 46° 08' 59".4

Apparent declination of Star  $89^{\circ} 28' 30''.5$ .

Apt. N. P. D. of Star  $= 1^{\circ} 31' 29''.5 = 5489''.5 = \Delta$

Refraction (Ther.  $57^{\circ}$  — Bar. 30.013 inches) . . . . .  $- 55''.4$

Index error of Sextant . . . . .  $+ 2' 50''$

Errors of excentricity &c. of Sextant . . . . .  $+ 1' 28''$

Apparent A.R. of the Star *Polaris* ( $\alpha$  *Ursæ Minoris*) . .  $\begin{smallmatrix} h. & m. & s. \\ 1 & 03 & 57.3 \end{smallmatrix}$

Sidereal time at mean noon at this station . . . . .  $11\ 00\ 27.1$

Sidereal interval from mean noon, of Star's culmination .  $14\ 03\ 30.2$

Retardation of mean on Sidereal time . . . . .  $- 2\ 18.2$

Mean time of culmination of Star *Polaris* . . . . .  $14\ 01\ 12$

Chron. No. 2440, fast of mean time at time of observation  $4\ 29\ 24.8$

Time by Chronometer of culmination of Star *Polaris* . .  $6\ 30\ 36.8$

The reduction of the mean time of observation to sidereal time, in the preceding example, might have been omitted by using table of *A.R. in arc into mean time*, pages 152, &c. Thus—(1st observation)

Mean time of observation . . . . .  $1^h\ 33^m\ 09''.5$

Mean time culmination of *Polaris* . . . . .  $6\ 30\ 36.8$

Hour angle,  $p$ , in intervals of mean time . . . . .  $4\ 57\ 34.3$

Sidereal equivalents, in arc . . . . .  $\begin{smallmatrix} 4^h & = & 60^{\circ} 09' 51''.39 \\ 57^m & = & 14\ 17\ 20.45 \\ 34^s & = & 8\ 31.40 \\ .3 & = & 4.51 \end{smallmatrix}$

$p$ , in arc . . . . .  $= 74^{\circ} 35' 47''.75$

#### FORM FOR COMPUTATION—(1st observation)

| 1st term.         |                            | 2d term.            |                  | 3d term.               |
|-------------------|----------------------------|---------------------|------------------|------------------------|
| $\log \cos p (+)$ | $= 9.4242480$              | $\sin p$            | $= 9.98411$      |                        |
| $\Delta$          | $= 3.7395327$              | $\Delta$            | $= 3.73953$      |                        |
| $\Delta \cos p$   | $= 3.1637807$              | $\Delta \sin p$     | $= 3.72364$      | $\dots = 3.16378$      |
|                   | $= 1455''.1$               |                     |                  |                        |
| 1st term          | $= -24' 18''.1$            | $(\Delta \sin p)^2$ | $= 7.44728$      | $\dots = 7.44728$      |
| A                 | $= 46^{\circ} 31' 58.6$    | $\log a$            | $= 4.38454$      | $\log \beta = 8.89403$ |
|                   |                            | $\tan g A$          | $= 0.02325$      |                        |
|                   |                            |                     |                  | $9.50509$              |
| 2d term           | $= 46\ 07\ 40.5$           |                     | $1.85507$        | 3d t'm $= -0''.32$     |
|                   | $= + 1\ 11.63$             |                     | $= 71''.63$      |                        |
|                   |                            | 2d term             | $= + 1' 11''.63$ |                        |
|                   | $46\ 08\ 52.13$            |                     |                  |                        |
| 3d term           | $= - 0.32$                 |                     |                  |                        |
| Latitude          | $= 46^{\circ} 08' 51''.81$ |                     |                  |                        |

### VIII. *Determination of the Latitude by transits over the prime vertical.*

Suppose a Transit instrument so placed, that the transit axis is on the meridian, or very nearly so, and that the axis is horizontal, and the collimation nothing :

1. Call the time  $T$ , at which a star, whose declination is  $D$ , passes the middle wire of the instrument on the eastern side of the meridian, the clock correction to reduce the observed time to the true  $E$ , and the right ascension of the star  $AR$ ; and let  $T'$  and  $E'$  denote the corresponding quantities for the western transit. Then the two-hour angles, in sidereal time, will be, the eastern negative,

$$t = T + E - AR, \quad t' = T' + E' - AR.$$

Let the unknown Latitude of the place be  $L$ , and the Azimuth of the line of collimation,  $a$ . The spherical triangle, formed by great circles connecting the Zenith, the Pole, and the place of the Star, gives the following relations :

$$\begin{aligned} \cot a &= \frac{\cos t \cos D \sin L - \sin D \cos L}{\cos D \sin t} \\ &= \frac{\cos t' \cos D \sin L - \sin D \cos L}{\cos D \sin t'} \end{aligned}$$

Whence,

$$\tan L = \tan D \frac{\cos \frac{1}{2}(t' + t)}{\cos \frac{1}{2}(t' - t)}$$

If the instrument is very nearly on the prime vertical,  $\cos \frac{1}{2}(t + t) = \cos 0^\circ = 1$ , and

$$\tan L = \tan D \sec. \frac{1}{2}(t' - t)$$

for the passage over the middle wire of the instrument.

2. Call the time of passage of the Star, from a side wire to the middle wire,  $\tau$ .

Let the distance, in arc, of one of the lateral wires from the middle wire, measured on a great circle, be  $15 f$ ;  $f$  being the equatorial interval of the wire, in time.

Then, to reduce the transit over a side wire, to the centre wire,

$$\tau = \frac{f}{\sin(L + D) \cdot \sin(L - D) \pm \psi f} \frac{1}{2}$$

The upper sign of the term  $\pm \psi f$ , is to be used for wires crossed by the Star earlier than the middle wire in the eastern transit, and later in the western transit, and the lower sign in the opposite cases. An approximate latitude may be used for  $L$ .

3. Should the optical axis not coincide with the middle wire, substitute  $f \pm c$ , for  $f$  in the above, according as the error of collimation  $c$ , lies on the same or opposite sides of  $f$ .

4. The preceding formula gives the latitude on the supposition that the axis of the instrument is parallel to the horizon. If the instrument is on the prime vertical, but the north end of the axis is, for instance,  $n$  seconds too high, the axis is parallel to the horizon of a place whose latitude is  $n$  seconds less than where the instrument is placed, and the true latitude is, therefore,

$$L + n$$

5. But should the instrument not be on the prime vertical, the true latitude becomes

$$L + n \sin a$$

$a$  being the Azimuth of the centre wire of the telescope, supposed in collimation.

This may be found from the time elapsed between the E. and W. transits of the same star, thus :

$$\cot u = \tan \frac{1}{2} (t' - t) \sin D .$$

$$\sin a = \cos D \frac{\sin u}{\cos L} .$$

$a$  is taken between  $0^\circ$  and  $90^\circ$  when the north end of the transit axis is between the north and west, and between  $90^\circ$  and  $180^\circ$  when the same end is between the north and east.

If  $n$  is called *plus* when the north end of the axis is too high, and *vice versa*, the signs of the corrections are indicated by those of the quantities resulting from the formula.

When  $a$  is nearly  $90^\circ$ , the correction is exceedingly small ; so that, when the instrument is placed nearly east and west, we may proceed in all the computations as if it were exactly so.

6. The instrument should be set up in the firmest manner. A change of Azimuth between the east and west transits of a Star will affect the result much less than an equal change of level.

It is better, in order to obtain a close result in the shortest time, to observe several Stars on the same evening, and between the first and last observations to determine with the level the inclination of the axis several times, and then to interpolate for transits between the times of observation of the level. It is of course understood that the changes of inclination must be small, which will be the case if the instrument is properly placed.



7. In order to point the telescope rightly, the hour angles and zenith distances of the Stars to be observed must be computed for the time of transit.

When the telescope is on the prime vertical, calling  $p$  the hour angle, and  $z$ , the zenith distance of the Star, then

$$\cos p = \tan g D \cot L$$

$$\cos z = \frac{\sin D}{\sin L}$$

An allowance must be made for the time of crossing the first wire, and for change of zenith distance from the first to the middle wire.

8. To correct, for errors of Collimation, irregularity in the pivots, etc., the instrument may be reversed between the transits over each vertical; i. e., the wires on one side of the centre wire are observed, the instrument reversed in its Y's, and the transit over the same wires continued, but in an inverse order. So that, in each vertical the same wire is at one time as far north as it is at another south of the optical axis.

Then let  $L$  = the latitude sought,

$D$  = the apparent declination of the Star,

$t$  = the hour angle, illuminated axis *north*,

=  $\frac{1}{2}$  diff. of sidereal time of transit over the same wire, for same position of axis.

$t$  = hour angle, illuminated axis *south*,

$$\tan g L = \frac{\tan g D}{\cos \frac{1}{2} (t' + t) \cdot \cos \frac{1}{2} (t' - t)}$$

IX. To determine the Latitude of a place, by observing the difference of the meridional zenith distances of two Stars on opposite sides of the zenith, with the zenith and equal altitude telescope.

Compute an approximate latitude by the formula.

$$L = \frac{1}{2} \{ 180^\circ - (\Delta + \Delta') \} + \frac{1}{2} (z - z')$$

where  $\Delta$  and  $\Delta'$  are the polar distances of the south and north Stars respectively, and  $(z - z')$  the quantity measured by the micrometer. Then,

1. The *correction for level* is applied by adding the angle which the vertical axis of the instrument makes with the zenith, when its inclination is *southward*, or subtracting it when to the northward. This correction is found by multiplying the value of 1 division of the level scale, in arc, by one-half the mean change, in level divisions, which any one end of the bubble undergoes by reversing the instrument on the meridian; or, if  $o$  and  $e$ ,  $o'$  and  $e'$  denote the readings of the object and eye-ends of the bubble, for south and north stars respectively; corrections for level =  $\frac{1}{2} (o' - e') - \frac{1}{2} (o - e) \times$  the value of 1 division of the level scale in arc.

2. The correction for *error of meridional position* of the central vertical wire, is found by computing the usual "reduction to the meridian" for each star; then the difference between the reductions for the northern and southern stars is taken, and one-half that difference added or subtracted, according as the reduction for the *northern* star is *greater* or less than that for the southern; or,

$$\text{correction for position} = \frac{m' - m}{2}$$

$m$  being the reduction for stars south, and  $m'$  for stars north of the zenith.

3. The *correction for Refraction* is applied similarly to this last, but with a contrary sign; or,

$$\text{correction for refraction} = \frac{r - r'}{2}$$

$(r - r')$  being small, no note need be taken of the state of the barometer and thermometer at the time of observation. It is sufficient to use the actual tabular quantities.

Including all the corrections, the general expression for Latitude will be

$$L = \frac{180 - (\Delta + \Delta')}{2} + \frac{(z - z')}{2} \cdot a + \frac{(o' + e) - (o + e')}{4} \cdot b \\ + \frac{(m' - m)}{2} + \frac{(r - r')}{2}.$$

$a$  and  $b$  being the arc values of 1 division of the micrometer and level scale respectively.

4. Should the Star be observed on one side or the other of the central wire, the reduction to the meridian becomes

$$m = \frac{225}{4} \sin 1'' \cdot \sin 2 \Delta \cdot p^2 \\ = [6.4356974] \sin 2 \Delta \cdot p^2$$

$p$  being the hour angle of the Star in seconds of time.  $\sin 2 \Delta$  is negative when the Star is south of the equator or sub-pole.

5. To find the value  $a$ , of 1 division of the micrometer, note the time by chronometer of the transit of Polaris over the moveable wire placed vertically, and set successively to, say, every hundredth division of its scale. Then let  $x$  be the angular distance *from the meridian* at which any reading of the screw was had;  $p$ , the hour angle of the Star at the same instant, and  $\Delta$  its polar distance,

$$\sin x = \sin \Delta \sin p.$$

The value of  $x$  is computed for each reading, and the differences of these values, divided by the differences of the corresponding micrometer readings, give values for the screw.

6. The value  $b$ , of 1 division of the level scale will be best found by using, in conjunction with the micrometer, a distant point as a mark, or the central wire of another instrument used as a collimator; for the space above or below the mark, passed over by the horizontal wire of the micrometer, during the bubble's run over the scale, as the telescope's elevation is gradually altered, may afterwards be measured by the micrometer screw.

7. To correct, as much as possible, an erroneous determination of the value of the micrometer screw, select stars for observation such, if practicable, that the greatest Z. D. of a pair will belong as often to the N. Star as to the S. Star; for if the Z. D. of the N. Star is the greatest, the observed quantity is subtractive; if least, additive. For, as a general rule, the error of latitude, arising from an erroneous value to the micrometer screw, will be the least when in a set of stars,

$$\Sigma z - \Sigma z' = 0.$$

## FORM FOR RECORD AND COMPUTATION.

*Latitude, Station*      *Observations with Zenith Telescope*      *by*

| Date.             | No. of<br>S. A. C. | N. or<br>S. | Micrometers |        |                | Diff. Z. D. |      | Polar<br>distances. | Approximate<br>Latitude. | Levels. |      | State of Level. | Meridian dis-<br>tances. | Reduction to<br>meridian. | Mean refrac-<br>tion. | Corrections. |          |                  | Latitude.   |
|-------------------|--------------------|-------------|-------------|--------|----------------|-------------|------|---------------------|--------------------------|---------|------|-----------------|--------------------------|---------------------------|-----------------------|--------------|----------|------------------|-------------|
|                   |                    |             | A.          | B.     | Bymi.<br>crom. | In arc.     | "    |                     |                          | O.      | E.   |                 |                          |                           |                       | Level.       | Merid'n. | Refrac-<br>tion. |             |
| 1846.<br>Sept. 20 | 6640               | N.          | ....        | 1388.3 | ....           | ....        | "    | 33 38 10.29         | 42° 30'                  | 36.2    | 49.0 | -6.4            | 92.0                     | 0.40                      | 15.38                 | "            | "        | "                | 0 1 "       |
|                   | 6600               | S.          | 378.5       | ....   | 1664.8752      | 01          | .... | 63 21 06.28         | ....                     | 35.0    | 49.8 | +7.4            | 95.0                     | 0.85                      | 15.63                 | "            | "        | "                | "           |
|                   |                    |             |             |        |                |             |      | 94 59 17.07         |                          |         |      |                 |                          |                           |                       |              |          |                  |             |
|                   |                    |             |             |        |                |             |      | 85 00 48.93         |                          |         |      |                 |                          |                           |                       |              |          |                  |             |
|                   |                    |             |             |        |                |             |      | 12 33.01            |                          |         |      |                 |                          |                           |                       |              |          |                  |             |
| Sept. 20          | 6682               | N.          | ....        | 255.5  | ....           | ....        | .... | 29 47 01.20         | 37° 47'                  | ....    | .... | ....            | ....                     | ....                      | ....                  | +0.66        | -0.92    | +3.10            | 42 36 38.03 |
|                   | 6666               | S.          | ....        | 1298.7 | 1027.9         | 464.00      | .... | 64 51 56.23         | ....                     | 41.7    | 42.0 | -0.1            | 39.0                     | 1.03                      | 18.53                 |              |          |                  |             |
|                   |                    |             |             |        |                |             |      | 94 38 57.43         |                          | 41.9    | 43.3 | +1.0            | 94.0                     | 0.73                      | 18.38                 |              |          |                  |             |
|                   |                    |             |             |        |                |             |      | 85 21 02.57         |                          |         |      |                 |                          |                           |                       |              |          |                  |             |
|                   |                    |             |             |        |                |             |      | 7 44.00             |                          |         |      |                 |                          |                           |                       |              |          |                  |             |
|                   |                    |             |             |        |                |             |      | 85 13 18.57         | 39° 98'                  | ....    | .... | ....            | ....                     | ....                      | ....                  | +0.57        | +0.15    | -0.07            | 42 36 39.93 |

X. *Knowing the time and the latitude of the place, to find the Azimuth of the Sun or a Star.*

$$\text{tang } \frac{1}{2} (A + S) = \cot \frac{1}{2} p \frac{\cos \frac{1}{2} (\Delta - \lambda)}{\cos \frac{1}{2} (\Delta + \lambda)},$$

$$\text{tang } \frac{1}{2} (A - S) = \cot \frac{1}{2} p \frac{\sin \frac{1}{2} (\Delta - \lambda)}{\sin \frac{1}{2} (\Delta + \lambda)},$$

$$A = \frac{1}{2} (A + S) \mp \frac{1}{2} (A - S)$$

the *upper* or *negative* sign is used when  $\lambda$  is greater than  $\Delta$ .

Where

$A$  = the azimuth counted from the *north*, which must be subtracted from  $180^\circ$  if counted from the south.

$S$  = the angle at the star, called the angle of variation.

$\lambda$  = the co-latitude of the place.

$\Delta$  = the north polar distance of the sun or star.

$p$  = the hour angle at the pole.

XI. *Without the use of a chronometer, by observing the altitude of the sun or star at the same instant with the observation of the azimuth.*

Let  $Z$  = the zenith distance, corrected for refraction, parallax, and semidiameter.

$$\text{Cos } \frac{1}{2} A = \frac{\sin k \cdot \sin (k - \Delta)}{\sin Z \sin \lambda}$$

$$2k = Z + \Delta + \lambda$$

**XII.** *To find the amplitude of a celestial object at its rising or setting; by amplitude is meant the complement of the azimuth, or distance from the east or west points of the horizon.*

This is a particular case of the preceding problem. When the object appears to be in the horizon, its zenith distance, instead of being  $90^\circ$ , is, on account of refraction and parallax,  $90^\circ + k$ .

$$\begin{aligned}\text{Where } k &= \text{hor. refraction} - \text{hor. parallax} \\ &= 33' 45'' - \text{hor. parallax.}\end{aligned}$$

For stars, the hor. par. = 0 and  $k = 90^\circ 33' 45''$ , for the sun,  $k = 33' 45'' - 8'' 6$  and  $k = 90^\circ 33' 36''.4$ ; the mean refraction and mean hor. par. are here used as these observations are not susceptible of a great degree of accuracy.

**XIII.** *To find the true meridian by the method of equal altitudes of the Sun.*

The instrument remaining stationary, observe the readings of the horizontal limb when the altitude of the Sun's centre, or of either limb, is the same in the forenoon and afternoon.

Then, the correction to the mean of these two readings for the change in the sun's declination in the interval, is

$$c = \frac{\frac{1}{2}(D - D')}{\cos L \cdot \sin \frac{1}{2}(t - t')}$$

where

$D - D'$  = the change in the sun's declination in the interval of the observations,

$(t - t')$  = this interval of time, expressed in arc

$L$  = the latitude of the place.

XIV. *To find the azimuth of Polaris at its greatest eastern or western elongation.*

$$\cos p = \tan \Delta \cot \lambda = \cot D \tan L = \tan L \tan \Delta.$$

$$\cos L \sin A = \sin \Delta = \cos D, \text{ where,}$$

$p$  = the hour angle of the Star,  $A$  = the required azimuth,  
 $D$  = its declination,  $L$  = the lat. of the place,  
 $\Delta$  = its polar distance,  $\lambda$  = the co-latitude.

The first equations give the hour angle of the Star at its greatest elongation; hence the sidereal time of elongation.

The second, the azimuth of the Star at its greatest elongation.

The azimuth at *any* hour angle is found by the methods X and XI, or by the formula

$$A \text{ (in seconds)} = \frac{\sin p}{\cos L} \left\{ \Delta + \Delta^2 \sin 1'' \cos p \tan L \right\}$$

The most approved method is to observe a series of azimuths of Polaris *about* the elongation, say for not more than 30 minutes before and after, and to reduce them to the elongation; to do this, compute from the known latitude, the azimuth of the Star at its greatest elongation =  $A$ , and call the sidereal time from elongation  $t$ ; the correction to the azimuth will be,

$$c = (112.5) t^2 \sin 1'' \tan A$$

$$\log (112.5) \sin 1'' = 6.7367274.$$

The quantities found in the tables for "reduction to the meridian"  $\left( 2 \frac{\sin^2 \frac{1}{2} p}{\sin 1''} \right)$  correspond very nearly to  $(112.5) t^2 \sin 1''$ , when  $t$  does not exceed  $15'$ ; so, by entering the table with the time from elongation, and multiplying the tabular quantities by  $\tan A$ , we obtain the



required correction in seconds of arc. This will be found a convenient substitute for the more rigorous method.

In these observations, the optical axis of the telescope of the theodolite must be made to describe a truly vertical plane.

If the axis of the telescope is not horizontal, the correction to the azimuth will be

$$\pm \frac{d}{4} [(w + w') - (e + e')] \text{ tang } \star\text{'s altitude}$$

where  $d$  = the value of one division of the level scale,

$w$  = the inclination of the level to the *west*,

$e$  = the inclination of the level to the *east*,

$w'$  and  $e'$ , the same values after *reversing* the level.

#### XV. *Correction for Run in Reading Microscopes.*

As it is difficult to adjust the microscopes so that five revolutions of the micrometer screw shall carry the wire exactly over one of the five-minute spaces on the limb of the instrument, (if it be so graduated,) it is preferred to observe the number of revolutions and the part of a revolution made by the screw while the wire passes over the space; then

Let  $m$  = the mean of *first readings*, that is, the readings obtained by turning the screw in the direction of increasing numbers from zero of the comb.

$m'$  = the mean of *second, or reverse, readings*.

Then, (mean) Run =  $r = m - m' + 300$ , and

$$\text{true (mean) reading} = \frac{300 \cdot m}{r} = \frac{300 (r + m' - 300)}{r}$$

= the number of minutes and seconds to be added to the degrees and minutes of the limb.

XVI. *Lunar distances.*

To determine the *true* distance of the moon from the sun, or a star; the *apparent* distance, together with the *apparent* altitudes of the moon and the sun, or star, being given.

Let,

|                                        |                                        |
|----------------------------------------|----------------------------------------|
| $d$ = apparent distance                | $d'$ = true distance                   |
| $H$ = moon's app't altitude            | $H'$ = moon's true altitude            |
| $h$ = sun's app't altitude             | $h'$ = sun's true altitude             |
| $P$ = moon's hor. par. at place        | $P'$ = moon's par. in altitude         |
| $p$ = sun's hor. parallax              | $p'$ = sun's par. in altitude          |
| $S$ = moon's hor. semidiameter         | $S'$ = moon's augm. semidiameter       |
| $s$ = sun's semidiameter               | $D$ = observed distance                |
| $R$ = refraction for moon's altitude   | $r$ = refraction for sun's altitude    |
| $A$ = observed altitude of moon's limb | $a$ = observed altitude of sun's limb. |

$P = \pi - \pi \cdot E \cdot \sin^2 L$ ; where  $\pi$  = moon's equatorial horizontal parallax.

$E$  = the ellipticity,  $\log E = 7.5233789$ ;  $L$  = the latitude of place.

|                     |                                |
|---------------------|--------------------------------|
| $S = [9.43537] P$   | $S' = S + \text{augmentation}$ |
| $H = A \pm S'$      | $h = a \pm s$                  |
| $P' = P \cos H$     | $p' = p \cos h$                |
| $H' = H + (P' - R)$ | $h' = h - (r - p')$            |

*For a Star or a Planet.*

$$h' = h - r \qquad d = D \pm S'$$

$$\sin^2 C = \frac{\cos h' \cos H'}{\cos h \cos H} \cos \frac{1}{2}(h+H+d) \cos \frac{1}{2}(h+H-d)$$

$$\sin^2 \frac{1}{2} d' = \cos \left\{ \frac{1}{2}(h' + H') + C \right\} \cos \left\{ \frac{1}{2}(h' + H') - C \right\}$$

The *reduced* distance being thus found, the longitude may be deduced from it as follows:

Suppose that at 5<sup>hr</sup> 05<sup>m</sup> 56<sup>s</sup> mean time, 29th April, 1838, at a place whose longitude is presumed to be 4<sup>hr</sup> 45<sup>m</sup> 00<sup>s</sup> west of Greenwich, the result of observations gave the *reduced* distance between the sun and moon,  $d' = 71^\circ 05' 35''$

Mean time obs'n = 5<sup>hr</sup> 05<sup>m</sup> 56<sup>s</sup>

Approx. long'de = 4 45 00

9 50 56 approx. Greenwich m.  
time of observation.

|                                                |                          |  |
|------------------------------------------------|--------------------------|--|
| By Naut. Alm. at IX <sup>h</sup> = 70° 41' 30" | 70° 41' 30"              |  |
| (April 29th) XII <sup>h</sup> = 72° 07' 47"    | $d' = 71^\circ 05' 35''$ |  |
| 1 26 17                                        | 24 05"                   |  |

Increase of distance in 3<sup>hr</sup> = 5177".0     $\delta d' = 1445''$

Then 5177" : 10800 :: 1445" :  $x = 0^h 50^m 14.5$

Add 9<sup>hr</sup>

Greenwich mean time deduced = 9<sup>hr</sup> 50<sup>m</sup> 14.5

Mean time at place = 5 05 56.0

Longitude, deduced = 4<sup>h</sup> 44<sup>m</sup> 18.5

The reduction of this proportion is very much facilitated by the use of *Proportional Logarithms*, or logs. of  $\frac{3^{\text{hrs}}}{T}$  given in treatises on Navigation, in conjunction with those in the Nautical Almanac.

The proportion, however, requires a correction for second differences, when greater accuracy is desired, arising from the irregularity of the moon's motion.

A closer approximation to the true value of the quantity  $x$  being

$$X = \frac{3^{\text{hrs}} \delta d'}{A + \frac{1}{2} B x}$$

In which  $B = \frac{1}{2}$  the sum of the second differences, and  $A =$  the middle first difference  $- B$ ; thus,

*From the Nautical Almanac, April 29, 1838.*

|                     | 1st difference. | 2d difference.        |
|---------------------|-----------------|-----------------------|
| At VI = 69° 14' 54" |                 |                       |
| IX = 70° 41' 30"    | + 1° 26' 36"    |                       |
| XII = 72° 07' 47"   | + 1° 26' 17"    | = $\Delta_1$ — 0' 19" |
| XV = 73° 33' 46"    | + 1° 25' 59"    | — 0' 18"              |

$$x = 50^{\text{m}} 14.5 = 0^{\text{hrs}} 83736 \text{ (table page 173.)}$$

$$B = -9''.2; A = \Delta_1 - B = 5177'' + 9''.2 = 5186''.2$$

$$\delta d = 1445''; \frac{1}{2} B x = -2''.56; A + \frac{1}{2} B x = 5183''.64$$

whence

$$X = \frac{10800 \times 1445''}{5183''.64} = 50^{\text{m}} 10.6.$$

$$\text{and, longitude deduced} = 4^{\text{hrs}} 44^{\text{m}} 14.6.$$

*Reduction of the Moon's Equatorial Horizontal Parallax to the Horizontal Parallax in any Latitude.*

| LATITUDE. | HORIZONTAL PARALLAX. |      |      |      |      |
|-----------|----------------------|------|------|------|------|
|           | 54'                  | 56'  | 58'  | 60'  | 62'  |
| 0         | "                    | "    | "    | "    | "    |
| 0         | 0.0                  | 0.0  | 0.0  | 0.0  | 0.0  |
| 8         | 0.2                  | 0.2  | 0.2  | 0.2  | 0.2  |
| 16        | 0.8                  | 0.8  | 0.9  | 0.9  | 0.9  |
| 20        | 1.3                  | 1.3  | 1.4  | 1.4  | 1.5  |
| 24        | 1.8                  | 1.9  | 1.9  | 2.0  | 2.0  |
| 28        | 2.4                  | 2.5  | 2.6  | 2.6  | 2.7  |
| 32        | 3.0                  | 3.1  | 3.3  | 3.4  | 3.5  |
| 36        | 3.7                  | 3.9  | 4.0  | 4.1  | 4.3  |
| 40        | 4.5                  | 4.6  | 4.8  | 5.0  | 5.1  |
| 44        | 5.2                  | 5.4  | 5.6  | 5.8  | 6.0  |
| 48        | 6.0                  | 6.2  | 6.4  | 6.6  | 6.8  |
| 52        | 6.7                  | 7.0  | 7.2  | 7.4  | 7.6  |
| 56        | 7.4                  | 7.7  | 8.0  | 8.2  | 8.5  |
| 60        | 8.1                  | 8.4  | 8.7  | 9.0  | 9.3  |
| 64        | 8.8                  | 9.1  | 9.4  | 9.7  | 10.0 |
| 68        | 9.3                  | 9.6  | 10.0 | 10.3 | 10.6 |
| 72        | 9.8                  | 10.1 | 10.4 | 10.8 | 11.2 |
| 76        | 10.2                 | 10.6 | 10.9 | 11.3 | 11.7 |
| 84        | 10.7                 | 11.1 | 11.5 | 11.9 | 12.0 |
| 90        | 10.8                 | 11.2 | 11.6 | 12.0 | 12.4 |

The moon's horizontal parallax, given in the second page of each month, in the "American Nautical Almanac," for noon and midnight, is the equatorial parallax for Greenwich mean noon and midnight; from thence it is to be deduced for the time and place of observation. The correction for latitude, on account of the spheroidal figure of the earth, can be made from the table above. Thus, supposing the hor. equat. par. to be 58'; the hor. par. in lat  $52^{\circ}$  would be  $58' - 7''.2 = 57' 52''.8$ .

*Augmentation of the Moon's Semidiameter, on account of  
her apparent altitude.*

| APPARENT AL-<br>TITUDE. | HORIZONTAL SEMIDIAMETER. |         |          |         |          |         |
|-------------------------|--------------------------|---------|----------|---------|----------|---------|
|                         | 14' 30''                 | 15' 0'' | 15' 30'' | 16' 0'' | 16' 30'' | 17' 0'' |
| 0                       | "                        | "       | "        | "       | "        | "       |
| 0                       | 0.00                     | 0.00    | 0.00     | 0.00    | 0.00     | 0.00    |
| 3                       | 0.71                     | 0.75    | 0.80     | 0.86    | 0.92     | 0.97    |
| 6                       | 1.41                     | 1.50    | 1.60     | 1.71    | 1.83     | 1.94    |
| 9                       | 2.11                     | 2.25    | 2.40     | 2.56    | 2.73     | 2.90    |
| 12                      | 2.81                     | 3.00    | 3.20     | 3.41    | 3.63     | 3.86    |
| 15                      | 3.50                     | 3.74    | 3.99     | 4.25    | 4.52     | 4.80    |
| 18                      | 4.17                     | 4.46    | 4.76     | 5.07    | 5.39     | 5.73    |
| 21                      | 4.84                     | 5.18    | 5.52     | 5.89    | 6.26     | 6.65    |
| 24                      | 5.49                     | 5.88    | 6.27     | 6.68    | 7.11     | 7.54    |
| 27                      | 6.13                     | 6.56    | 7.00     | 7.46    | 7.93     | 8.42    |
| 30                      | 6.75                     | 7.23    | 7.71     | 8.22    | 8.74     | 9.28    |
| 33                      | 7.35                     | 7.88    | 8.40     | 8.96    | 9.52     | 10.12   |
| 36                      | 7.93                     | 8.50    | 9.07     | 9.67    | 10.28    | 10.92   |
| 39                      | 8.49                     | 9.10    | 9.72     | 10.36   | 11.02    | 11.66   |
| 42                      | 9.03                     | 9.68    | 10.34    | 11.02   | 11.72    | 12.44   |
| 45                      | 9.55                     | 10.23   | 10.93    | 11.65   | 12.39    | 13.15   |
| 48                      | 10.05                    | 10.76   | 11.49    | 12.25   | 13.03    | 13.83   |
| 51                      | 10.52                    | 11.26   | 12.02    | 12.81   | 13.63    | 14.46   |
| 54                      | 10.95                    | 11.72   | 12.52    | 13.34   | 14.19    | 15.06   |
| 57                      | 11.35                    | 12.15   | 12.98    | 13.83   | 14.72    | 15.62   |
| 60                      | 11.72                    | 12.55   | 13.40    | 14.29   | 15.20    | 16.13   |
| 63                      | 12.06                    | 12.91   | 13.79    | 14.70   | 15.64    | 16.60   |
| 66                      | 12.37                    | 13.24   | 14.14    | 15.08   | 16.04    | 17.03   |
| 69                      | 12.64                    | 13.53   | 14.46    | 15.41   | 16.39    | 17.40   |
| 72                      | 12.88                    | 13.79   | 14.73    | 15.70   | 16.70    | 17.73   |
| 75                      | 13.08                    | 14.01   | 14.96    | 15.95   | 16.96    | 18.01   |
| 78                      | 13.24                    | 14.18   | 15.15    | 16.15   | 17.18    | 18.24   |
| 81                      | 13.37                    | 14.32   | 15.30    | 16.31   | 17.35    | 18.42   |
| 84                      | 13.46                    | 14.42   | 15.41    | 16.42   | 17.47    | 18.55   |
| 87                      | 13.52                    | 14.48   | 15.47    | 16.49   | 17.54    | 18.62   |
| 90                      | 13.54                    | 14.50   | 15.49    | 16.51   | 17.57    | 18.65   |

XVII. *Longitude by Lunar Culminations.*

1. *Interpolation.*—When the quantities in the ephemeris are given in intervals of  $12^{\text{hr}}$ , and the assumed meridian is  $+$ , or west of Greenwich, the following arrangement will be found convenient:

Let  $a_1$  = the moon's place, from the ephemeris, for the preceding noon or midnight,

$a'$  = the moon's place, for the following midnight or noon,

$a = \frac{1}{2} (a_1 + a')$ ,

$b$  = the middle first difference,

$c$  = the mean of the two middle second differences,

$= \frac{1}{2} (c_1 + c')$ ,

$d$  = the middle third difference,

$e$  = the mean of the two fourth differences

$= \frac{1}{2} (e_1 + e')$ ,

$f$  = the fifth differences,

$t$  = the interval in seconds since the date for  $a_1$ ,

$m$  = the variation of the moon's place for the interval  $(t - 6^{\text{hr}})$ ,

$n$  = the average hourly variation,

$n'$  = the true hourly variation at the instant,  $t$ ,

Enclosing in brackets the constant log. co-efficients,

Let  $X = [5.3645163] (t - 6^{\text{h}} 0^{\text{m}} 0^{\text{s}})$

$X' = [0.42800] t (t - 12^{\text{h}} 0^{\text{m}} 0^{\text{s}})$

$X'' = [9.5229] XX'$ .

$X''' = [9.6499] X' (t + 12^{\text{h}} 0^{\text{m}} 0^{\text{s}}) (t - 24^{\text{h}} 0^{\text{m}} 0^{\text{s}})$

Then:

$$m = b X + c X' + d X'' + e X'''$$

$$n = [3.25527] \left( \frac{b + 2m}{t} \right)$$

$$n' = \frac{1}{15} \{ (b + \frac{1}{15}d - \frac{1}{15}f) + (c - \frac{1}{5}e) X + d X' \}$$

If the corrections beyond the *second* differences are neglected, then

$$m = b X + c X'$$

$$n = [3.25527] \left( \frac{b + 2m}{t} \right)$$

This will require but four quantities from the ephemeris ; two preceding and two following the time  $t$ .

2. To apply this to *moon culminations* :

Let AR = the right ascension in the Nautical Almanac of the moon's bright limb at Greenwich for the upper transit next preceding the transit observed.

AR' = the observed AR of the moon's bright limb at the place whose longitude,  $L$ , is required.

Assume an approximate longitude,  $l$ , and compute from the Nautical Almanac, by means of the foregoing method of interpolation, what the increase,  $m$ , in the AR of the moon's bright limb from its last transit at Greenwich, should be for that longitude.

As the correction, in this case, is to be applied to  $a_1$ , instead of  $\frac{1}{2} (a_1 + a')$ , the co-efficient  $X$  becomes =  $[5.3645163] l$ ; the other co-efficients remaining the same, merely changing  $t$  to  $l$ .

By your own observations and the Nautical Almanac, this change is  $(AR' - AR)$ ; then

$$\text{as } m : (AR' - AR) :: l : L \text{ and}$$

$$L = (AR' - AR) \cdot \frac{l}{m}$$



As the moon's motion in right ascension is not uniform, this proportion is only true when the values of  $l$  and  $L$  are nearly equal; but it is supposed that the approximate longitude is known to within a minute of time. It has also been supposed that both  $AR$  and  $AR'$  are correctly determined; that the quantities in the Nautical Almanac are free from errors in the Lunar Tables, and those of nutation, &c.; and that the observed  $AR$  is corrected for error of clock and errors of position, etc., in the Transit instrument.

It is to eliminate these sources of error that *moon culminating stars* are observed in conjunction with the moon, and that corresponding observations at points whose positions are accurately known, are substituted for the tabular values, although the elements of the Nautical Almanac give very good approximations.

The complete method will be better illustrated by an example:

Suppose that at a station, whose longitude is presumed to be  $4^h 55^m 50^s$  west of Greenwich, the following transits have been taken with a Chronometer marking sidereal time; the error of the Chronometer being immaterial, but the Transit instrument being supposed in the meridian, or very nearly so.

|                                      |                      |                         |
|--------------------------------------|----------------------|-------------------------|
| February 18, $\zeta$ Geminorum       | $6^h 54^m 41^s.75$   |                         |
| $\delta$ Geminorum                   | $7 \ 10 \ 38.97$     |                         |
| $\mathcal{D}$ 's 1st Limb            | — — —                | $7^h 28^m 06^s.76$      |
| $\zeta$ Cancri                       | $8 \ 03 \ 06.11$     |                         |
| Sum                                  | $3) 22 \ 08 \ 26.83$ | $7 \ 22 \ 48.943$       |
|                                      |                      | Diff. $0 \ 15 \ 17.817$ |
| Rate of Chronometer + $3^s$ , daily, |                      | — $.0318$               |
| Corrected difference = $t$ ,         |                      | $= 0 \ 15 \ 17.785$     |

And suppose the following to be the corresponding observations at Greenwich, (these, however, are from the Nautical Almanac.)

|                                |                             |                             |
|--------------------------------|-----------------------------|-----------------------------|
| February 18, $\zeta$ Geminorum | $6^h$ 54 <sup>m</sup> 57.41 |                             |
| $\delta$ Geminorum             | 7 10 54.36                  |                             |
| $\mathcal{D}$ 's 1st Limb      | - - -                       | $7^h$ 27 <sup>m</sup> 47.66 |
| $\zeta$ Cancrī                 | 8 03 21.44                  |                             |
|                                | 3) 22 09 13.21              | 7 23 04.403                 |
| Difference = $t'$              |                             | = 0 04 43.257               |
| $t$ ,                          |                             | = 0 15 17.785               |

then  $t, -t' =$  observed increase in  $\mathcal{D}$ 's AR =  $m' = 10 \ 34.528$

In the same manner would be obtained, for other corresponding observations, values of  $m', m'', \&c.$

Next, compute this increase from the Nautical Almanac, as follows :

|                                                          |               |
|----------------------------------------------------------|---------------|
| <i>Approximate Longitude</i> = $l = 4^h \ 55^m \ 50^s$ . |               |
| $l = 4^h \ 55^m \ 50^s = 17750^s$ ; log                  | 4.2491984     |
| constant . . . . .                                       | = 5.3645163   |
| log X . . . . .                                          | = + 9.6137147 |
| $l - 12 \text{ hrs.} = -25450^s$ ; log = -4.40568        |               |
| log $l$ . . . . .                                        | = + 4.24919   |
| constant . . . . .                                       | = + 0.42800   |
| log $X'$ . . . . .                                       | = - 9.08287   |
| log X . . . . .                                          | = + 9.6137    |
| log $X'$ . . . . .                                       | = - 9.0828    |
| constant . . . . .                                       | = + 9.5229    |
| log $X''$ . . . . .                                      | = - 8.2194    |
| $l + 12 \text{ hrs.} = 60950^s$ ; log                    | = + 4.7849    |
| $l - 24 \text{ hrs.} = 68650^s$ ; log                    | = - 4.8366    |
| log $X'$ . . . . .                                       | = - 9.0828    |
| constant . . . . .                                       | = + 9.6499    |
| log $X'''$ . . . . .                                     | = + 8.3542    |

| Day                                                                                                                                                                                                                                                                                                     | Ce | AR D's 1st limb by Naut. Almanac.                  | $\Delta_1$                            | $\Delta_2$                           | $\Delta_3$           | $\Delta_4$    |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|----------------------------------------------------|---------------------------------------|--------------------------------------|----------------------|---------------|
| 17                                                                                                                                                                                                                                                                                                      | U  | 6 <sup>h</sup> 35 <sup>m</sup> 55 <sup>s</sup> .73 | + 26 <sup>m</sup> 00 <sup>s</sup> .54 | — 0 <sup>m</sup> 09 <sup>s</sup> .15 |                      |               |
| "                                                                                                                                                                                                                                                                                                       | L  | 7 01 56.57                                         | + 25 51.39                            | $e_1 = -0$ 10.21                     | — 01 <sup>m</sup> 06 | $e_1 = +0.81$ |
| 18                                                                                                                                                                                                                                                                                                      | U  | 7 27 47.66                                         | $b = +25$ 41.18                       | $e_1^1 = -0$ 10.46                   | $d = -$ 0.25         | $e_1 = +0.84$ |
| "                                                                                                                                                                                                                                                                                                       | L  | 7 53 28.84                                         | + 25 30.72                            | — 0 09.87                            | + 0.59               |               |
| 19                                                                                                                                                                                                                                                                                                      | U  | 8 18 59.56                                         | + 25 20.85                            |                                      |                      |               |
| "                                                                                                                                                                                                                                                                                                       | L  | 8 44 20.41                                         |                                       |                                      |                      |               |
| Sum of differences . . .                                                                                                                                                                                                                                                                                |    |                                                    |                                       |                                      |                      |               |
| Upper left hand quantity . . .                                                                                                                                                                                                                                                                          |    |                                                    |                                       |                                      |                      |               |
| Check. Sum + upper left }<br>= lower left }                                                                                                                                                                                                                                                             |    |                                                    |                                       |                                      |                      |               |
| $b, c, d, e,$                                                                                                                                                                                                                                                                                           |    |                                                    |                                       |                                      |                      |               |
| $\log b, \log c, \log d, \log e$                                                                                                                                                                                                                                                                        |    |                                                    |                                       |                                      |                      |               |
| $\log X, \log X', \log X'', \log X'''$                                                                                                                                                                                                                                                                  |    |                                                    |                                       |                                      |                      |               |
| $\log b X, \log c X', \text{etc}$                                                                                                                                                                                                                                                                       |    |                                                    |                                       |                                      |                      |               |
| $b X, c X', d X'', \text{etc}$                                                                                                                                                                                                                                                                          |    |                                                    |                                       |                                      |                      |               |
| $\begin{array}{r} b X \\ e X' \\ c X'' \\ X''' \\ \hline \end{array} = 633^{\circ}.240$ $\begin{array}{r} \\ \\ \\ + \\ \hline \end{array} = +1.250$ $\begin{array}{r} \\ \\ \\ + \\ \hline \end{array} = .004$ $\begin{array}{r} \\ \\ \\ + \\ \hline \end{array} = .018$ $\hline 634^{\circ}.512 = m$ |    |                                                    |                                       |                                      |                      |               |
| $\begin{array}{r} \log l \\ \log m \\ \hline \end{array} = 4.2491984$ $\begin{array}{r} \\ \hline \end{array} = 2.8024399$ $\log \frac{l}{m} = 1.4467585$                                                                                                                                               |    |                                                    |                                       |                                      |                      |               |

Then,

$$\text{observed increase} = 634.528 = m'$$

$$\text{computed do.} = 634.512 = m$$

$$\text{observed excess} = m' - m = 0.016.$$

$$\begin{aligned} \text{Longitude, deduced,} &= 4^{\text{h}} 55^{\text{m}} 50^{\text{s}} + \frac{l}{m}(m' - m) \\ &= 4^{\text{h}} 55^{\text{m}} 50.45 \end{aligned}$$

If there are corresponding observations at some other well known point, say Cambridge, Mass., longitude =  $4^{\text{h}} 44^{\text{m}} 32^{\text{s}} = l'$ ; compute the increase  $m_1$  for this longitude, by changing the co-efficients  $X, X', X'',$  etc., to correspond to  $l'$ . Then  $(m - m_1)$  will be the computed increase for Cambridge to your station, and  $\frac{l'}{m_1}$  the rate of this increase, with which proceed as above.

It often happens that two observers do not use the same number of wires, or that the same number of stars are not observed at the two places. In such cases the observed increase of the right ascension of the moon's limb requires a correction, which Mr. Walker deduces as follows, from Gauss's method :

For the European observatory and western station respectively,

Let  $A'$  and  $A$  = the observed AR of a star,

$$E = A' - A \text{ for the same star,}$$

$$E = \text{a similar value for another star,}$$

$l$  and  $l'$  = the number of wires on which each limb was observed,

$a$  and  $a'$  = similar values for a star,

$$\lambda = \frac{l l'}{l + l'}, \text{ for the moon's limb,}$$

$$u = \frac{a a'}{a + a'}, \text{ for one star.}$$

$u'$  = a similar value for another star,

$\Sigma$  = symbol to denote the aggregate of similar quantities,

$\epsilon$  = the correction required.

$$\text{Then } \epsilon = \frac{\Sigma \left( E \frac{\lambda u}{\lambda + u} \right)}{\Sigma \frac{\lambda u}{\lambda + u}}$$

$$\text{and } L = l + \frac{l}{m} (m' - m + \epsilon)$$

Also, calling  $W$ , the *weight* of each day's comparison,

$$W = \frac{\sigma \lambda}{(\sigma + \lambda) z^3}$$

in which  $z$  is the same as  $\frac{l}{m}$  and  $\sigma = u + u' + u''$ , etc.

For the weight of the result of all the comparisons, we have

$$\Sigma W = \Sigma \frac{\sigma \lambda}{(\sigma + \lambda) z^3}$$

Let  $e$  denote the probable error of observation, and  $E$  the probable error of the final result; then,

$$E = \Sigma \sqrt{\frac{e^2}{\Sigma \frac{\sigma \lambda}{(\sigma + \lambda) z^3}}}$$

It frequently happens that the moon cannot be observed on the middle wire, in which case she is far enough from the meridian to have a sensible parallax in

right ascension; and as it may be very desirable not to lose the observation, this parallax must be computed and applied to the hour angle from the middle wire, which is supposed to be nearly coincident with the meridian.

Denoting this parallax in right ascension by  $p$ , the horizontal parallax by  $w$ , the latitude of the place of observation by  $\phi$ , and the true declination of the moon by  $\delta$ , we have from the ordinary series for the parallax in right ascension, neglecting the terms after the first, which would in this case be insignificant,

$$p = \theta \sin w \cos \phi \sec \delta,$$

in which  $\theta$ , is the hour angle, or equatorial interval in sidereal time from the lateral wire on which the moon is observed to the central wire; so that, at the instant of observation, the actual distance of the moon's limb from the central wire is:

$$\theta - \theta \sin w \cos \phi \sec \delta,$$

and the reduction to meridian or middle wire will be

$$\pm \frac{\theta}{\cos \delta} \cdot \frac{1 - \sin w \cos \phi \sec \delta}{1 - 0.00277 m}$$

in which  $m$ , is the motion of the moon in right ascension in one day, expressed in degrees. The upper sign is to be used when the observation is on a wire *before*, and the lower *after* the middle wire.

XVIII. *The value of a quantity at three consecutive whole hours,  $T-1$ ,  $T$  and  $T+1$ , being given, to find its value at an intermediate time  $T'$ , and its hourly variation at that time.*

Attending to the algebraic signs, subtract the value of the quantity at the time  $T-1$ , from its value at the time  $T$ ; and its value at the time  $T$ , from its value at the time  $T+1$ ; and the remainders will be the *first differences*. Subtract the first of these from the second, and the remainder will be the *second difference*. Let  $a$  = the value of the quantity at the time  $T$ ;  $b$  = the half sum of the first differences;  $c$  = the second difference; and  $t$  = the interval between  $T$  and  $T'$ , expressed in the fraction of an hour, and marked negative when  $T'$  is *earlier* than  $T$ . Then the value of the quantity at the time  $T'$ , will be

$$a + t b + \frac{t^2}{2} c.$$

And the hourly variation of the quantity at the time  $T'$ , will be

$$b + t c.$$

EXAMPLE.

Given the moon's declination, on a certain day, as follows:

At  $10^h$ ,  $D = + 15^\circ 58' 50''.1$ ; at  $11^h$ ,  $D = 15^\circ 47' 11''.0$ ;

At  $12^h$ ,  $D = 15^\circ 35' 27''.1$ . Required its value at  $10\frac{3}{4}^h$ .

|                                                                                        | D                       | 1st differences. | 2d difference. |
|----------------------------------------------------------------------------------------|-------------------------|------------------|----------------|
| 10                                                                                     | $+ 15^\circ 58' 50''.1$ |                  |                |
| 11                                                                                     | $15^\circ 47' 11''.0$   | $- 11' 39''.1$   |                |
| 12                                                                                     | $15^\circ 35' 27''.1$   | $- 11' 43''.9$   | $- 4''.8$      |
| $a = + 15^\circ 47' 11''.0$ , $b = - 11' 41''.5$ , $c = - 4''.8$ , $t = - \frac{3}{4}$ |                         |                  |                |
| $t b = + 4' 40''.6$                                                                    |                         |                  |                |
| $\frac{t^2}{2} c = - 0''.4$                                                            |                         |                  |                |
| $D = + 15^\circ 51' 51''.2$ at time $T'$                                               |                         |                  |                |
| $b = - 11' 41''.5$                                                                     |                         |                  |                |
| $t. c = + 1''.9$                                                                       |                         |                  |                |
| Hourly variation at time $T' = - 11' 39''.6$                                           |                         |                  |                |

**XIX. To find the Longitude of a place from an observed occultation of a fixed star by the Moon.**

Let A = Moon's AR,

A' = Star's AR,

D = Moon's declination,

D' = Star's declination,

A'' = Moon's hourly variation in AR,

D'' = Moon's hourly variation in declination,

$\pi$  = Moon's equatorial horizontal parallax,

H' = Star's hour angle for Greenwich,

$k = \frac{\text{sine moon's appt. semidiam.}}{\pi} = \text{constant} = 0.2725,$

$\log = 9.43536,$

$\phi$  = Geographical north latitude of place,

$\phi'$  = Geocentric north latitude of place,

$\rho$  = Earth's radius at place.

It is unnecessary to compute  $\phi'$  and  $\rho$  separately, as

$$\rho \sin \phi' = \frac{(1-e^2)}{\sqrt{1-e^2 \sin^2 \phi}} \cdot \sin \phi = A \sin \phi$$

$$\rho \cos \phi' = \frac{1}{\sqrt{1-e^2 \sin^2 \phi}} \cdot \cos \phi = B \cos \phi$$

in which  $e = .081697$  = the Earth's eccentricity; and as the values of  $\log A$  and  $\log B$  may be taken from the following table, with the argument  $\phi$  :

| $\phi$ | Log A. | Log B. |
|--------|--------|--------|
| 0      | 9.9971 | 0.0000 |
| 10     | 9.9971 | 0.0000 |
| 20     | 9.9973 | 0.0002 |
| 30     | 9.9975 | 0.0004 |
| 40     | 9.9977 | 0.0006 |
| 50     | 9.9979 | 0.0009 |
| 60     | 9.9982 | 0.0011 |
| 70     | 9.9984 | 0.0013 |



1. With the estimated Longitude of the place, reduce the observed mean time of immersion to Greenwich time. Let  $T$  stand for this time, and  $T'$  for the same time, taken to the nearest tenth of an hour. From the Nautical Almanac, find for the time  $T'$  by the problem on page 232, the values of  $A$ ,  $D$ ,  $A''$ ,  $D''$ , and by proportion, the value of  $\pi$ ; and also take out the values of  $A'$ ,  $D'$ , and the sidereal time of mean moon.

2. With the values of  $A$ ,  $D$ , etc., at the time  $T'$ , find the values of  $p$ ,  $q$ ,  $p'$  and  $q'$ , from the following formulæ:

$$p = \frac{(A - A') \cos D}{\pi}, \quad c = \frac{D - D'}{\pi}$$

$$\log B = \log p + \log \sin D' + 4.6856$$

$$d = B (A - A'); \quad q = c + \frac{1}{2} d,$$

$$a' = \frac{A'' \cos D}{\pi}, \quad b' = \frac{D''}{\pi}$$

$$c' = B A'' \quad d' = B D''$$

$$p' = a' - d' \quad q' = b' + c'$$

3. To the sidereal time at mean noon, add the sidereal time corresponding to the interval that  $T$  is past noon, and from the sum subtract  $A'$ . To the remainder, apply the longitude of the place in time, by *adding* if it is *east*, but *subtracting* if it is *west*, and converting the result into degrees, it will be  $H$ , the star's hour angle at the observed time of immersion.

4. Having found  $\log \rho \cos \phi'$  and  $\log \rho \sin \phi'$ , for the place, find  $u$ ,  $v$ ,  $N$ ,  $F$ ,  $t$  and  $t''$  by the following formulæ:

$$f = \rho \sin \phi' \cos D'$$

$$u = \rho \cos \phi' \sin H, \quad g = \rho \cos \phi' \cos H \sin D'$$

$$v = f - g,$$

$$\cot N = \frac{q'}{p'}, \quad d = (p - u) \cot N,$$

$$\cos F = \frac{(d + v - q) \sin N}{k},$$

$$t = \frac{k \cos (N + F)}{p'}, \quad t'' = \frac{p - u}{p'}.$$

Then will  $T' - t'' + t$ , be the corrected Greenwich mean time of the immersion. The difference between this and the observed time, will be the Longitude in time; *west* if the observed time is the *earlier* of the two, but *east*, if it is *later*.

In a similar manner would be deduced the Longitude from the observed emersion, except, that instead of  $t$ , we find  $t' = \frac{k \cos (N - F)}{p'}$ . When the immersion and emersion have both been observed, the Longitude should be obtained from each, and the mean of the two results taken.

EXAMPLE.

Suppose the observed immersion of  $\iota$  Leonis, on Jan. 7th, 1836, at a place in Latitude  $52^\circ 08' 28''$  N., estimated Longitude 0 h. 1 m. W., was 10 h. 45 m. 53.3 sec., mean time; required the Longitude of the place.

The observed time of immersion reduced to Greenwich time is,  
 $T = 10 \text{ h. } 46 \text{ m. } 53.3 \text{ sec.}$  Taking  $T' = 10.8 \text{ h.} = 10\frac{1}{2} \text{ h.}$ , we easily  
 find from the Nautical Almanac,

$$\begin{aligned} A &= 10^h 20^m 33.89 & D &= + 15^\circ 49' 31''.2 \\ A' &= 12 \quad 23 \quad 26.39 & D' &= + 14^\circ 58' 38''.8 \\ A'' &= 122^\circ.905 = (\text{in arc}), 1843''.6; & D'' &= - 700''.5 \end{aligned}$$

$$A - A' = - 2587''.5; \quad D - D' = 3052''.4; \quad \pi = 3362''.0$$

$$\begin{aligned} A - A' &\dots\dots \log 3.41288 - & D - D' &\dots\dots \log 3.48464 \\ \pi &= \text{Ar. Co.} \quad 6.47340 & \pi &= \text{Ar. Co.} \log 6.47340 \end{aligned}$$

$$D = \dots\dots \cos 9.98322 \quad c = .9079 = 9.95804$$

$$p = - \dots .7404 = 9.86950 - \quad \frac{1}{2} d = .0012$$

$$D' = \dots \sin 9.4124 \quad q = .9091$$

$$\underline{4.6856}$$

$$B = 3.9675 -$$

$$A - A' \dots\dots \log 3.4129$$

$$d = .0024 = 7.3804$$

$$A'' = \dots\dots \log 3.26567$$

$$\pi \dots \text{Ar. Co.} \log 6.47340$$

$$D \dots\dots\dots \cos 9.98322$$

$$D'' \dots\dots \log 2.84541 -$$

$$\pi \text{ . Ar. Co.} \log 6.47340$$

$$b'' = - .2084 = 9.31881 -$$

$$a' = .5276 = \dots 9.72229$$

$$B = 3.9675 -$$

$$B = 3.9675 -$$

$$A'' \dots\dots\dots 3.2657 -$$

$$D'' \dots\dots\dots 2.8454 -$$

$$c' = - .0017 = 7.2332 -$$

$$d' = .0006 = 6.8129$$

$$p' = a' - d' = .5270;$$

$$q' = b' + c' = - .2101$$

Sidereal time at mean noon Greenwich from N. A. =  $19^h 04^m 22.41$

Sidereal interval from noon to time T. . . . .  $10 \quad 48 \quad 39.57$

$$\underline{5 \quad 53 \quad 01.98}$$

$$A' \dots\dots\dots 10 \quad 23 \quad 26.39$$

$$\underline{- \quad 4 \quad 30 \quad 24.41}$$

$$\underline{1 \quad 00}$$

$$H = - 67^\circ 51' 06'' = - \quad 4 \quad 31 \quad 24.41$$

From page 233 we have

$$\log g \cos \phi' = 9.78888$$

$$\log g \sin \phi' = 9.89538$$

$$g \sin \phi' = 9.89538$$

$$D' \cos \quad \quad 9.98499$$

$$f = .7592 = 9.88037$$

$$g \cos \phi \quad . . . \quad 9.78888$$

$$g \cos \phi \quad . . . \quad 9.78888$$

$$H \quad . . . \quad \sin 9.96671 -$$

$$H \quad . . . \quad \cos 9.57635$$

$$u = - .5696 = 9.75559 -$$

$$D' \quad . . . \quad \sin 9.41236$$

$$v = .6993$$

$$g = .0599 = 8.77759$$

$$q' \quad . . . \quad \log 9.32243 -$$

$$N \quad . . . \quad \sin 9.96797$$

$$p' \text{ Ar. Co.} \quad \log 0.27819 \quad d + v - q = - .1417 \log 9.15137$$

$$N = 111^\circ 44' 10'' \cot 9.60062 -$$

$$k \text{ Ar. Co.} \quad \log 0.56463$$

$$p - u = - .1708 = \log 9.23249 -, \quad F = 118^\circ 53' 00'' \cos 9.68397 -$$

$$d = .0681 = 8.83311$$

$$N + F = 230^\circ 37' 10'' \cos 9.80241 -, \quad p - u \quad . . . \quad \log 9.23249 -$$

$$k \quad . . . \quad \log 9.43537 \quad p' \text{ Ar. Co.} \quad \log 0.27819$$

$$p' \text{ Ar. Co.} \quad \log 0.27819 \quad t'' = - .3241 = 9.51068 -$$

$$t = - .3281 \quad 9.51597 -$$

$$T' - t'' + t = 10^h 47^m 45^s.6$$

$$\text{Observed time} = 10 \quad 45 \quad 53.3$$

$$\text{Longitude of place} = 1^m 52^s.3 \text{ west.}$$

### XIX. *Formulae for Probable Error and Precision.*

1. Let  $n, n',$  etc., = the results found by observation.

$x$  = their arithmetical mean; or the result deduced from these by the method of least squares,

$E_2$  = (mean error),

$E_1$  = (mean error)<sup>1</sup> = arithmetical mean without regard to sign,

$m$  = the number of observations,

$r$  = probable error of a single observation,  $n, n',$  etc.,

$R$  = probable error of final result,  $x$ ,

$h$  = measure of exactness of a single observation  $n, n',$

$H$  = measure of exactness of final result,  $x$ ,

$w$  = probable error of an observation assumed as the standard of excellence,

$p, p',$  etc., = the weights of the determinations of several variables,

$\Sigma$  = symbol representing the sum,

$$E_2 = \sqrt{\frac{\Sigma (x - n)^2}{m - 1}} \quad E_1 = \frac{\Sigma (x - n)}{m - 1}$$

$$r = 0.674489 E_2 \quad r = 0.845347 E_1$$

$$h = \frac{0.469360}{r} \quad H = h \sqrt{m}$$

$$R = \frac{r}{\sqrt{m}}$$

2. By the *weight* of any determination, is meant its relative approximation to the true value.

It may be measured by the number of equally good observations (one of which is assumed to represent the unit of excellence) necessary to give a result equally near the true value.

The weights of two determinations are to each other in the direct proportion of the squares of their relative measures of exactness, and in the inverse proportion of the squares of their probable errors:

$$p = \frac{w^2}{r^2}, \quad p' = \frac{w^2}{r'^2}$$

and calling the weight of any function of the two determinations, whose weights are  $p$  and  $p'$ ,

$$P = \frac{pp'}{p + p'}$$

the probable error of the value of the function is

$$R' = \frac{w}{P} = \sqrt{r'^2 + r^2}$$

If the index or measure of precision vary as any element  $v$ , involved in any given determination,

or  $h : h' :: v : v' \dots h' = \frac{h v'}{v}$ , then will the weight become (see page 230.)

$$P = \frac{p p' v'^2}{p + p'},$$

If there be but a single variable, and this has been found by different examinations, giving the values of  $a, a', a''$ , etc., with probable errors  $r, r', r''$ , etc., or the weights  $p$ ,

$p', p'',$  etc.; and we seek to find from them the most probable value of  $x$ ,

$$x = \frac{a p + a' p' + a'' p'' + \text{etc.}}{p + p' + p'' + \text{etc.}} = \frac{\frac{a}{p^2} + \frac{a'}{p'^2} + \frac{a''}{p''^2} + \text{etc.}}{\frac{1}{p^2} + \frac{1}{p'^2} + \frac{1}{p''^2} + \text{etc.}};$$

Its weight

$$P = p + p' + p'' + \text{etc.};$$

Its probable error

$$R'' = \frac{1}{\sqrt{\frac{1}{p^2} + \frac{1}{p'^2} + \frac{1}{p''^2} + \text{etc.}}}$$

*Position of some of the principal Observatories, etc.*

| PLACE.                   | Latitude North. | LONGITUDE                           |            |                                    |            |                        |  | AUTHORITIES. |
|--------------------------|-----------------|-------------------------------------|------------|------------------------------------|------------|------------------------|--|--------------|
|                          |                 | From the Observatory at Washington. |            | From the Observatory at Greenwich. |            |                        |  |              |
|                          |                 | In time.                            | In arc.    | In time.                           | In arc.    |                        |  |              |
|                          | O ° ' "         | H M S                               | O ° ' "    | H M S                              | O ° ' "    |                        |  |              |
| Greenwich Observatory    | 51 28 38.2      | E. 5 08 11.2                        | 77 02 48.0 | .....                              | .....      | Am. Naut. Alm., (1855) |  |              |
| Paris                    | 48 50 13.2      | E. 5 17 32.7                        | 79 23 09.9 | E. 0 09 21.5                       | 2 20 21.9  |                        |  |              |
| Cambridge, Mass.         | 42 22 48.6      | E. 0 23 41.5                        | 5 55 23.1  | W. 4 44 29.6                       | 71 07 24.9 | "                      |  |              |
| Cincinnati, Ohio,        | 39 05 54.0      | W. 0 29 46.9                        | 7 26 42.8  | W. 5 37 58.0                       | 84 29 30.8 | "                      |  |              |
| Georgetown, D. C.,       | 38 54 26.1      | W. 0 00 06.2                        | 0 01 33.0  | W. 5 08 17.4                       | 77 04 21.0 | "                      |  |              |
| Hudson, Ohio,            | 41 14 42.6      | W. 0 17 32.1                        | 4 23 00.9  | W. 5 25 43.3                       | 81 25 48.9 | "                      |  |              |
| Philadelphia             | 39 57 07.5      | E. 0 07 33.6                        | 1 53 24.6  | W. 5 00 37.6                       | 75 09 23.4 | "                      |  |              |
| Washington               | 38 53 39.3      | .....                               | .....      | W. 5 08 11.2                       | 77 02 48.0 | "                      |  |              |
| Washington, Capitol..... | 38 53 19.9      | E. 0 00 10.2                        | 0 02 33.0  | W. 5 08 01.0                       | 77 00 15.0 | Coast Survey (1852)    |  |              |



|                                        |                                                         |               |
|----------------------------------------|---------------------------------------------------------|---------------|
| Falls St. Anthony, U. S. Cottage,      | Lat. = 44° 58' 40"                                      | Nicellet.     |
|                                        | Lon. = 6 <sup>h</sup> 12 <sup>m</sup> 42 <sup>s</sup>   | "             |
| Fort Leavenworth, Landing . . . . .    | Lat. = 39° 31' 14"                                      | Emory.        |
|                                        | Lon. = 6 <sup>h</sup> 18 <sup>m</sup> 56 <sup>s</sup>   | Nicollet.     |
| Council Bluffs . . . . .               | Lat. = 41° 25' 04"                                      | Graham.       |
|                                        | Lon. = 6 <sup>h</sup> 22 <sup>m</sup> 55.5 <sup>s</sup> | "             |
| Fort Gibson, old block house . . . . . | Lat. = 35° 47' 34".8                                    | Woodruff.     |
|                                        | Lon. = 6 <sup>h</sup> 21 <sup>m</sup> 00.9 <sup>s</sup> | "             |
| San Antonio, Texas . . . . .           | Lat. = 29° 25' 22".0                                    | Johnston.     |
|                                        | Lon. = 6 <sup>h</sup> 33 <sup>m</sup> 57 <sup>s</sup>   | "             |
| Paso del Norte, Plaza . . . . .        | Lat. = 31° 44' 16"                                      | Salazar.      |
|                                        | Lon. = 7 <sup>h</sup> 05 <sup>m</sup> 15 <sup>s</sup>   | "             |
| Frontera, White's rancheria . . . . .  | Lat. = 31° 48' 39"                                      | Whipple.      |
|                                        | Lon. = 7 <sup>h</sup> 05 <sup>m</sup> 54 <sup>s</sup>   | "             |
| Santa Fé . . . . .                     | Lat. = 35° 41' 06"                                      | Emory.        |
|                                        | Lon. = 7 <sup>h</sup> 04 <sup>m</sup> 10 <sup>s</sup>   | "             |
| Bent's Fort . . . . .                  | Lat. = 38° 02' 22"                                      | Fremont.      |
|                                        | Lon. = 6 <sup>h</sup> 54 <sup>m</sup> 13.3 <sup>s</sup> | "             |
| Fort Laramie . . . . .                 | Lat. = 42° 12' 10"                                      | Fremont.      |
|                                        | Lon. = 6 <sup>h</sup> 53 <sup>m</sup> 10.9 <sup>s</sup> | "             |
| Fort Hall . . . . .                    | Lat. = 43° 01' 30"                                      | Fremont.      |
|                                        | Lon. = 7 <sup>h</sup> 29 <sup>m</sup> 59.6 <sup>s</sup> | "             |
| San Diego, Coast Survey obs'y,         | Lat. = 32° 41' 57".9                                    | Coast Sur'y,  |
|                                        | Lon. = 7 <sup>h</sup> 48 <sup>m</sup> 53.4 <sup>s</sup> | Rep't of '51. |
| Point Conception C. S. obs'y,          | Lat. = 34° 26' 56".3                                    | Coast Sur'y,  |
|                                        | Lon. = 8 <sup>h</sup> 01 <sup>m</sup> 42.2 <sup>s</sup> | Rep't of '51. |
| Point Pinos, Coast Survey obs'y        | Lat. = 36° 37' 59".8                                    | Coast Sur'y,  |
|                                        | Lon. = 8 <sup>h</sup> 07 <sup>m</sup> 37.4 <sup>s</sup> | Rep't of '51. |
| San Francisco, Presidio Hill . . . . . | Lat. = 37° 47' 35".6                                    | Coast Sur'y,  |
|                                        | Lon. = 8 <sup>h</sup> 09 <sup>m</sup> 47.2 <sup>s</sup> | Rep't of '51. |

Longitudes west from Greenwich.

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